

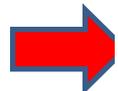
PHY 113 A General Physics I

9-9:50 AM MWF Olin 101

Plan for Lecture 8:

Chapter 5 – More applications of Newton's laws

- 1. Two dimensional statics and dynamics**
- 2. Friction forces**



No.	Lecture Date	Topic	Text Sections	Problem Assignments	Assignment Due Date
1	08/29/2012	Units & measurement	1.1-1.6	1.2,1.6,1.13,1.20	
2	08/31/2012	Motion in 1d -- constant velocity	2.1-2.3	2.1,2.8	09/07/2012
3	09/03/2012	Motion in 1d -- constant acceleration	2.4-2.8	2.13,2.16	09/07/2012
4	09/05/2012	Vectors	3.1-3.4	3.3,3.22	09/07/2012
5	09/07/2012	Motion in 2d	4.1-4.3	4.3,4.50	09/10/2012
6	09/10/2012	Circular motion	4.4-4.6	4.29,4.30	09/12/2012
7	09/12/2012	Newton's laws	5.1-5.6	5.1,5.13	09/14/2012
8	09/14/2012	Newton's laws applied	5.7-5.8	5.20,5.30,5.48	09/17/2012
	09/17/2012	Review	1-5		
	09/19/2012	Exam	1-5		
9	09/21/2012	More applications of Newton's laws	6.1-6.4		09/24/2012
10	09/24/2012	Work	7.1,7.4		09/26/2012

Isaac Newton, English physicist and mathematician (1642—1727)



1. In the absence of a net force, an object remains at constant velocity or at rest.
2. In the presence of a net force F , the motion of an object of mass m is described by the form $F=ma$.
3. $F_{12} = -F_{21}$.

<http://www.newton.ac.uk/newton.html>

Detail: “Inertial” frame of reference

Strictly speaking, Newton’s laws work only in a reference frame (coordinate system) that is stationary or moving at constant velocity. In a non-inertial (accelerating) reference frame, there are some extra contributions.

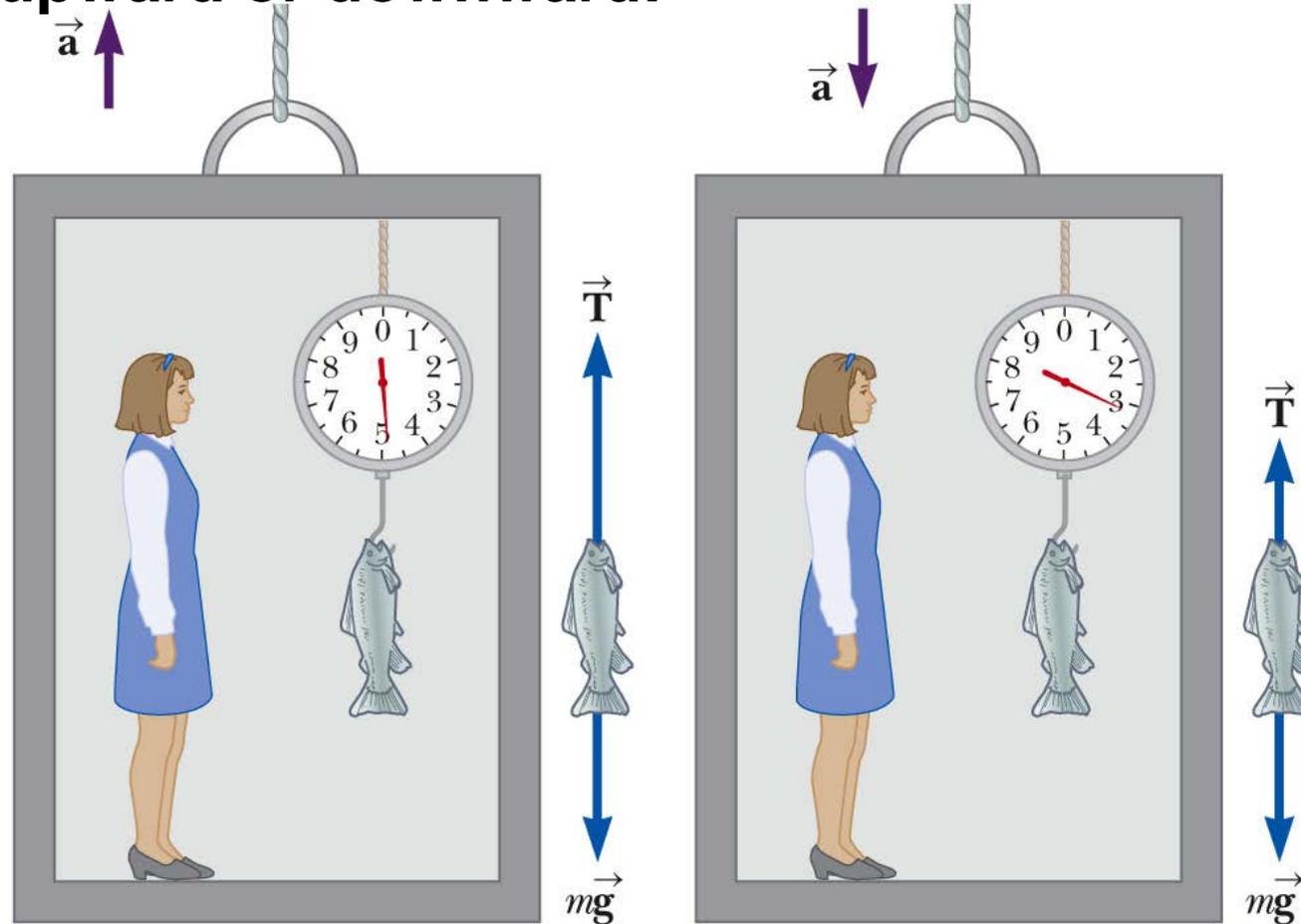
iclicker question:

