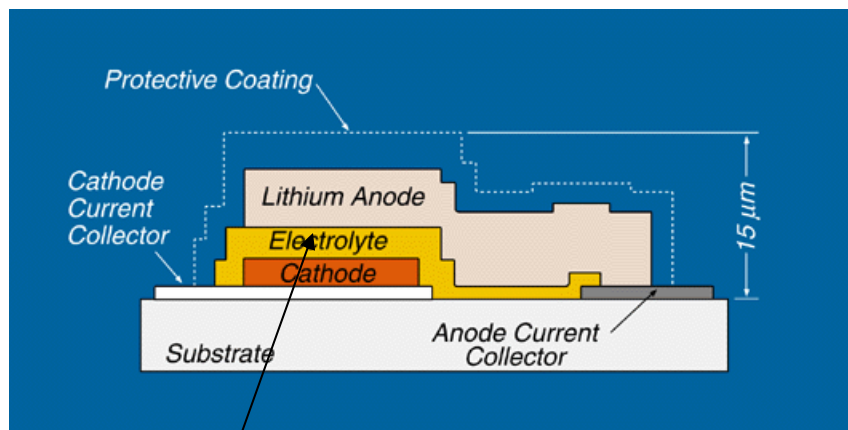


First-principles simulations of extended structures in the lithium phosphorous oxynitride electrolytes

Yaojun Du and N. A. W. Holzwarth

The structure of thin film battery²



Solid state electrolytes that are physically and chemically stable can be made very thin. Such as LiPON (Li_3PO_4)

The thin film LiPON, having the composition of $\text{Li}_{3+x}\text{PO}_{4-y}\text{N}_z$ with $x = 3z - 2y$ has been developed as a solid state electrolyte for Li ion batteries by ORNL¹.

Conductivities of various LiPON material are measured^{1,3}

$$\sigma(T) = \frac{K}{T} e^{-E_A/kT}$$

For various LiPON materials,^{1,3-6} the activation energies are determined to be 0.4 – 0.7 eV.

For instance, for $\text{Li}_{0.99}\text{PO}_{2.55}\text{N}_{0.30}$, Wang et al. measured the activation energy of 0.6 eV.⁶

1. B. Wang et al., *J. of Solid State Chemistry* **115**, 313 (1995).
2. <http://www.ms.ornl.gov/researchgroups/Functional/BatteryWeb/CrossSection.html>
3. C. H. Choi et al., *Electrochemical and Solid-state Letters*, **5**, A14 (2002).
4. Y. Hamon et al., *Solid State Ionics* **177**, 257 (2006).
5. Wen-Yuan Liu et al., *Electrochemical and Solid-state Letters*, **7**, J36 (2004).
6. B. Wang et al., *Journal of Non-Crystalline Solids* **183**, 297 (1995).

Motivation and goal

The goal of this work is to optimize the structure and stoichiometry of LiPON electrolytes for use in Li ion batteries which can achieve the highest ionic conductivity.

A number of groups have addressed this problem experimentally and have found evidence for linear chains of phosphates with bridging -O- and -N- sites and more complicated phosphate structures such as triply coordinated N.¹

In this talk, we will discuss first-principles simulations on naturally occurring crystals and constructed artificial crystals, focusing on these particular structures and their effects on the migration of Li ions.

Outline

1. Method
2. Optimize the LiPO_3 crystal has a linear chain structure (P-O-P) observed in the LiPON glasses.
3. Construction of an artificial LiPO_3 crystal which also contains P-O-P chains and which is amenable for NEB treatment.
4. Construction of the $\text{Li}_2\text{PO}_2\text{N}$ crystal which contains P-N-P chains.
5. Characterize the triply-coordinated N based on the $\alpha\text{-P}_3\text{N}_5$, Also study its effect on the migration of Li ions.
6. Conclusion.

