

Announcements

1. Tentatively changed schedule; postponing first exam – Tuesday, Sept. 30th
2. HW 1 and HW 2 WebAssign sets due today before midnight
3. Summary of 1-dimensional motion relationships
4. Today's lecture – vectors
 - a. What are they and what do they have to do with us?
 - b. How to combine them – adding and subtracting
 - c. How to multiply them & why would we want to

Displacement, velocity, and acceleration:

1. Displacement $x(t) = \int_0^t dt' v(t') = \int_0^t dt' \int_0^{t'} dt'' a(t'')$

2. Velocity $v(t) = \frac{dx(t)}{dt} = \int_0^t dt' a(t')$

3. Acceleration $a(t) = \frac{dv(t)}{dt}$

Special case of constant acceleration: $a(t) = a_0$
(assume that initial time is $t=0s$)

$$v(t) = v_0 + a_0 t$$

$$x(t) = x_0 + v_0 t + \frac{1}{2} a_0 t^2 = x_0 + \frac{1}{2} (v_0 + v(t)) t$$

$$(v(t))^2 = (v_0)^2 + 2 a_0 (x(t) - x_0)$$

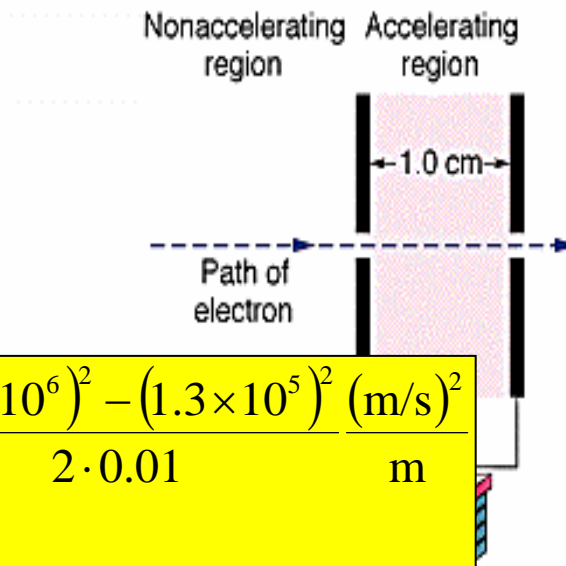
$$v(t) = v_0 + a_0 t$$

$$x(t) = x_0 + v_0 t + \frac{1}{2} a_0 t^2 = x_0 + \frac{1}{2} (v_0 + v(t)) t$$

$$(v(t))^2 = (v_0)^2 + 2 a_0 (x(t) - x_0)$$

5. HRWG 2.P.029. [52220] An electron with initial velocity $v_0 = 1.3 \times 10^5 \text{ m/s}$ enters a region 1.0 cm long where it is electrically accelerated (Fig. 2-25). It emerges with velocity $v = 5.90 \times 10^6 \text{ m/s}$. What was its acceleration, assumed constant? (Such a process occurs in the electron gun in a cathode-ray tube, used in television receivers and oscilloscopes.)

[0.0952381] m/s^2



$$a_0 = \frac{v(t)^2 - v_0^2}{2(x(t) - x_0)} = \frac{(5.9 \times 10^6)^2 - (1.3 \times 10^5)^2 \text{ (m/s)}^2}{2 \cdot 0.01 \text{ m}}$$

$$= 1.7 \times 10^{15} \text{ m/s}^2$$

Figure 2-25

$$v(t) = v_0 + a_0 t$$

$$\rightarrow a_0 = -g = -9.8 \text{ m/s}^2$$

$$x(t) = x_0 + v_0 t + \frac{1}{2} a_0 t^2 = x_0 + \frac{1}{2} (v_0 + v(t)) t$$

$$(v(t))^2 = (v_0)^2 + 2 a_0 (x(t) - x_0)$$

8. HR006 2.P.054. [52229] A basketball player, standing near the basket to grab a rebound, jumps 90 cm vertically.

(a) How much (total) time does the player spend in the top 25 cm of this jump?