Are we (here in Winston-Salem)

- A. In an inertial frame of reference (exactly)**
- B. In a non-inertial frame of reference**

Newton’s laws are only approximately true in Winston-Salem, but the corrections are very small.

Example from last time – elevator accelerating upward or downward:



$$T - mg = ma$$

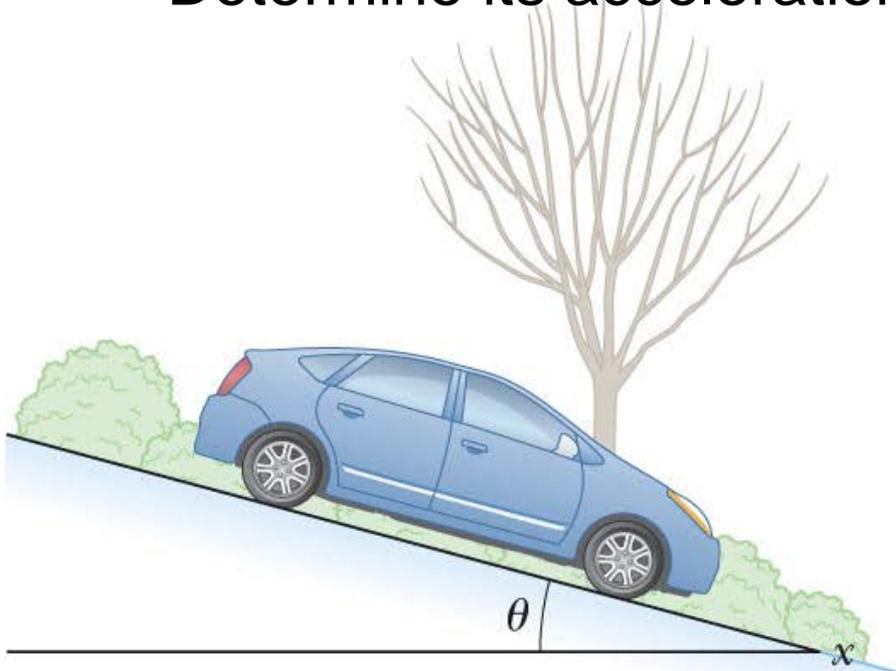
$$T = m(g + a)$$

$$T - mg = -ma$$

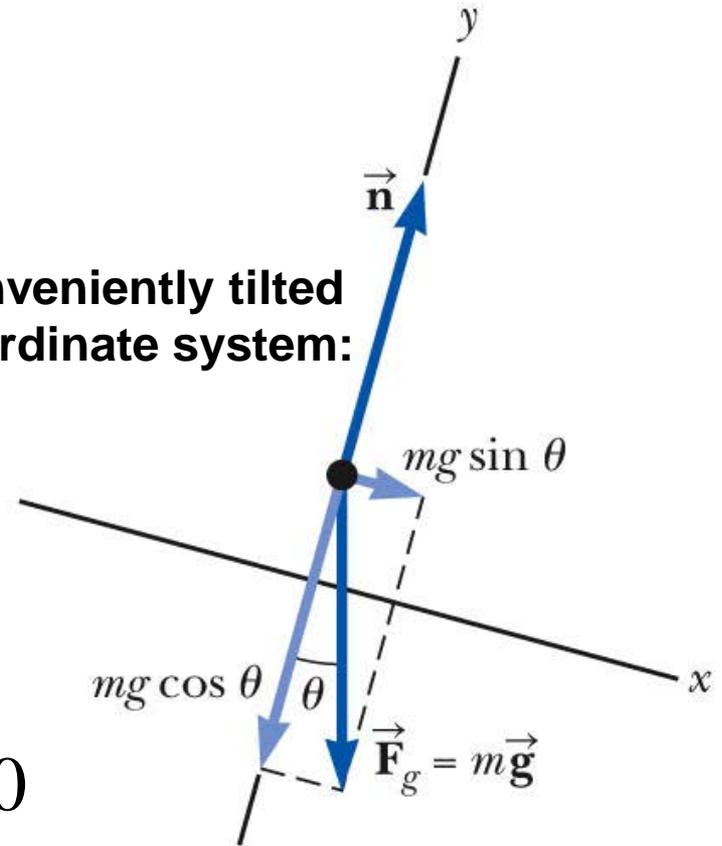
$$T = m(g - a)$$

Example: 2-dimensional forces

A car of mass m is on an icy (frictionless) driveway, inclined at an angle θ as shown. Determine its acceleration.



Conveniently tilted coordinate system:



$$\text{Along } y: \quad n - mg \cos \theta = 0$$

$$\text{Along } x: \quad mg \sin \theta = ma_x$$

$$a_x = g \sin \theta$$

Friction forces

The term “friction” is used to describe the category of forces that *oppose* motion. One example is surface friction which acts on two touching solid objects. Another example is air friction. There are several reasonable models to quantify these phenomena.

$$\text{Surface friction: } f = \begin{cases} -F_{\text{applied}} \\ \pm \mu N \end{cases}$$