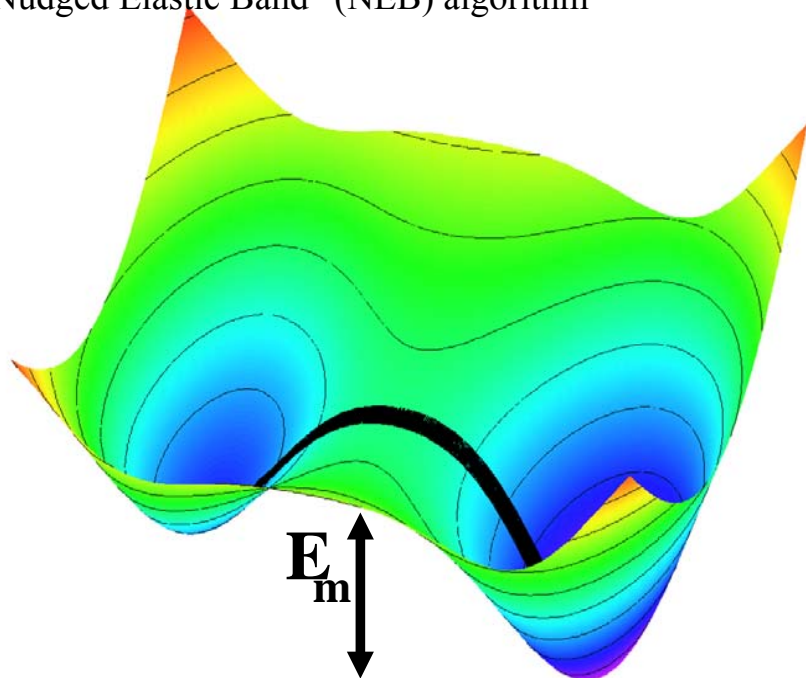
1. B. Wang et al., J. of Solid State Chemistry **115**, 313 (1995).

Method

Quantum ESPRESSO (*PWscf*)¹ package and ultra-soft pseudopotential formalism of Vanderbilt using LDA.

Ionic conductivity via activated hopping

Schematic diagram of minimal energy path, estimated using “Nudged Elastic Band” (NEB) algorithm²



1. www.pwscf.org
2. H. Jónsson *et al.*, in *Classical and Quantum Dynamics in Condensed Phase Simulations*, edited by Berne, Ciccotti, and Coker (World Scientific 1998), p. 385; G. Henkelman *et al*, *JCP* **113**, 9901, 9978 (2000).

Arrhenius relation

$$\sigma \cdot T = K e^{-E_A/kT}$$

Experimental conductivities for single γ -Li₃PO₄ crystals by Ivanov-Shitz *et al*, *Cryst. Reports* **46**, 864 (2001):

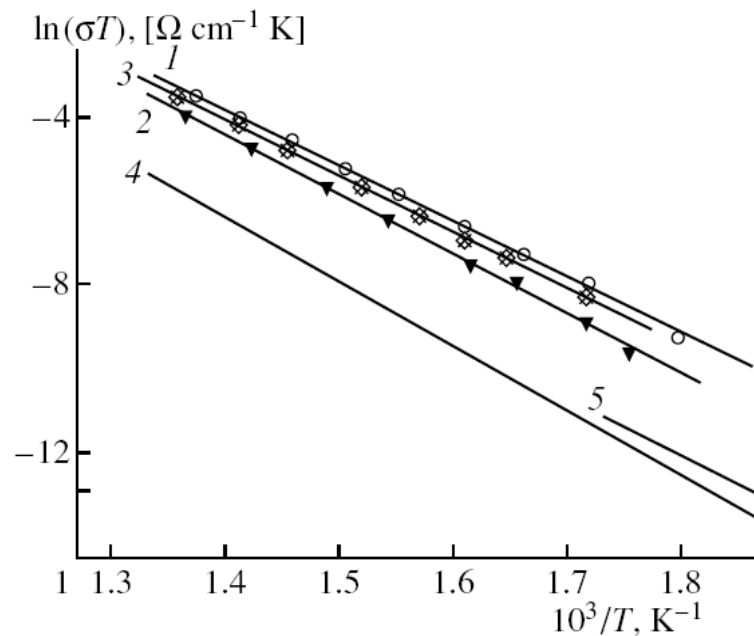


Fig. 2. Temperature dependences of conductivity in γ -Li₃PO₄: (1–3) for single crystals measured along the (1) *a*-axis, (2) *b*-axis, (3) *c*-axis and (4, 5) for a polycrystal (4) according to [4, 5] and (5) according to [7].

$E_A = 1.14, 1.23, 1.14, 1.31, 1.24$ eV for cases 1,2,3,4,5, respectively.

Perfect LiPO_3 crystal

The LiPO_3 crystal contains linear chains of phosphates connected with bridging -O- sites^{1,2}.

