

What is the Dark Matter?

Standard Model Particles and Hot Dark Matter

Could It Be Standard Model Particles?

- Our best fit for all our parameters:
- What is all that dark matter?
- If it is standard model particles, it must be stable
- Only stable particles are:
 - Protons and neutrons (and their anti-particles)
 - Electrons (and their anti-particles)
 - Photons
 - All three neutrinos
- Photons are easy to detect – we can see them
- Because universe is charge neutral, every electron is associated with a proton
 - Which makes their mass irrelevant
- We therefore narrow it down to baryons or neutrinos

$$\Omega_b = 0.0490 \pm 0.0010$$

$$\Omega_d = 0.2607 \pm 0.0053$$

$$\Omega_\Lambda = 0.6889 \pm 0.0056$$

Could the Dark Matter Be Baryons?

Arguments against dark matter being baryons:

- Counting baryons indicate that the estimate for identified baryons is, if anything, *smaller* than what we need
- The numbers at right are based mostly on studying the CMBR
- The CMBR was generated at recombination
- You can't stuff baryons in white dwarfs, etc., made later
- Also, we can get an estimate by studying primordial nucleosynthesis
- And this yields the same baryon density
- Bottom line: It's very difficult to imagine it's all baryons

$$\Omega_b = 0.0490 \pm 0.0010$$

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What Do We Know About Neutrinos?

- We have clear evidence that there are three neutrinos
 - Predicted by theory
 - Indirectly measured by primordial nucleosynthesis
 - Directly measured by studying decay of Z-boson

$$\Omega_b = 0.0490 \pm 0.0010$$

$$\Omega_d = 0.2607 \pm 0.0053$$

$$\Omega_\Lambda = 0.6889 \pm 0.0056$$

- *Direct* measurements for neutrinos masses give only negative results

$$m_{\nu e} < 2 \text{ eV}/c^2$$

- We can best measure the neutrino corresponding to the electron

$$m_2^2 - m_1^2 \approx (7.4 \pm 0.1) \times 10^{-5} \text{ eV}^2 / c^4 ,$$

- *Indirect* observations can only measure some *differences* between neutrino masses

$$|m_3^2 - m_1^2| \approx (2.48 \pm 0.04) \times 10^{-3} \text{ eV}^2 / c^4$$

- The smallest the masses could be: $m_1 \approx 0, \quad m_2 \approx 0.009 \text{ eV}/c^2, \quad m_3 \approx 0.050 \text{ eV}/c^2$

$$m_1 \approx m_2 \approx m_3 \approx 1.1 \text{ eV}/c^2$$

- The largest the masses could be:

- Sum of masses

$$0.06 \text{ eV} < \sum_{i=1}^3 m_i c^2 < 3.3 \text{ eV} .$$

So Could It Be Neutrinos?

$$0.06 \text{ eV} < \sum_{i=1}^3 m_i c^2 < 3.3 \text{ eV} .$$

$$\begin{aligned}\Omega_b &= 0.0490 \pm 0.0010 \\ \Omega_d &= 0.2607 \pm 0.0053 \\ \Omega_\Lambda &= 0.6889 \pm 0.0056\end{aligned}$$

- The number density of neutrinos was computed previously

$$\boxed{T_{\nu 0} = 1.945 \text{ K}} \quad n_{\nu i} = \frac{\zeta(3)}{\pi^2} \left(\frac{k_B T_\nu}{\hbar c} \right)^3 \frac{3}{4} \cdot 2 = 1.12 \times 10^8 \text{ m}^{-3}$$

- In a homework, we then calculated the contribution to Ω

$$\Omega_\nu = \frac{8\pi G \rho_\nu}{3H_0^2} = \frac{8\pi G n_\nu}{3H_0^2 c^2} \sum_{i=1}^3 m_{\nu i} c^2 = \frac{1}{43.3 \text{ eV}} \sum_{i=1}^3 m_{\nu i} c^2 = 0.0014 - 0.076$$

- To get it to be *all* of the dark matter, we would need neutrinos of mass 3.7 eV each
- This makes it clear that neutrinos are apparently not *all* of the dark matter
- But it could still be *much* of the dark matter
- We also have to be nervous that the neutrinos might work