Normal force between surfaces

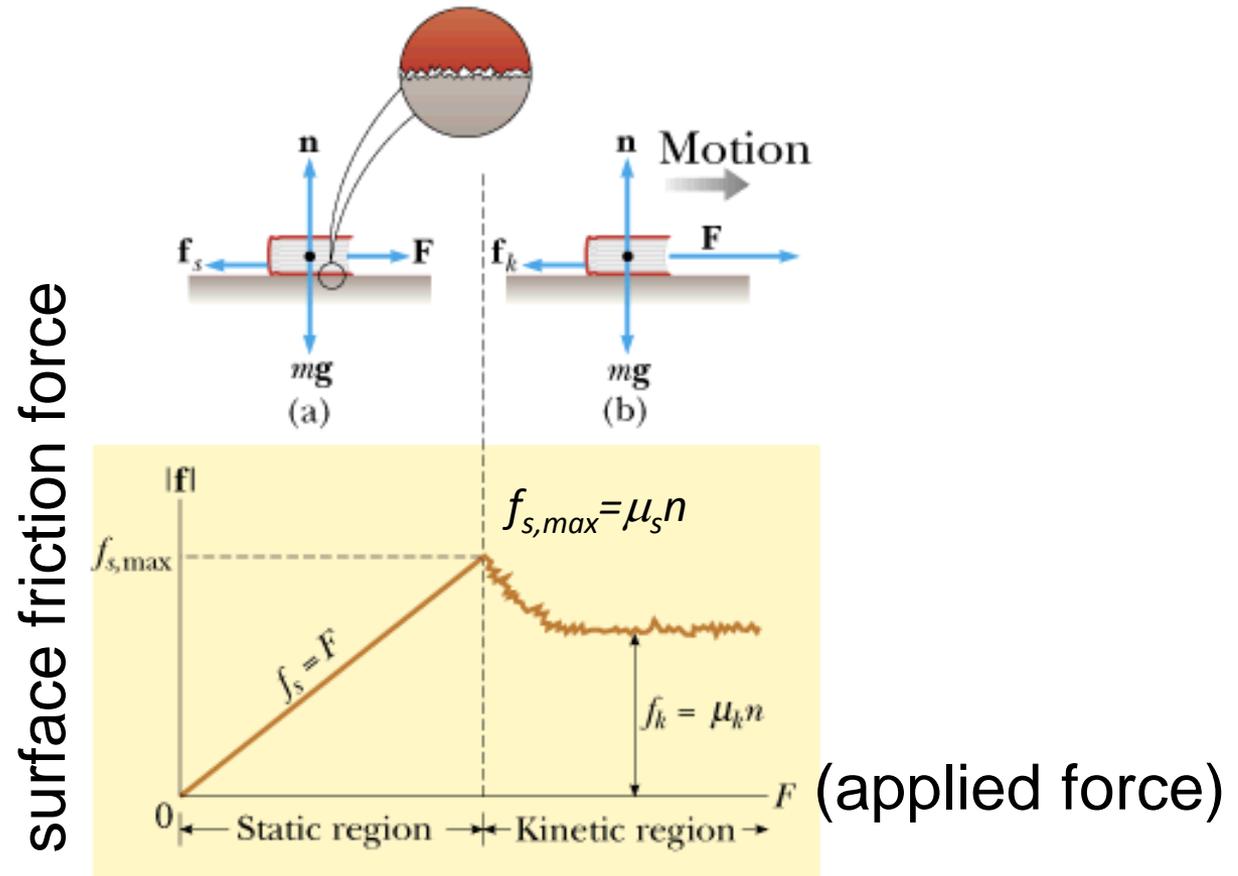
Material-dependent coefficient

$$\text{Air friction: } D = \begin{cases} -Kv & \text{at low speed} \\ -K'v^2 & \text{at high speed} \end{cases}$$

K and K' are materials and shape dependent constants

Models of surface friction forces

Serway, Physics for Scientists and Engineers, 5/e
Figure 5.17

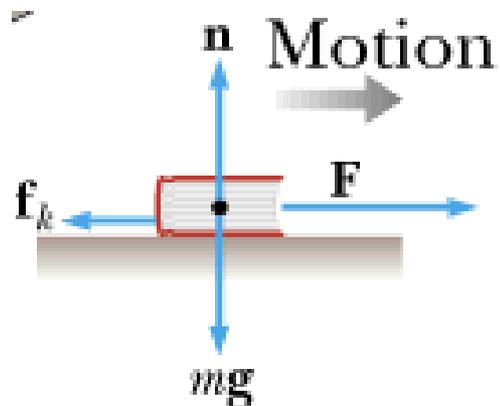