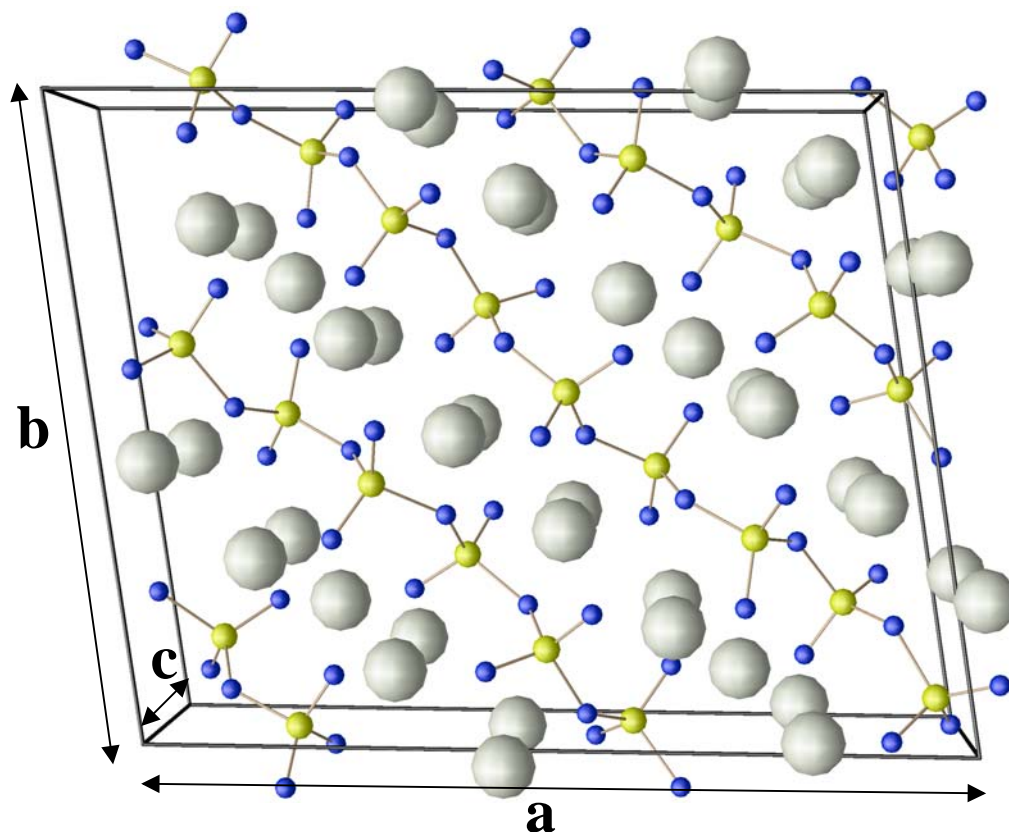
Based on the experiment data, we optimize the primitive cell of a LiPO_3 crystal with 100 atoms .

For the bridging O

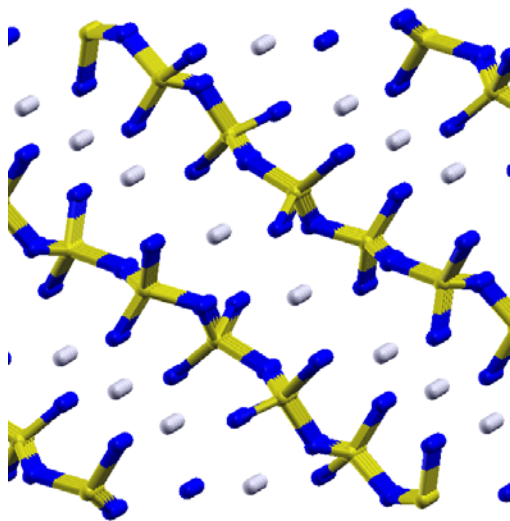
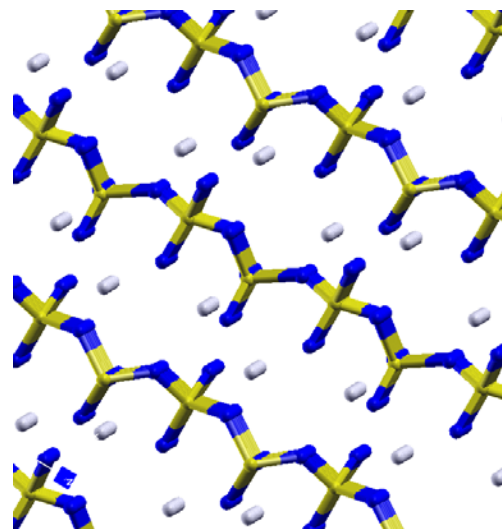
	This work (LDA)	Experiment ²
Bond angle (degree)	126.7 – 136.9	127.4 – 137.9
Bond length (Ang.)	1.59-1.61	1.57 – 1.62