Hot and Cold Dark Matter

- Two generic categories of dark matter:
 - Cold dark matter is anything that froze out when it was non-relativistic
 - Hot dark matter is anything that froze out when it was relativistic
- Neutrinos are the classic example of hot dark matter
- Typically, hot dark matter will have a number density comparable to the density of photons
- They will become non-relativistic right at the time of matter-radiation equality
- No matter what they are, we will need a mass \sim few eV, depending on several details
- For definiteness, we will work out what happens if we have three neutrinos with mass 3.7 eV each

So What's Wrong With Hot Dark Matter? (1)

The list is long

- We will focus on one aspect: structure formation
- Consider the momentum of neutrinos of mass $3.7 \text{ eV}/c^2$
- At freeze out, their energy is roughly $3k_B T_\nu$ and momentum is $p = E/c = 3k_B T_\nu/c$

- At the time of matter-radiation equality, this formula still works

$$p = \frac{3k_B T_\nu}{c} = \frac{3 \cdot 0.714 k_B T}{c} = 1.63 \text{ eV}/c$$

- These are now non-relativistic, so their velocity will be

$$v = \frac{p}{m} = c \frac{pc}{mc^2} = c \frac{1.63 \text{ eV}}{3.7 \text{ eV}} = 0.44c$$

- They will therefore move a distance

$$d = vt = 0.44 (3.00 \times 10^8 \text{ m/s}) (57,000 \text{ y}) (3.156 \times 10^7 \text{ s/y}) = 2.4 \times 10^{20} \text{ m}$$

$$d = 7.7 \text{ kpc}$$

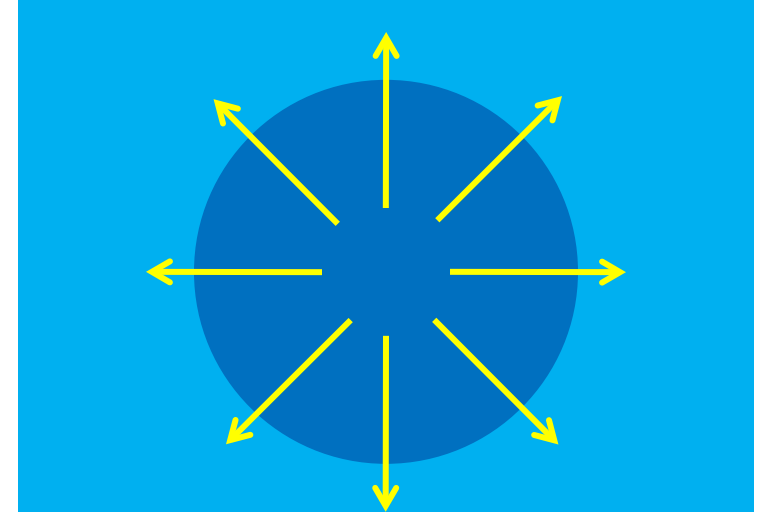
So What's Wrong With Hot Dark Matter? (2)

- Suppose at this time, there were a region smaller than this that had high density
- Neutrinos would simply run from high density region to low density
- Any scales smaller than this are wiped out
- Matter-radiation equality came at roughly $z = 3400$
- So fluctuations on this scale would have grown by a factor of 3401, and now would be of size

$$d_0 = (1+z)d = 3401(7.7 \text{ kpc}) = 26 \text{ Mpc}$$

- This is size of the Laniekea Supercluster
- Suggests superclusters formed before clusters, galaxies, or globular clusters
- But observations suggest smaller objects were probably first

$$d = 7.7 \text{ kpc}$$



Learning About Neutrinos from Cosmology

$$0.06 \text{ eV} < \sum_{i=1}^3 m_i c^2 < 3.3 \text{ eV} .$$

$$\Omega_\nu = \frac{1}{43.3 \text{ eV}} \sum_{i=1}^3 m_{\nu i} c^2$$

$$\Omega_b = 0.0486$$

$$\Omega_d = 0.2589$$

$$\Omega_\Lambda = 0.6911$$

$$\Omega_\nu = 0.0014$$

- If mass sum is $11 \text{ eV}/c^2$, all dark matter would be neutrinos
 - But it doesn't lead to a universe that looks like ours
- If mass sum is $3.3 \text{ eV}/c^2$, a significant fraction of dark matter would be neutrinos
- How low can we make the neutrino masses and lead to a universe that looks like ours?
- Assume a specific neutrino mass sum
- Predict large scale structure and small angular CMBR variations
- Match to experiment
- We find