Coefficients μ_s , μ_k depend on the surfaces; usually, $\mu_s > \mu_k$

Some estimates of static and kinetic friction:

Material	μ_s	μ_k
Rubber on concrete	1.0	0.8
Wood on wood	0.3	0.2
Steel on steel with lubrication	0.09	0.05
Teflon on teflon	0.04	0.04

Surface friction:



$$F - f_s = 0 \text{ if } F < \mu_s n = \mu_s mg$$

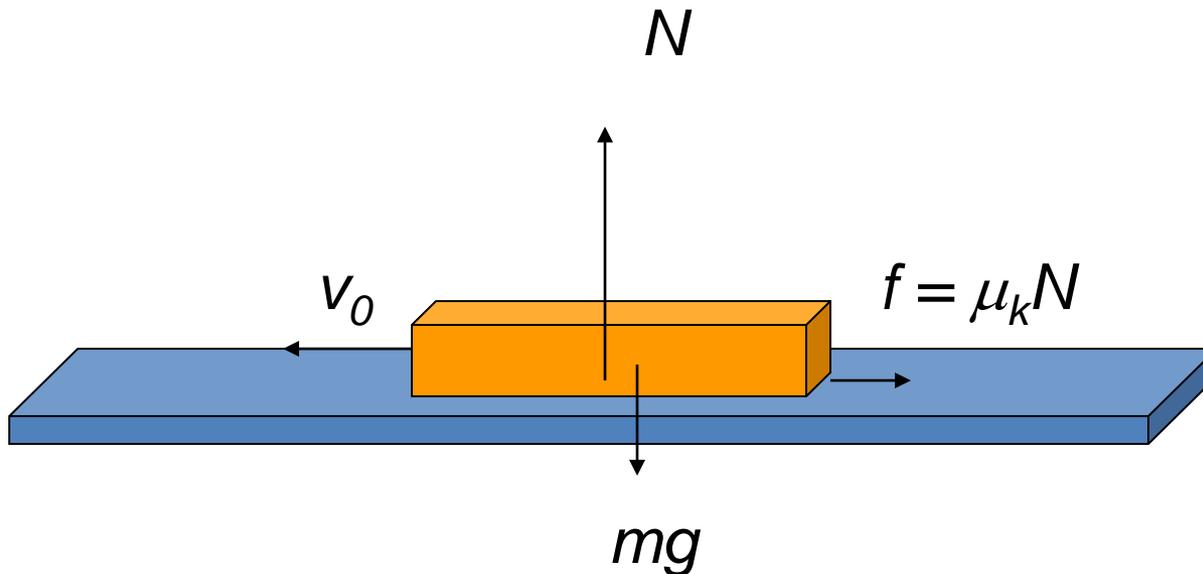
if $F > \mu_s n = \mu_s mg$, then $F - f_k = ma$ ($f_k = \mu_k mg$)

