PHY 113 A General Physics I 9-9:50 AM MWF Olin 101

Plan for Lecture 5:

Chapter 4 - Motion in two dimensions

- 1. Position, velocity, and acceleration in two dimensions
- 2. Two dimensional motion with constant acceleration

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Note that in many of the Webassign problem sets there are some zero point "extra practice" problems set in the assignment for your consideration. 1 08/29/2012 1.2.1.6.1.13.1.20 Motion in 1d -- constant velocity 2 08/31/2012 2.1-2.3 2128 3 09/03/2012 2.4-2.8 2.13.2.16 09/07/2012 09/07/2012 4 09/05/2012 5 09/07/2012 Motion in 2d 4.1-4.3 4.3.4.50 09/10/2012 6 09/10/2012 Circular motion 4.4-4.6 4.29,4.30 09/12/2012 7 09/12/2012 Newton's laws 5.1-5.6 09/14/2012 8 09/14/2012 Newton's laws applied 5.7-5.8 09/17/2012 09/17/2012 Review 09/19/2012 Exam 9 09/21/2012 More applications of 6.1-6.4 09/24/2012 PHY 113 A Fall 2012 -- Lecture 5

In the previous lecture, we introduced the abstract notion of a vector. In this lecture, we will use that notion to describe position, velocity, and acceleration vectors in two dimensions.

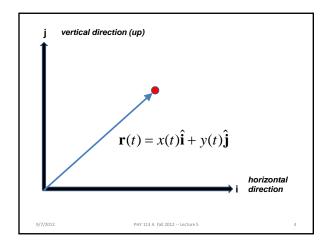
iclicker exercise:

Why spend time studying two dimensions when the world as we know it is three dimensions?

- A. Because it is difficult to draw 3 dimensions.
- B. Because in physics class, 2 dimensions are hard enough to understand.
- C. Because if we understand 2 dimensions, extension of the ideas to 3 dimensions is trivial.
- D. On Fridays, it is good to stick to a plane.

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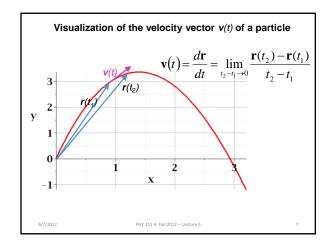
Vectors relevant to motion in two dimenstions

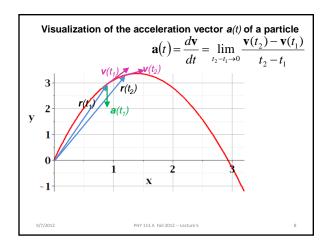
Displacement: r(t) = x(t) i + y(t) j

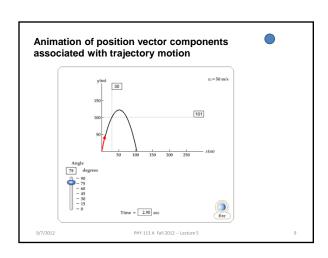
Velocity: $\mathbf{v}(t) = \mathsf{v}_{\mathsf{x}}(t) \ \mathbf{i} + \mathsf{v}_{\mathsf{y}}(t) \ \mathbf{j}$ $\mathbf{v}_{\mathsf{x}} = \frac{d\mathsf{x}}{dt} \qquad \mathbf{v}_{\mathsf{y}} = \frac{d\mathsf{y}}{dt}$

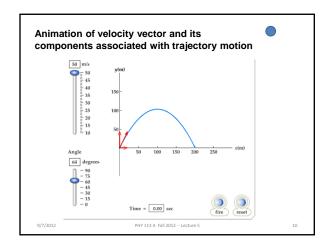
Acceleration: $\mathbf{a}(t) = \mathbf{a}_{\mathbf{x}}(t) \mathbf{i} + \mathbf{a}_{\mathbf{y}}(t) \mathbf{j}$ $\mathbf{a}_{x} = \frac{dv_{x}}{dt}$ $\mathbf{a}_{y} = \frac{dv_{y}}{dt}$

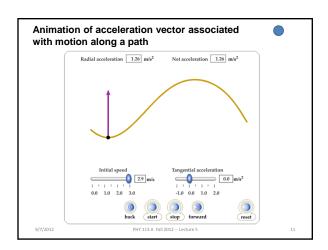
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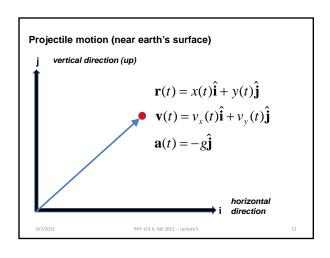