$$\sum_{i=1}^3 m_{\nu i} c^2 < 0.13 \text{ eV}$$

- This gives us limits on Ω_ν

$$0.0014 < \Omega_\nu < 0.0030$$

- Normally assumed to be near the lower end of this limit

Cold Dark Matter

Annihilation of Cold Dark Matter

- We have ruled out hot dark matter
 - Matter which fell out of equilibrium before it became non-relativistic
- Now consider cold dark matter
 - Matter which was non-relativistic when it fell out of equilibrium
- It must be stable (or very long-lived) particles that are not in the standard model
- Call the particle X and its mass m_X
- Like all particles, it must have an anti-particle X -bar
 - Though the anti-particle could be the same particle
- Generally, when particles combine with anti-particles, they can annihilate:

$$X\bar{X} \rightarrow e^+e^- \quad \text{if not its own anti-particle}$$

$$XX \rightarrow e^+e^- \quad \text{if it is its own anti-particle}$$

- So why didn't they all annihilate when $3k_B T$ drops below m_X ?

What Stops the Annihilation Process?

$X\bar{X} \rightarrow e^+e^-$ if not its own anti-particle

$XX \rightarrow e^+e^-$ if it is its own anti-particle

- There are two reasons this process could stop:
- There is an excess of X 's over anti- X 's
 - This only makes sense if X 's and anti- X 's are distinct
- The X 's and anti- X 's become so low in density that they have trouble finding each other
 - Makes sense in either case
- If it's the former, we can't really figure out how many there should be left
- If it's the latter, then the process should stop when the average X collides only once in the age of the universe with its anti-particles
- We'll assume this second case

$$\boxed{\Gamma t \approx 1}$$

When Does the Annihilation Happen?

$$X\bar{X} \rightarrow e^+e^- \quad \text{or} \quad XX \rightarrow e^+e^-$$

$$\Gamma t \approx 1$$

- X particles will begin disappearing as soon as $k_B T < m_X c^2/3$
- At this point, any remaining X 's will be non-relativistic
- And so long as they remain in thermal equilibrium, their density will be proportional to

$$E = m_X c^2$$

$$n \propto \exp\left(-\frac{E}{k_B T}\right) = \exp\left(-\frac{m_X c^2}{k_B T}\right)$$

- Because we need to get rid of most, but not all of them, we need to have $k_B T$ well below $m_X c^2/3$
- We need about
 - Almost independent of mass

$$k_B T_F \approx \frac{1}{30} m_X c^2$$

- The average kinetic energy at this time is about
- Match this to the non-relativistic formula for kinetic energy
- And we have the velocity

$$E_{kin} = \frac{3}{2} k_B T_F = \frac{1}{2} m_X v^2$$

$$v = \sqrt{\frac{3k_B T_F}{m_X}}$$

Density of Dark Matter at Freezeout

$$X\bar{X} \rightarrow e^+e^- \quad \text{or} \quad XX \rightarrow e^+e^-$$

$$\boxed{\Gamma t \approx 1}$$

$$\boxed{v = \sqrt{\frac{3k_B T_F}{m_X}}}$$

- The rate at which any collision occurs is

$$\Gamma = n_X \sigma(\Delta v)$$

- n is number density
- σ is cross-section
- Δv is relative velocity

$$t = \frac{2.42 \text{ s}}{\sqrt{g_{\text{eff}}}} \left(\frac{\text{MeV}}{k_B T_F} \right)^2$$

- We also know the time-temperature relationship
- Freezeout occurs when density has dropped to the point where

$$1 = \Gamma t = n_F \sigma(\Delta v) t = n_F \sigma \sqrt{\frac{3k_B T_F}{m_X}} \frac{2.42 \text{ s}}{\sqrt{g_{\text{eff}}}} \left(\frac{\text{MeV}}{k_B T_F} \right)^2 = n_F \sigma \frac{4.19 \text{ s} \cdot \text{MeV}^2}{\sqrt{g_{\text{eff}} m_X} (k_B T_F)^{3/2}}$$

- Solve for n_F :

$$n_F = \frac{\sqrt{g_{\text{eff}} m_X} (k_B T_F)^{3/2}}{\sigma (4.19 \text{ s} \cdot \text{MeV}^2)}$$

- Multiply n_F by m_X to get the density:

$$\rho_d = n_F m_X = \frac{\sqrt{g_{\text{eff}}} (k_B T_F m_X)^{3/2}}{\sigma (4.19 \text{ s} \cdot \text{MeV}^2)}$$