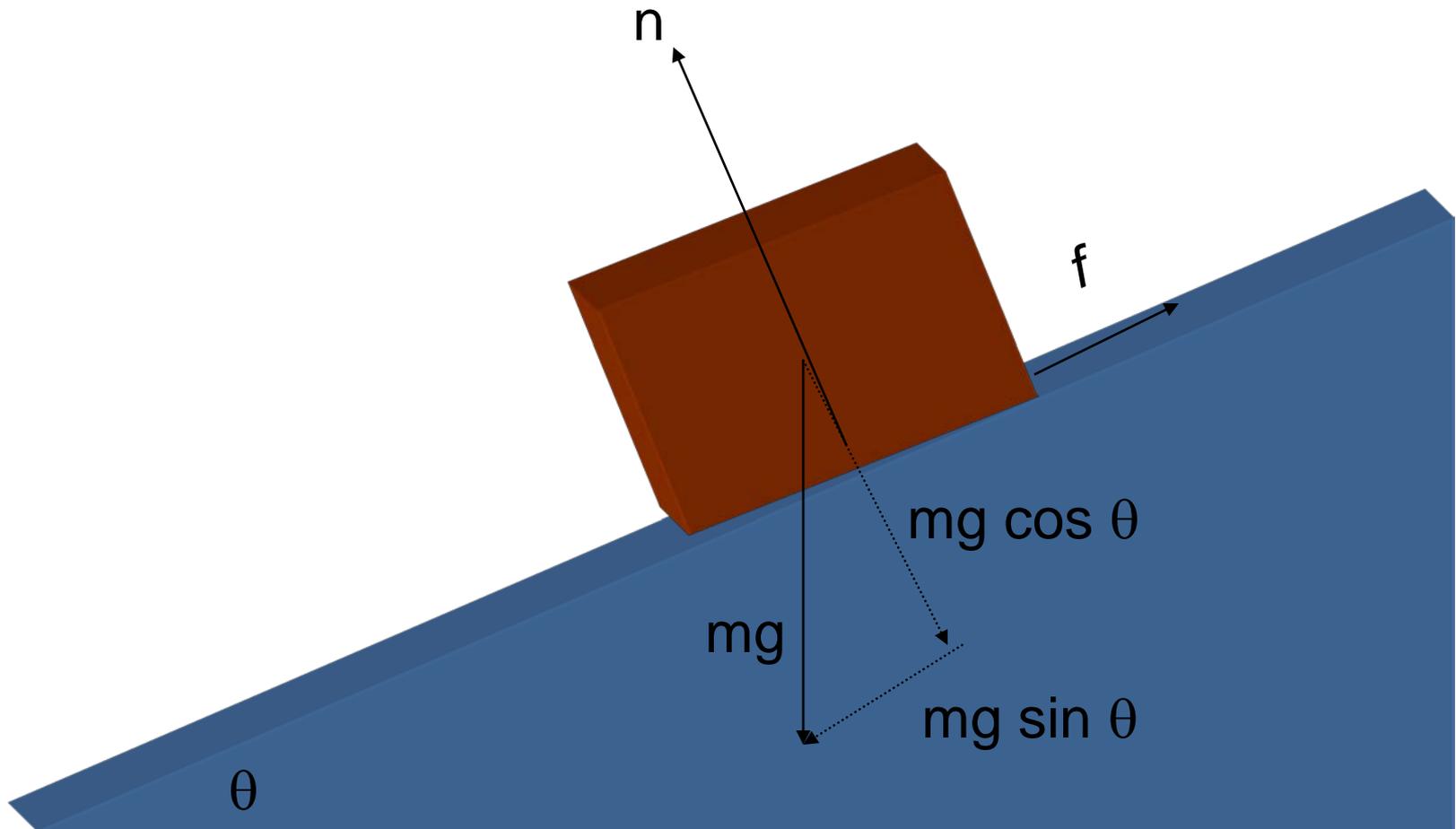
$$a = \frac{F - \mu_k mg}{m}$$

iclicker exercise:

The figure below shows a block of mass m moving to left at constant velocity v_0 . How is this possible?

- A. There is an additional horizontal force pulling the block to the left.
- B. There is an additional horizontal force pulling the block to the right.
- C. This is not a possible physical situation.





just before block slips:

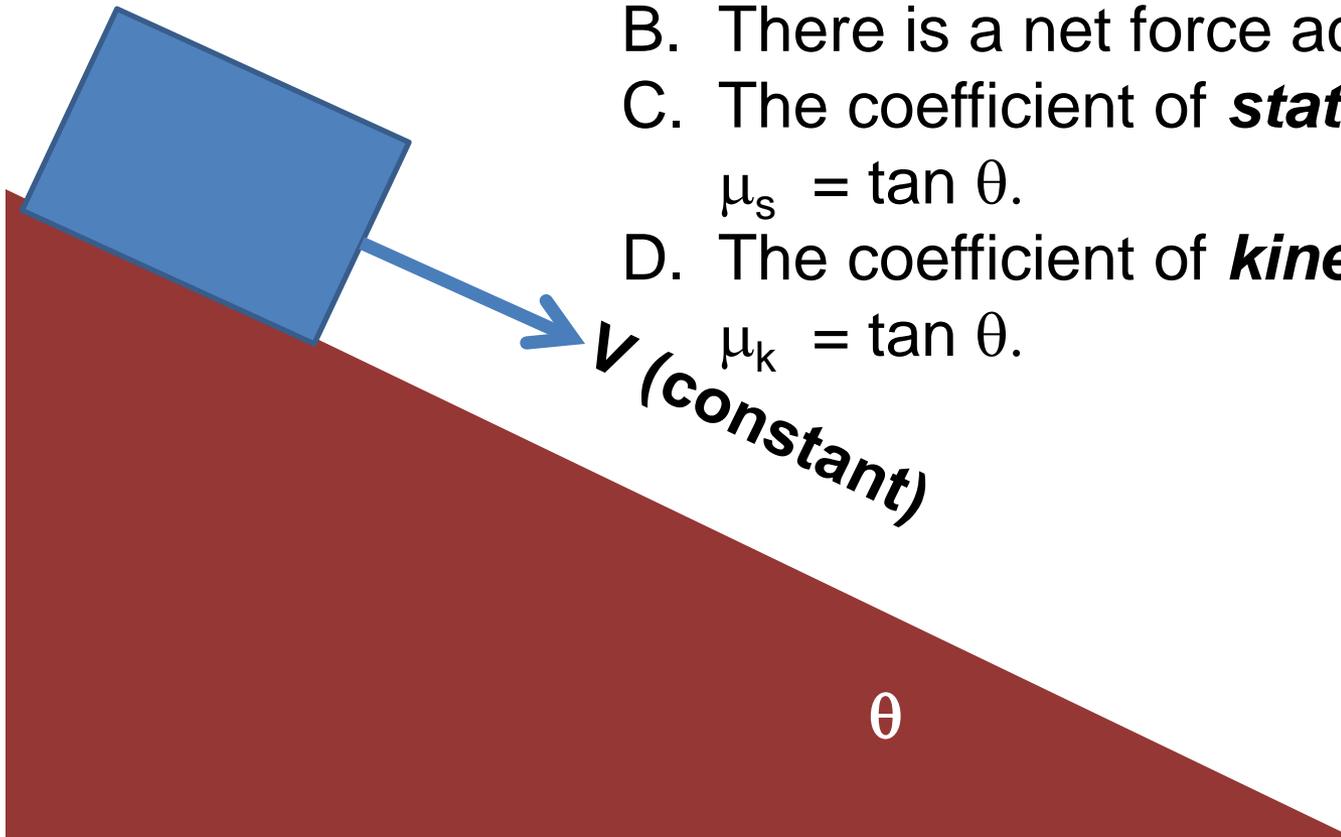
$$f_{s,\max} - mg \sin \theta = \mu_s n - mg \sin \theta = \mu_s mg \cos \theta - mg \sin \theta = 0$$

$$\rightarrow \mu_s = \tan \theta$$

iclicker exercise:

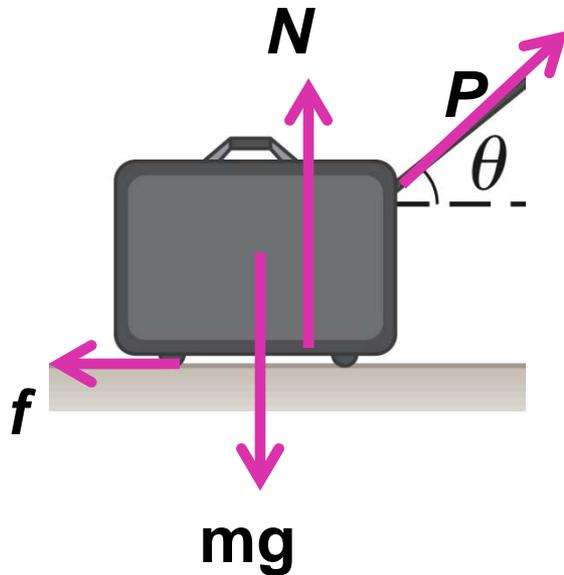
Suppose you place a box on an inclined surface as shown in the figure and you notice that the box slides down the incline at constant velocity V . Which of the following best explains the phenomenon:

- A. There is no net force acting on the box.
- B. There is a net force acting on the box.
- C. The coefficient of ***static*** friction is $\mu_s = \tan \theta$.
- D. The coefficient of ***kinetic*** friction is $\mu_k = \tan \theta$.