For the tetrahedral O

	This work (LDA)	Experiment ²
Bond angle (degree)	104.0 – 121.2	105.8 – 120.5
Bond length (Ang.)	1.49-1.50	1.47 – 1.49



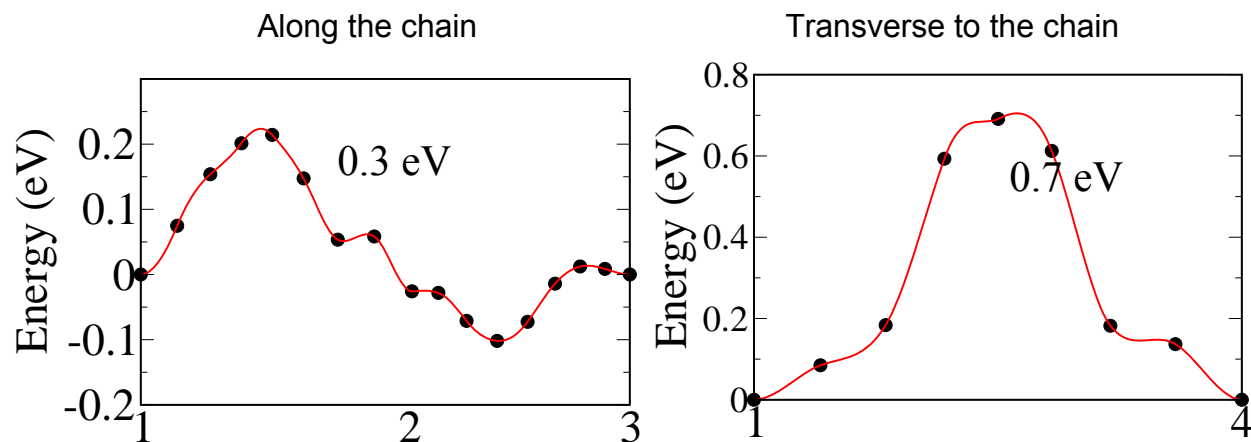
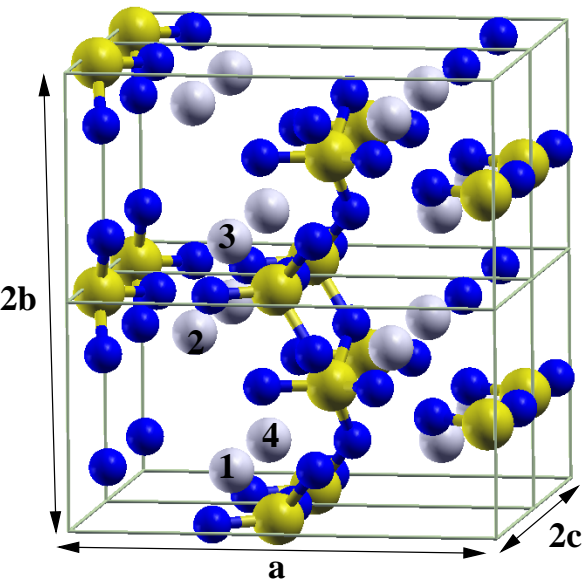
1. B. Wang et al., *J. of Non-Crystalline Solids* **183**, 297 (1995).
2. E. V. Murashova and N. N. Chudinova, *Crysallography Reports* **46**, 942 (2001)

The constructed LiPO_3 Naturally existing LiPO_3 Artificial LiPO_3

Comparison between the artificial and natural LiPO_3

	Total energy (eV/f.u.)	Volume (a.u.) ³ /f.u	Bond Angle (Bridging O)	Bond Length (Bridging O)	Bond Angle (Tetrahedral O)	Bond Length (Tetrahedral O)
Artificial	0.2	386.5	131.5 – 134.4	1.60 – 1.62	101.2 – 122.1	1.49
Natural	0	375.2	126.7 – 136.9	1.59 – 1.61	105.8 – 120.5	1.49-1.50