Projectile motion (near earth's surface)

$$\mathbf{r}(t) = x(t)\hat{\mathbf{i}} + y(t)\hat{\mathbf{j}}$$

$$\mathbf{v}(t) = \frac{d\mathbf{r}}{dt} = v_x(t)\hat{\mathbf{i}} + v_y(t)\hat{\mathbf{j}}$$

$$\mathbf{a}(t) = \frac{d\mathbf{v}}{dt} = -g\hat{\mathbf{j}}$$

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$$\Rightarrow \mathbf{v}(t) = \mathbf{v}_i - gt\hat{\mathbf{j}} \quad \text{note that } \mathbf{v}(t=0) = \mathbf{v}_i$$

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Projectile motion (near earth's surface)

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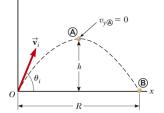
$$\mathbf{v}(t) = \frac{d\mathbf{r}}{dt} = \mathbf{v}_i - gt\hat{\mathbf{j}}$$

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$$\mathbf{v}_{i} = v_{xi}\hat{\mathbf{i}} + v_{yi}\hat{\mathbf{j}}$$

$$v_{xi} = |\mathbf{v}_i| \cos \theta_i$$

$$v_{yi} = |\mathbf{v}_i| \sin \theta_i$$



Projectile motion (near earth's surface)

Trajectory equation in vector form:

$$\mathbf{r}(t) = \mathbf{r}_i + \mathbf{v}_i t - \frac{1}{2} g t^2 \hat{\mathbf{j}}$$

$$\mathbf{v}(t) = \mathbf{v}_i - gt\hat{\mathbf{j}}$$

Trajectory equation in component form:

$$x(t) = x_i + v_{xi}t$$

$$v_{r}(t) = v_{ri}$$

$$y(t) = y_i + v_{yi}t - \frac{1}{2}gt^2$$
 $v_y(t) = v_{yi} - gt$

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Aside: The equations for position and velocity written in this way are call "parametric" equations. They are related to each other through the time parameter.

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Projectile motion (near earth's surface)

Trajectory equation in component form:

$$x(t) = x_i + v_{xi}t = x_i + v_i \cos \theta_i t$$

$$y(t) = y_i + v_{yi}t - \frac{1}{2}gt^2 = y_i + v_i \sin \theta_i t - \frac{1}{2}gt^2$$
$$v_x(t) = v_{xi} = v_i \cos \theta_i$$

$$v_{ii}(t) = v_{ii} - gt = v_i \sin \theta_i - g$$

 $v_y(t)=v_{yi}-gt=v_i\sin\theta_i-gt$ Trajectory path y(x); eliminating t from the equations:

$$t = \frac{x - x_i}{v_i \cos \theta_i} \quad y(x) = y_i + v_i \sin \theta_i \frac{x - x_i}{v_i \cos \theta_i} - \frac{1}{2} g \left(\frac{x - x_i}{v_i \cos \theta_i} \right)^2$$

$$y(x) = y_i + \tan \theta_i (x - x_i) - \frac{1}{2} g \left(\frac{x - x_i}{v_i \cos \theta_i} \right)^{\frac{1}{2}}$$

Projectile motion (near earth's surface) Summary of results

$$r(t) = r + v \cos \theta t \qquad v(t)$$

$$x(t) = x_i + v_i \cos \theta_i t$$
 $y(t) = y_i + v_i \sin \theta_i t - \frac{1}{2} g t^2$

$$v_{x}(t) = v_{i} \cos \theta_{i}$$

$$v_{y}(t) = v_{i} \sin \theta_{i} - gt$$

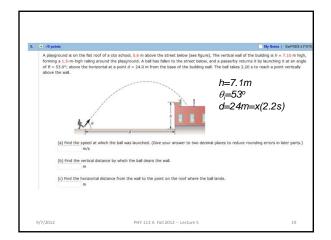
$$y(x) = y_i + \tan \theta_i (x - x_i) - \frac{1}{2} g \left(\frac{x - x_i}{v_i \cos \theta_i} \right)^2$$

iclicker exercise:

These equations are so beautiful that

- A. They should be framed and put on the wall.
- B. They should be used to perfect my tennis/golf/basketball/soccer technique.
- C. They are not that beautiful.

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Problem solving steps

- Visualize problem labeling variables
 Determine which basic physical principle(s) apply
 Write down the appropriate equations using the variables defined in
- 4. Check whether you have the correct amount of information to solve the problem (same number of known relationships and unknowns).

 5. Solve the equations.
- 6. Check whether your answer makes sense (units, order of magnitude,

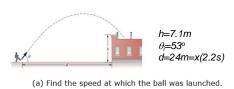


h=7.1m θ_i =53° d=24m=x(2.2s)

(a) Find the speed at which the ball was launched.

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$$x(t) = x_i + v_i \cos \theta_i t$$

$$d = x(2.2) = v_i \cos 53^{\circ} (2.2) = 24$$

$$\Rightarrow v_i = \frac{24m}{\cos 53^{\circ} (2.2s)} = 18.12698m/s$$

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