A woman at an airport is towing her 20 kg suitcase at constant speed by pulling on a strap at an angle θ above the horizontal. She pulls on the strap with a $P=35$ N force, and the friction force on the suitcase is $f=20$ N. What is the value of the angle θ ?

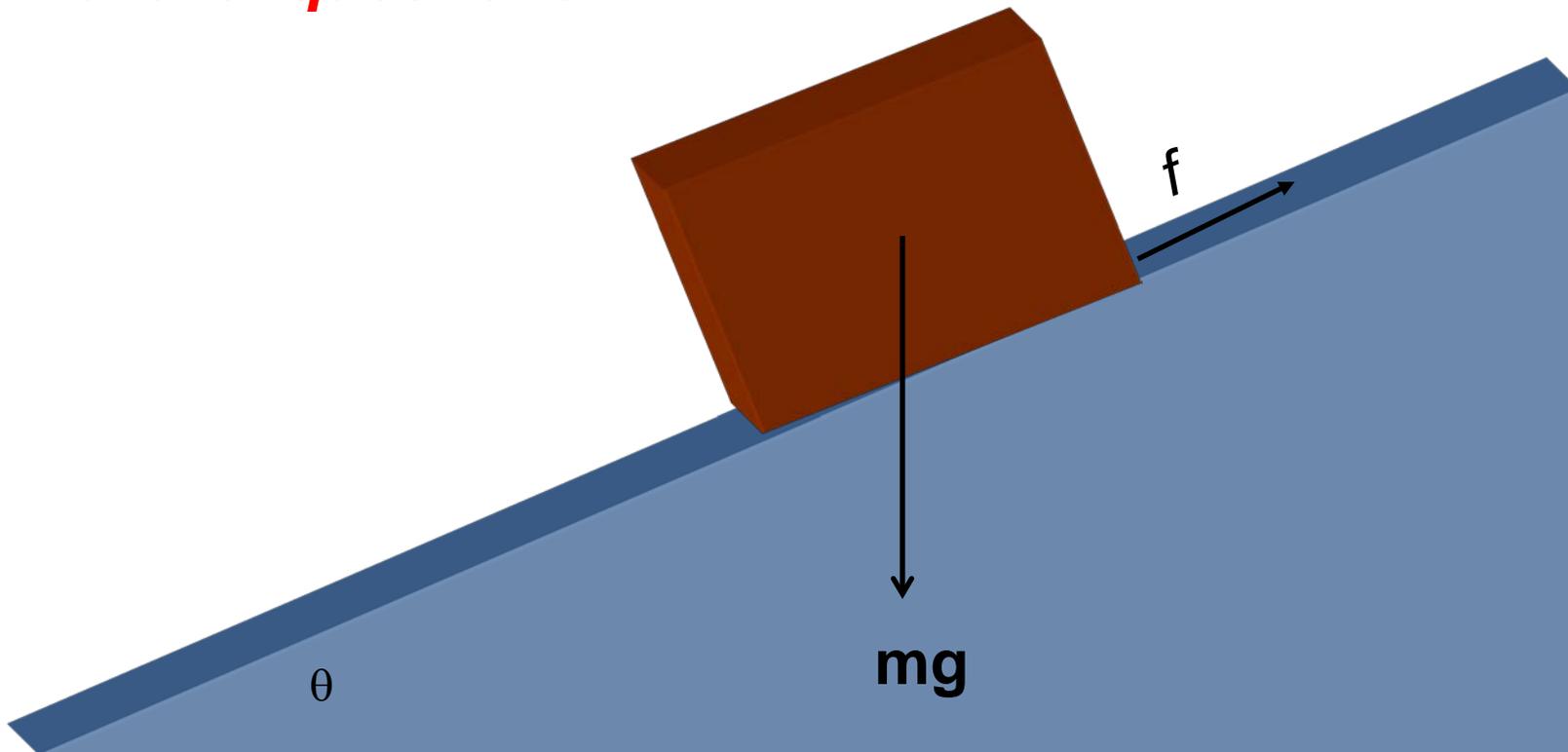


Horizontal components : $P \cos \theta - f = 0$

Vertical components : $P \sin \theta + N - mg = 0$

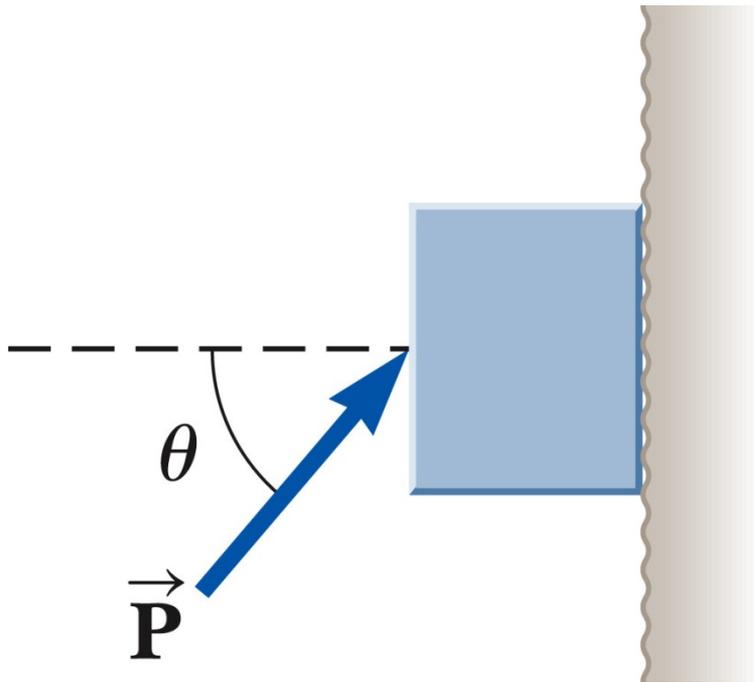
$$\Rightarrow \cos \theta = \frac{f}{P} = \frac{20}{35} \quad \theta = 55.15^\circ$$

iclicker questions:

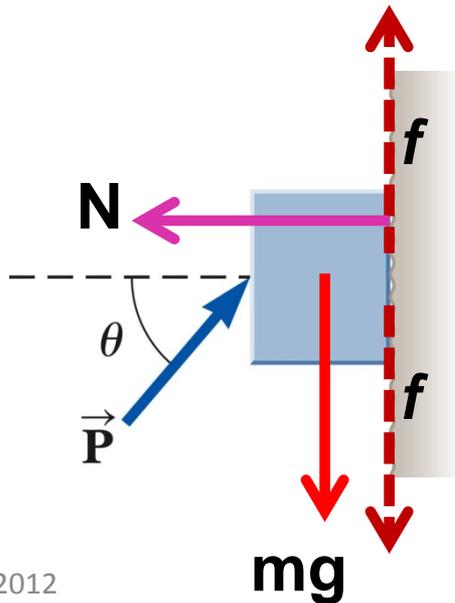


Suppose that $\mu_s=0.75$ which means that the block starts to slide when $\theta = \tan^{-1}(0.75) = 37^\circ$. What is f when $\theta = 20^\circ$?

- A. $mg \sin\theta$ B. $\mu_s mg \sin\theta$ C. $mg \cos\theta$ D. $\mu_s mg \cos\theta$

