| | Population Mean | Regression Slope Coefficient |
|--|---|--|
| The true value you're interested in | μ | β1 |
| What you say | Is the true mean of the variable Y really \mu,y0? | Does my independent variable have any effect on my dependent variable? Does my X variable have any effect on my Y variable? Does the slope coefficient on X have a value different than zero meaning no effect at all? Is β1 equal to zero? |
| The stated hypotheses | H_0 : E(Y) = µ_y,0 H_a: E(Y) ≠µ_y,0 (or H_1) | H_0 :β1=0 H_a: β1 ≠0 (or H_1) |
| How you'll estimate the true value: your estimator | Ybar = sum i=1 to n (Y_i) / n | β1hat = (sum (xi - xbar)* (yi- ybar)) / sum (xi- xbar)^2 |
| Step 1 | Compute standard error of your estimator. (A measure of the standard deviation of the sampling distribution of your *estimator*) SE(Ybar)= ohat_Ybar = s_y / sqrt(n) (sample std dev / sqrt sample size) | Compute the standard error of β 1hat. It's this crazy thing: σ hat_ β 1hat ^2 = 1/n * (1/(n-2)sum(xi=xbar)^2*ubari^2) / (1/n * sum(xi-xbar)^2) ^2. Alternativelyjust let Stata do it for you. |
| Step 2 | Compute the t-statistic. t = (Ybar - $\mu_y,0$)/(SE(Ybar)). Ok, so Ybar is from data, SE(Ybar) is from data, where is μ from? From your hypothesis! | Compute the t-statistic. t = (β 1hat - 0)/ SE(β 1hat) |
| Step 3 | Compute the p-value. The probability that you'd observe that Ybar in the distribution of the Ybar estimator. The probability left in the two tails given that t-value. Use the appendix tables, OR, if you just care if it's significant at the 5% level, just check if it's bigger than 1.96. | Compute the p-value. Same way you'd do it, except let's just let Stata do it. Reject if the t-value is greater than 1.96 for a 5% significance level. (95% confidence, 5% significance) |
| Optional Step 4 | Compute a confidence interval for your true value by figuring out the range for your estimator. 1. The set of values that cannot be rejected using a two-sided hypothesis test with 5% sig. 2. Interval that has 95% probability of containing the true μ value. 95% CI for μ Y = {Ybar ± 1.96 SE(Ybar)} | Compute a confidence interval. 95% CI for $\beta 1 = \{\beta 1 \text{hat } \pm 1.96 \text{ SE}(\beta 1 \text{hat})\}$. Because $\beta 1$ is a slope, you can also create a CI for a change in X. Multiply the sides of the CI by the change in x. ($\beta 1 \text{hat} + 1.96 \text{ *SE}(\beta 1 \text{hat})$)* Δx |