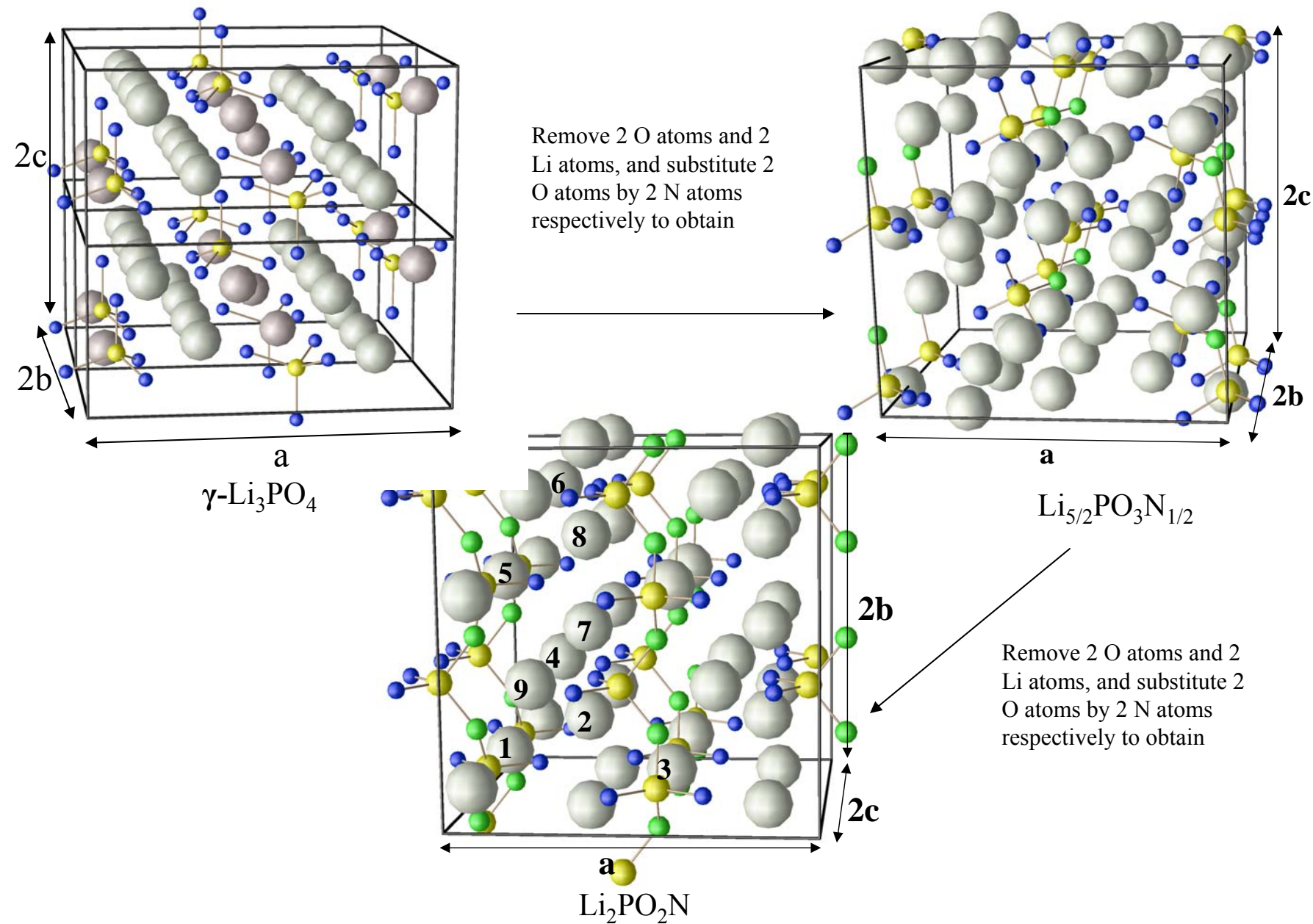
Simulations of the Li ion migration within the constructed LiPO_3



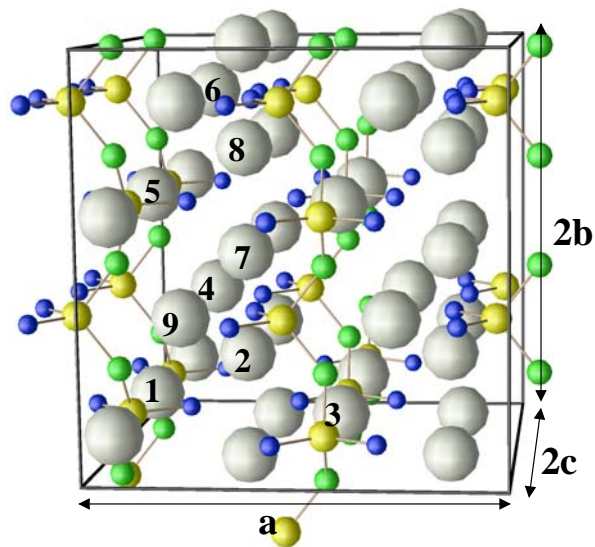
	This work (eV)	NMR ¹ (eV)	Impedance ² (eV)
E_m (eV)	0.3 – 0.7	0.66	0.76

1. Sandra et al., *Phys. Rev. B*, **77**, 104301 (2008).
2. B. K. Money and K. Hariharan, *Appl. Phys. A*, **88**, 647 (2007).