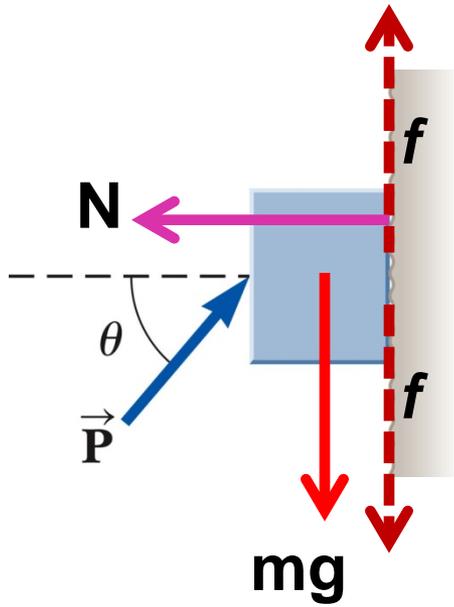


A block of mass 3 kg is pushed up against a wall by a force \mathbf{P} that makes an angle of $\theta=50^\circ$ with the horizontal. $\mu_s=0.25$. Determine the possible values for the magnitude of P that allow the block to remain stationary.



Vertical forces: $\pm \mu_s N + P \sin \theta - mg = 0$

Horizontal forces: $P \cos \theta - N = 0$



Vertical forces: $\pm \mu_s N + P \sin \theta - mg = 0$

Horizontal forces: $P \cos \theta - N = 0$

$$N = P \cos \theta$$

$$\pm \mu_s P \cos \theta + P \sin \theta - mg = 0$$

Solving for P :
$$P = \frac{mg}{\sin \theta \pm \mu_s \cos \theta}$$

$$P = \frac{3 \cdot 9.8 \text{ N}}{\sin 50^\circ \pm 0.25 \cos 50^\circ}$$

$$= \begin{cases} 31.72 \text{ N} \\ 48.57 \text{ N} \end{cases}$$