The Current Dark Matter Density

- We have the density at this time

$$\rho_d = \frac{\sqrt{g_{\text{eff}}} (k_B T_F m_X)^{3/2}}{\sigma (4.19 \text{ s} \cdot \text{MeV}^2)}$$

$$k_B T_F \approx \frac{1}{30} m_X c^2$$

- But the universe has continued to expand
 - Roughly $a \sim T^{-1}$
 - So density $\rho \sim T^3$

$$\rho_{d0} = \rho_d \left(\frac{T_0}{T_F} \right)^3 \cdot \frac{3.36}{g_{\text{eff}}} = \frac{0.802 (k_B T_0)^3}{\sigma \sqrt{g_{\text{eff}}} (\text{s} \cdot \text{MeV}^2)} \left(\frac{m_X}{k_B T_F} \right)^{3/2}$$

- So we have roughly

$$\frac{m_X}{k_B T_F} \approx \frac{30}{c^2}$$

- Small correction because of reheating as various particles annihilated

- Substitute the various quantities in:

$$\rho_{d0} = \frac{0.802 \left[(8.617 \times 10^{-5} \text{ eV/K}) (2.725 \text{ K}) \right]^3 30^{3/2}}{\sigma \sqrt{g_{\text{eff}}} (\text{s} \cdot 10^{12} \text{ eV}^2) (3.00 \times 10^8 \text{ m/s})^3} \cdot 1.602 \times 10^{-19} \text{ J/eV}$$

- Note that the mass has cancelled out
 - The only real unknown here is g_{eff}

$$\rho_{d0} = \frac{1.102 \times 10^{-65} \text{ kg/m}}{\sigma \sqrt{g_{\text{eff}}}}$$

The Annihilation Cross Section

- If we knew the cross-section, we could predict the current density

$$\rho_{d0} = \frac{1.102 \times 10^{-65} \text{ kg/m}}{\sigma \sqrt{g_{\text{eff}}}}$$

- But we know the current density

$$\rho_{d0} = 2.235 \times 10^{-27} \text{ kg/m}^3$$

- Turn this around and get the current cross-section

$$\sigma = \frac{1.102 \times 10^{-65} \text{ kg/m}}{\rho_d \sqrt{g_{\text{eff}}}}$$

- Exact value will depend g_{eff}
 - Which depends on number of particles at these unknown high energy

- For definiteness, let's pick $g_{\text{eff}} = 100$

$$\sigma = \frac{1.102 \times 10^{-65} \text{ kg/m}}{(2.235 \times 10^{-27} \text{ kg/m}^3) \sqrt{100}}$$

- This value is probably accurate to about a factor of two

$$\boxed{\sigma \approx 4.5 \times 10^{-40} \text{ m}^2}$$

What is the Mass of the Dark Matter Particle?

$$\boxed{\sigma \approx 4.5 \times 10^{-40} \text{ m}^2}$$

$$X\bar{X} \rightarrow e^+e^- \quad \text{or} \quad XX \rightarrow e^+e^-$$

- We have a pretty good idea of the cross-section
 - And we know it isn't any standard model particle
- Typical cross-sections depend on particle physics model, but ...

- Usually such cross sections look something like:

$$\sigma \approx \frac{\alpha_X^2 \hbar^2}{M^2 c^2}$$

- The factor α_X is a dimensionless *coupling constant*

- Typical values in most theories have $\alpha_X \sim 10^{-2} - 1$
 - Electromagnetism, for example, has $\alpha = 1/137$

$$\sigma \leq 4\pi \left(\frac{\hbar}{p} \right)^2$$

- There is also an approximate upper limit on the cross section
- Put this all together and you can get a range on the mass of the X :

$$10^2 \text{ GeV} < m_X c^2 < 10^5 \text{ GeV}$$

So What Is the Dark Matter?