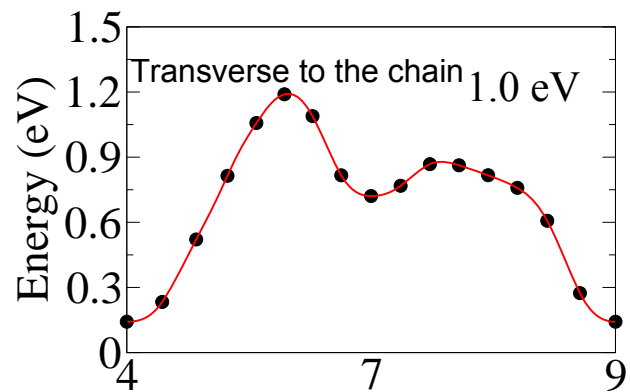
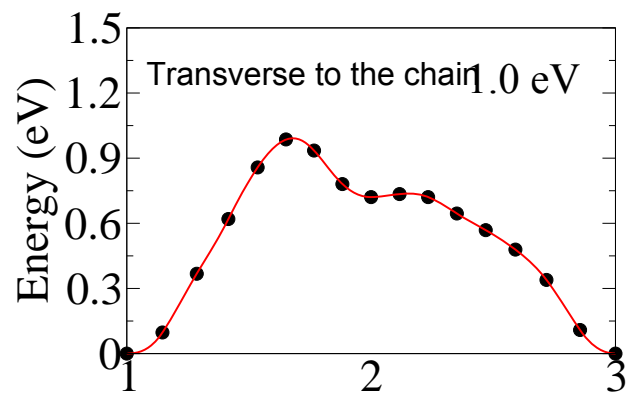
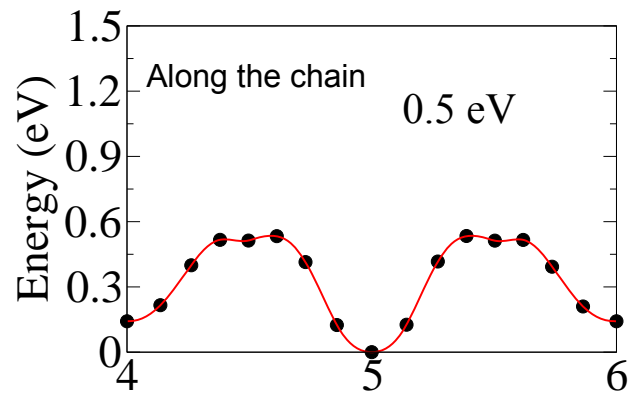
Formation of N-containing phosphate chains



Simulations of the Li ion migration within the constructed $\text{Li}_2\text{PO}_2\text{N}$



	Bridging N (P-N-P)	Tetrahedral O
Bond angle (degree)	130.9	103.2—114.8
Bond length (Ang.)	1.62 – 1.63	1.54 – 1.55



Migration within the chain structure

We have characterized the bonding situations of P-O-P and P-N-P structures and have shown that Li ion vacancies can diffuse along the P-O-P and P-N-P with migration barriers of 0.3 eV and 0.5 eV, respectively. On the other hand, if the Li ion vacancies diffuse perpendicular to the chain structures, the migration barrier will raise to 0.7 eV and 1.0 eV, respectively.