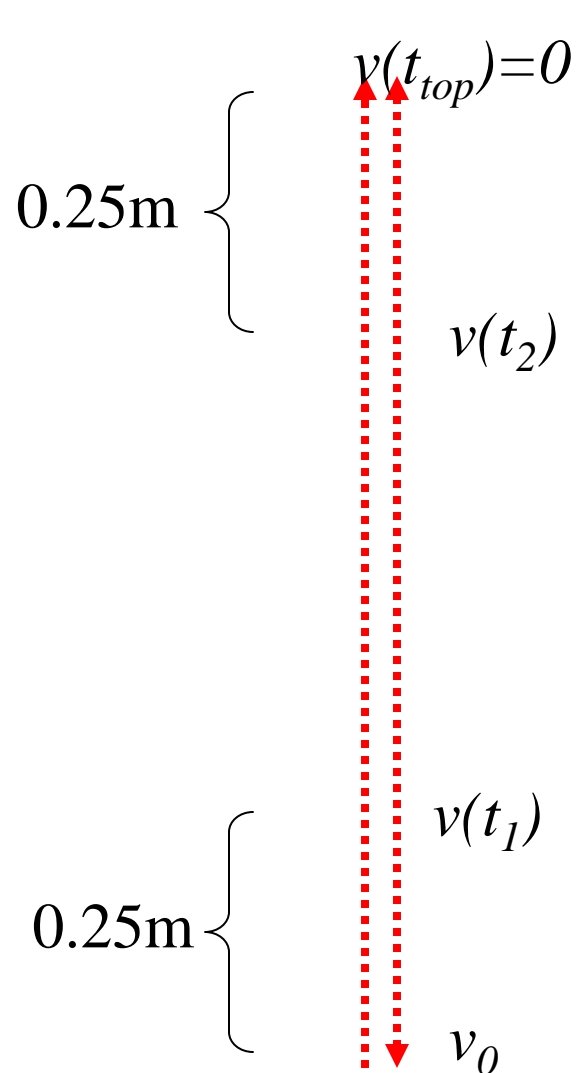
[0.0952381] ms

(b) How much (total) time does the player spend in the bottom 25 cm of this jump?

[0.0952381] ms

Does this help explain why such players seem to hang in the air at the tops of their jumps?

- No, it is an optical illusion and they spend the same amount of time at the tops and bottoms of their jumps.
- No, it is an optical illusion and they spend less time at the tops of their jumps.
- Yes, they spend more time at the tops of their jumps. [0.0952381]



$$v(t) = v_0 - g t$$

$$x(t) = x_0 + v_0 t - \frac{1}{2} g t^2$$

$$(v(t))^2 = (v_0)^2 - 2 g (x(t) - x_0)$$

$$v(t_{top})^2 = v(t_2)^2 - 2g(x(t_{top}) - x(t_2))$$

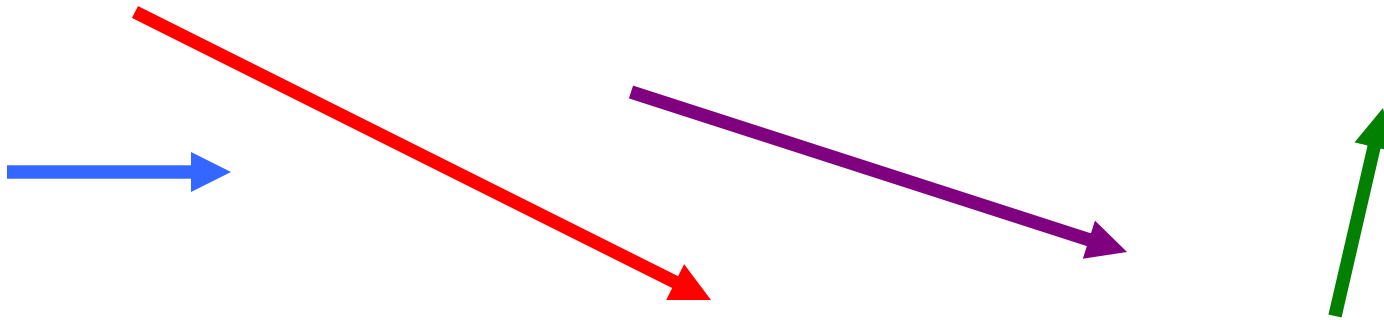
$$v(t_2) = \pm \sqrt{2 \cdot 9.8 \cdot 0.25} \text{ m/s} = \pm 2.2135 \text{ m/s}$$

