PHY 711 – Problem Set # 17

Continue reading Chapter 7 in Fetter and Walecka.

Consider the differential equation

$$\left(-\frac{d^2}{dx^2} - \lambda\right)\phi(x) = F_0 \sin\left(\frac{\pi x}{L}\right),\tag{1}$$

where $\phi(x=0)=0$ and $\frac{d\phi}{dx}(0)=0$ and where $\lambda,\,F_0$, and L are constants.

1. Show that the solution takes the form

$$\phi(x) = \frac{F_0}{\frac{\pi^2}{L^2} - \lambda} \left(\sin\left(\frac{\pi x}{L}\right) - \frac{\pi}{\sqrt{\lambda}L} \sin(\sqrt{\lambda}x) \right). \tag{2}$$

2. Use the method of Laplace transforms to verify this solution.