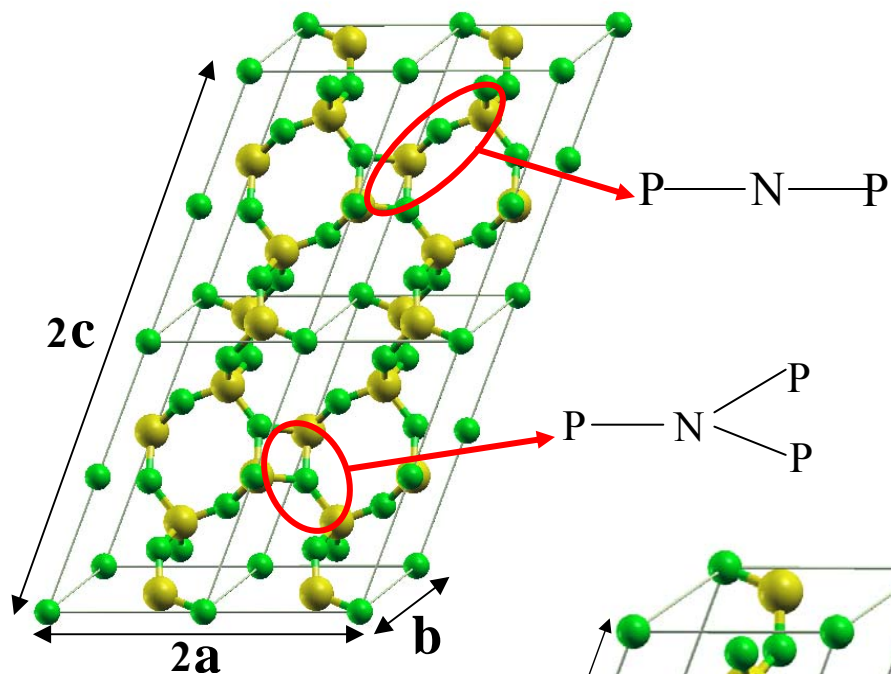
Next, we have will characterize the bonding situations of the triply coordinated N based on the α -P₃N₅ crystal, and study Li ion migration within the crystal.

The ratio between the doubly coordinated N and triply coordinated N is 0.3.¹



1. B. Wang et al., *Journal of Non-Crystalline Solids* **183**, 297 (1995).

Migration of Li ions within the α - P_3N_5 structure



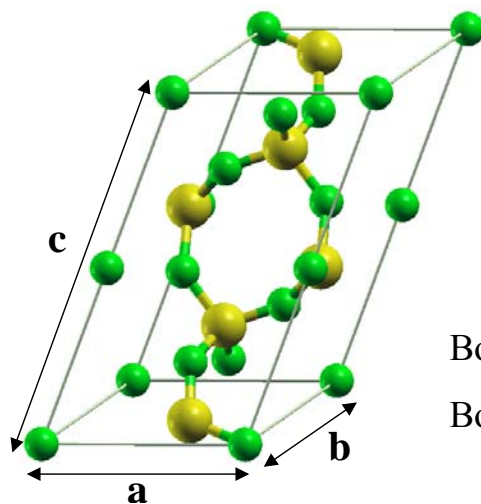
Six member ring that is proposed by Veprek².

Doubly Coordinated N

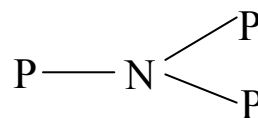


Bond Length: 1.55 and 1.56 Ang.

Bond Angle: 142.5 and 180 degree.



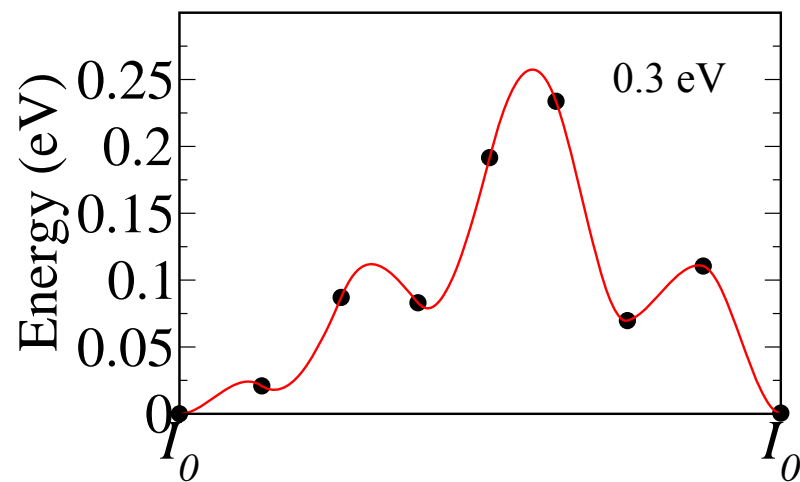
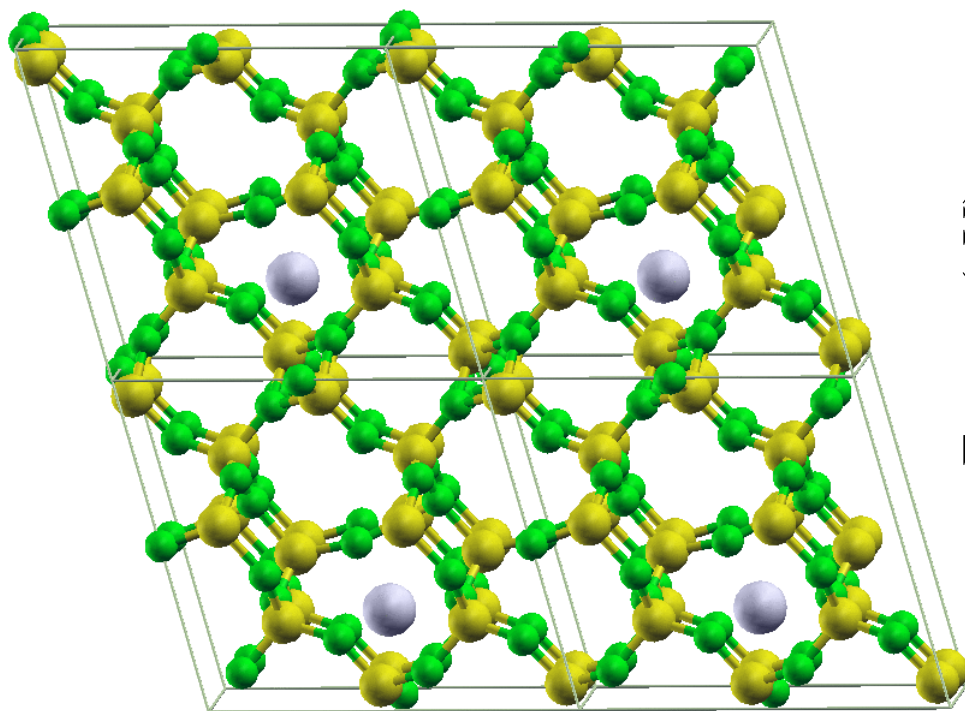
Triply Coordinated N¹