$$= v(t_{top}) - 9.8(t_2 - t_{top})$$

$$(t_2 - t_{top}) = \frac{2.2135}{9.8} \text{ s} = 0.2258 \text{ s}$$

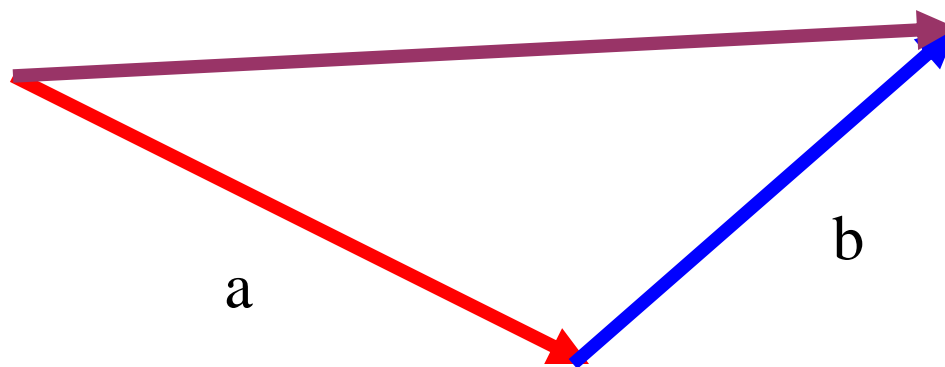
Definition of a vector

1. A vector can be visualized its length and direction.

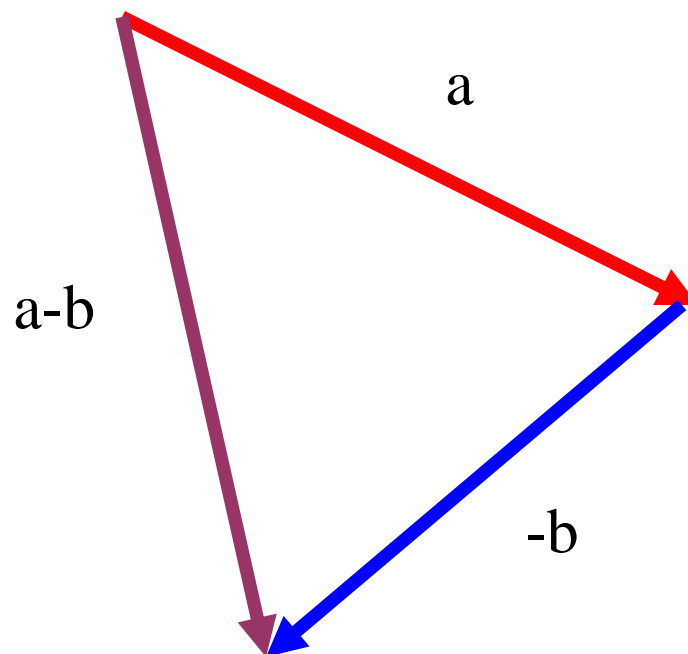


2. Addition, subtraction, and two forms of multiplication can be defined
3. Coordinate representations, and abstract extensions.

Vector addition:

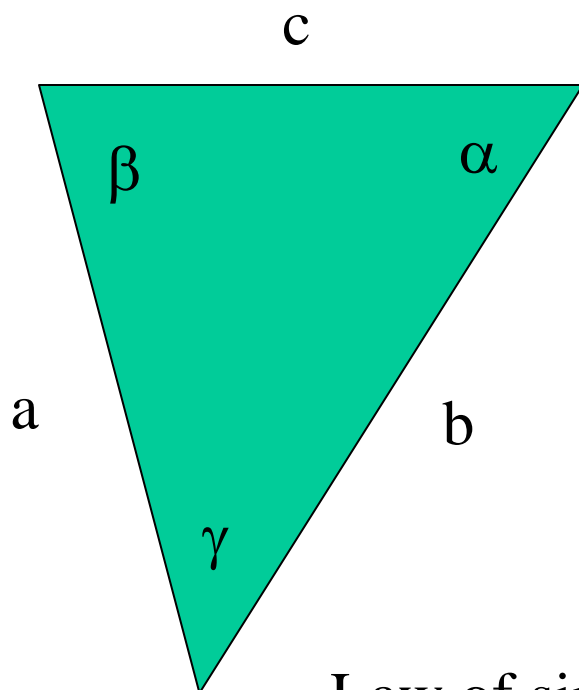


Vector subtraction:



