**Problem 1.** Suppose f(x) is a continuous function satisfying

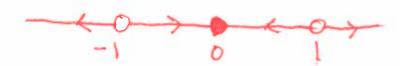
1. 
$$f(-1) = 0$$

2. 
$$f(0) = 0$$
,

3. 
$$f(1) = 0$$
,

$$4. \lim_{x\to\infty} f(x) = \infty.$$

If the system  $\dot{x} = f(x)$  has no semi-stable fixed points, sketch a phase portrait for this system.



**Problem 2.** Suppose f(x) is a continuous function satisfying

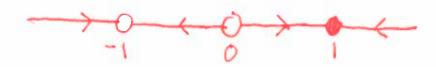
1. 
$$f(-1) = 0$$

2. 
$$f(0) = 0$$
,

3. 
$$f(1) = 0$$
,

4. 
$$f'(0) = 1$$
.

If the system  $\dot{x} = f(x)$  has no semi-stable fixed points, sketch a phase portrait for this system.



## **Instructor: John Gemmer**

**Problem 1.** Suppose f(x) is a continuous function satisfying

1. 
$$f(-1) = 0$$

2. 
$$f(0) = 0$$
,

3. 
$$f(1) = 0$$
,

$$4. \lim_{x \to \infty} f(x) = -\infty.$$

If the system  $\dot{x} = f(x)$  has no semi-stable fixed points, sketch a phase portrait for this system.



**Problem 2.** Suppose f(x) is a continuous function satisfying

1. 
$$f(-1) = 0$$

2. 
$$f(0) = 0$$
,

3. 
$$f(1) = 0$$
,

4. 
$$f'(0) = -1$$
.

If the system  $\dot{x} = f(x)$  has no semi-stable fixed points, sketch a phase portrait for this system.