$$\boxed{\sigma \approx 4.5 \times 10^{-40} \text{ m}^2}$$

$$10^2 \text{ GeV} < m_X c^2 < 10^5 \text{ GeV}$$

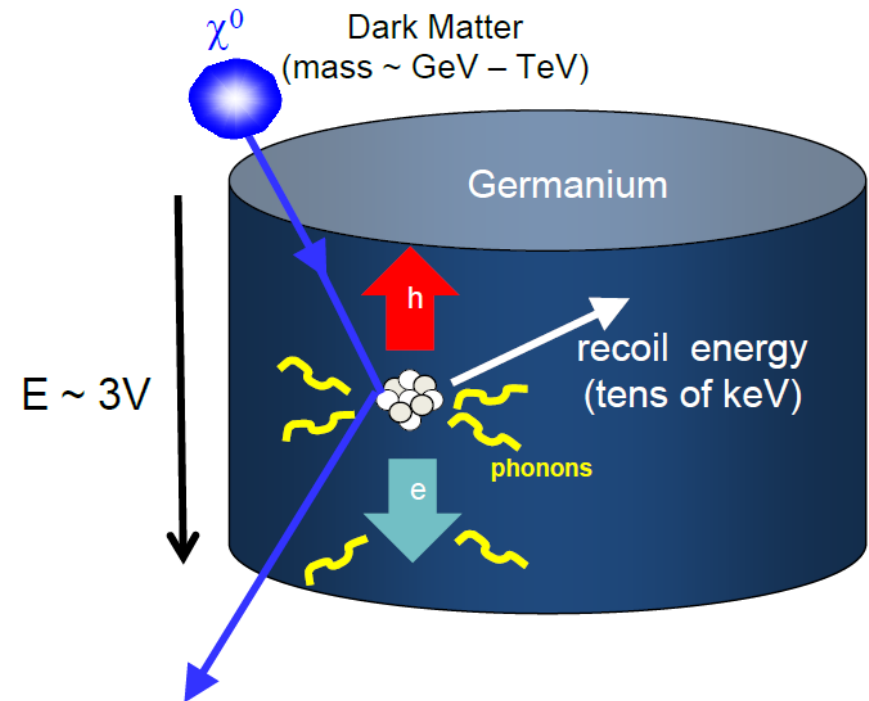
- Supersymmetry is supposed to have particle called the *Lightest Superpartner* that is both stable and can annihilate to ordinary particles
- It is predicted to be probably around $10^2 - 10^4 \text{ GeV}$
- It should be *perfect* for the dark matter
- But thus far, all such searches have been unsuccessful
 - So probably it is somewhat above 10^3 GeV
- Other theories contain massive particles that have only weak interactions
 - WIMPs = Weakly Interacting Massive Particles
- There are countless other candidate theories for the dark matter

Can We Detect the Dark Matter?

$$\sigma \approx 4.5 \times 10^{-40} \text{ m}^2$$

$$10^2 \text{ GeV} < m_X c^2 < 10^5 \text{ GeV}$$

- If it is lighter than a few TeV, we should find it soon
 - LHC operates at 7 TeV + 7 TeV
- But not sure how to discover it
- We can also look for collisions of the dark matter with ordinary nuclei
 - Should happen for WIMPs
 - Thus far, no detection
- It is also possible we will some day discover annihilation products from the remaining dark matter particles



$$X\bar{X} \rightarrow \gamma\gamma$$

Other Dark Matter Candidates

Is it Necessarily Cold Dark Matter?

- We discussed hot and cold dark matter
- We ruled out hot dark matter and therefore concluded it must be cold dark
 - But there may be other, even better alternatives
- How well does cold dark matter work?
- So well that the standard cosmological model is called the Λ CDM model
- But not perfectly!
- Many aspects of galaxy formation are fudged – they include factors that are poorly understood
- Also, most simulations indicate that dark matter should cluster more strongly towards the center of galaxies
- May indicate that we have some important details wrong

Random Examples of Crazy Dark Matter Ideas

- Countless alternatives have been proposed over the years
- Many of them have been tested and found wanting
- When you eliminate those, the list gets shorter
- One idea that is currently popular is warm dark matter
 - Particles were slightly non-relativistic when they froze out
- An example would be sterile neutrinos with mass \sim few keV/ c^2 or so
 - Neutrinos with little or no weak interactions
- Bottom line – we don't really know what the dark matter is
- ~~Eric D. Carlson, Marie E. Machacek, and Lawrence J. Hall, “Self Interacting Dark Matter,” Astrophys. J. 398, 43 (1992)~~
- ~~Eric D. Carlson, Rahim Esmailzadeh, Lawrence J. Hall, and Stephen D. H. Hsu, “Black Hole Nucleosynthesis and $\Omega_B = 1$,” Phys. Rev. Lett. 65, 2225 (1990).~~
- ~~Eric D. Carlson and L.J. Hall, “ ν_μ and ν_τ as dark matter,” Phys. Rev. D40, 3187 (1989).~~