Some useful trigonometric relations

(see Appendix E of your text)



Law of cosines:

$$a^2 = b^2 + c^2 - 2bc \cos \alpha$$

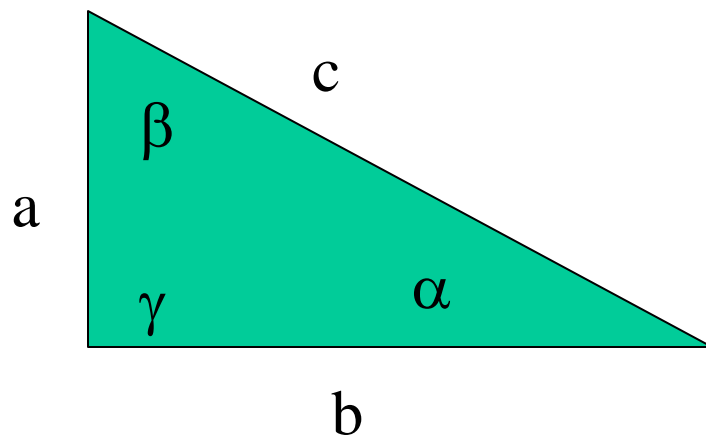
$$b^2 = c^2 + a^2 - 2ca \cos \beta$$

$$c^2 = a^2 + b^2 - 2ab \cos \gamma$$

Law of sines:

$$\frac{a}{\sin \alpha} = \frac{b}{\sin \beta} = \frac{c}{\sin \gamma}$$

Right triangle relations



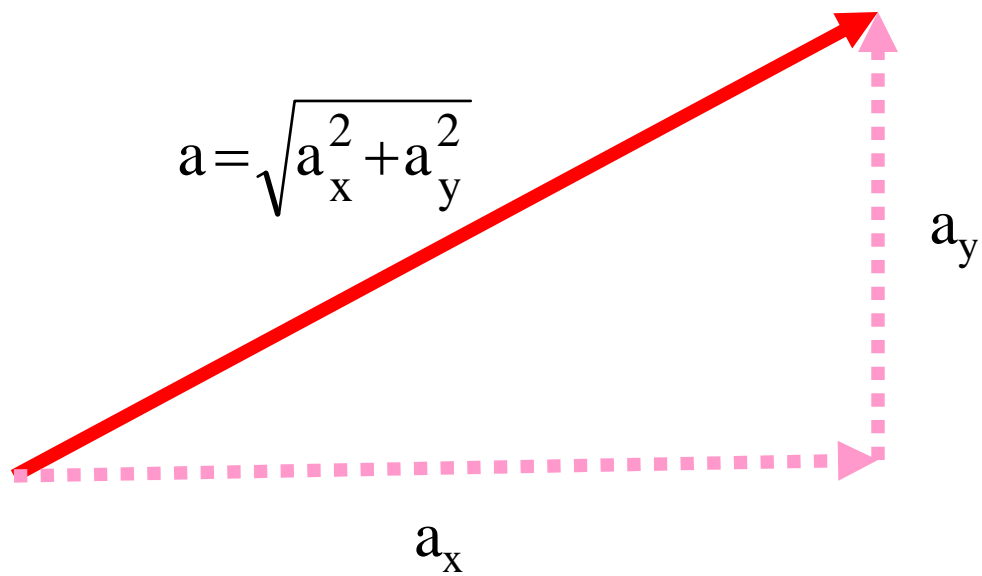
$$c = \sqrt{a^2 + b^2}$$

$$\tan \alpha = a/b$$

$$\sin \alpha = a/c$$

$$\cos \alpha = b/c$$

Vector components:



Vector components

$$\mathbf{R}_1 = x_1 \hat{\mathbf{x}} + y_1 \hat{\mathbf{y}} + z_1 \hat{\mathbf{z}}$$

$$\mathbf{R}_2 = x_2 \hat{\mathbf{x}} + y_2 \hat{\mathbf{y}} + z_2 \hat{\mathbf{z}}$$

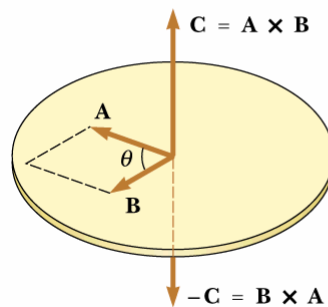
$$\mathbf{R}_1 + \mathbf{R}_2 = (x_1 + x_2) \hat{\mathbf{x}} + (y_1 + y_2) \hat{\mathbf{y}} + (z_1 + z_2) \hat{\mathbf{z}}$$

Vector multiplication

“Dot” product $\mathbf{A} \cdot \mathbf{B} \equiv AB \cos \theta_{AB}$; $\hat{\mathbf{x}} \cdot \hat{\mathbf{x}} = 1$

“Cross” product $|\mathbf{A} \times \mathbf{B}| \equiv AB \sin \theta_{AB}$; $\hat{\mathbf{x}} \times \hat{\mathbf{y}} = \hat{\mathbf{z}}$

Serway, Physics for Scientists and Engineers, 5/e
Figure 11.8



Right-hand rule



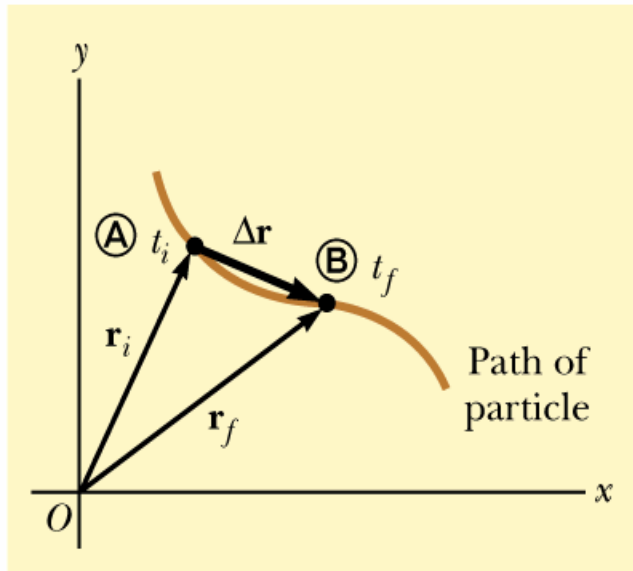
9/4/2003

Harcourt, Inc.

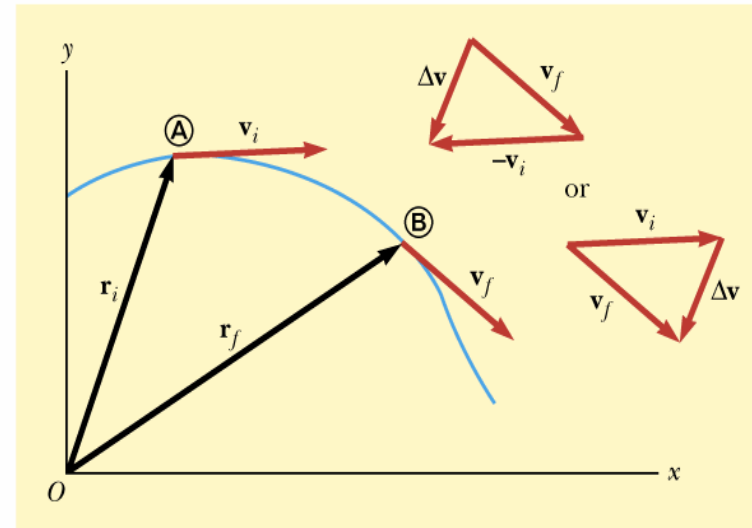
11

Examples of vectors: Position & Velocity

Serway, Physics for Scientists and Engineers, 5/e
Figure 4.1

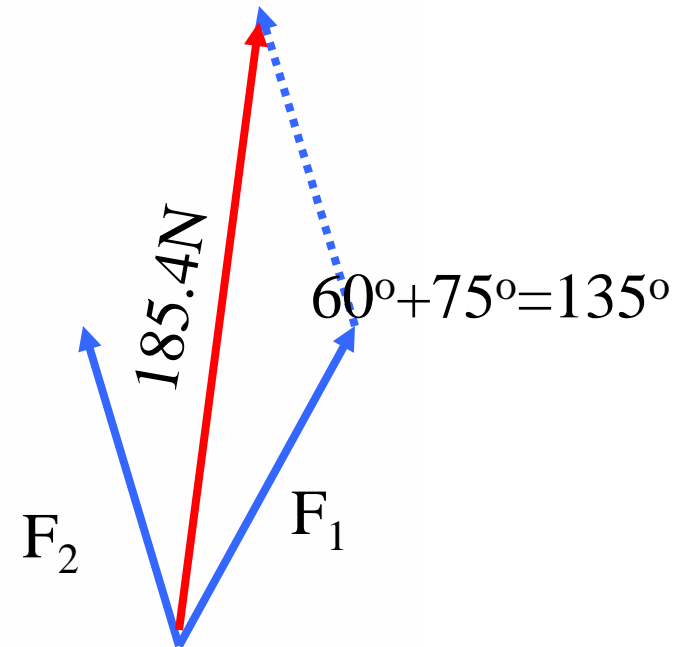
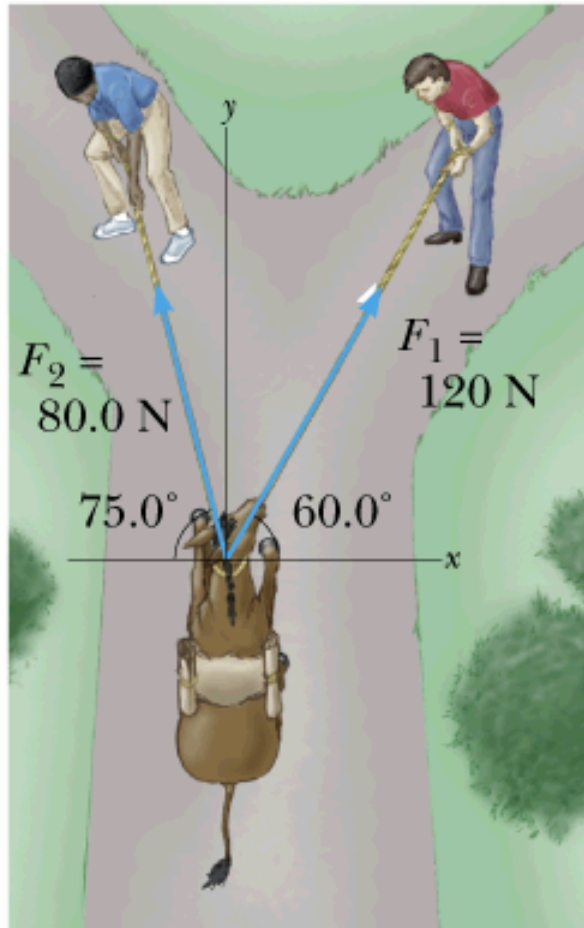


Serway, Physics for Scientists and Engineers, 5/e
Figure 4.3



Harcourt, Inc.

Harcourt, Inc.

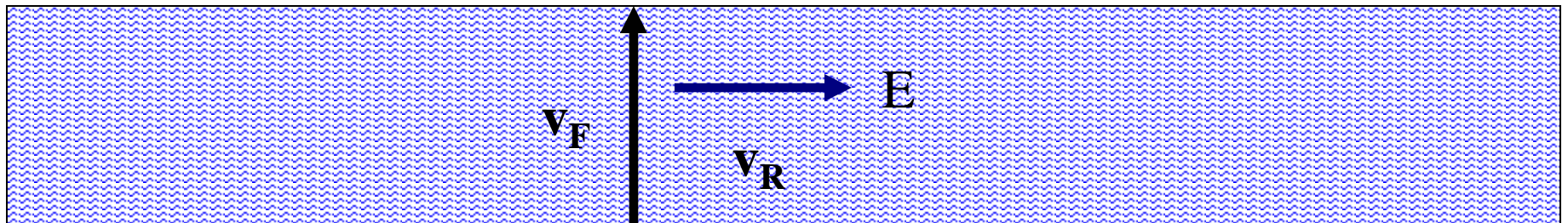


$$c^2 = a^2 + b^2 - 2ab \cos \gamma$$

Harcourt, Inc.

Peer instruction question

N



Suppose a Ferry moves due *north* at $v_F=4\text{m/s}$ across a river which is flowing *east* at a velocity of $v_R=3\text{m/s}$. What is the velocity of the Ferry relative to the water?

(a) 4m/s (north) (b) 7m/s 37° (east of north)

(c) 5m/s 37° (east of north) (d) 5m/s (west of north)