Bond Length: 1.66, 1.69, and 1.71 Ang.

Bond Angle: 127.2, 97.2, and 135.6 degree.

1. B. Wang *et al.*, *J. of Non-Crystalline Solids* **183**, 297 (1995).
2. S. Veprek *et al.*, *Philosophical Magazine B* **43**, 527 (1981).

Migration of Li ions within the α -P₃N₅ structure

Conclusion

1. We have constructed LiPO_3 with a 20-atom primitive cell. It contains the linear bridging structure of P-O-P that has the bond angle of $131.5 - 134.4$ degree and the bond length of $1.60 - 1.62$ Ang. On the other hand, the naturally existing LiPO_3 has the bond angle of $126.7 - 136.9$ degree and the bond length of $1.59-1.61$ Ang.
2. We have constructed $\text{Li}_2\text{PO}_2\text{N}$ with a 24-atom primitive cell. It contains the linear bridging structure of P-N-P that has the bond angle of $131.5 - 134.4$ degree and the bond length of $1.60 - 1.62$ Ang.
3. In both the constructed LiPO_3 and $\text{Li}_2\text{PO}_2\text{N}$, we have show that the linear structures of P-O-P and P-N-P provide 1D diffusion channel for Li ions. We expect that the migration barrier within LiPO_3 glasses to be 0.7 eV which is consistent with the experimental results.
4. Li ion can be inserted into the $\alpha\text{-P}_3\text{N}_5$ crystal and has a migration barrier of 0.3 eV. However, the connection between our results and the triply coordinated N within the LiPON material has yet to be confirmed.

Summary of migration energies for Li ion vacancies in $\text{Li}_{3+x}\text{PO}_{4-y}\text{N}_z$ with $x = 3z - 2y$

x	y	z	form	E_{exp} (eV)	E_{m} (eV)
0	0	0	$\gamma\text{-Li}_3\text{PO}_4$	1.1 ^{1,a}	0.7
-2	1	0	LiPO_3 (P-O-P)	0.66 – 0.76 ^{5,6}	0.5 – 0.7
-1	1	2	$\text{Li}_2\text{PO}_2\text{N}$ (P-N-P)		0.5 – 1.0 ^b
-3	4	5/3	$\alpha\text{-P}_3\text{N}_5$		0.3 ^b

^a The 1.1 eV activation energy includes the formation energy of intrinsic defects and the migration energy for an interstitialcy mechanism. (see Phys. Rev. B **76**, 174302 (2007)).

^b For various LiPON materials,²⁻⁴ the activation energies are determined to be 0.4 – 0.7 eV.

1. A. K. Ivanov-Shitz et al., *Crystallogr. Rep.* **46**, 864 (2001).
2. Y. Hamon et al., *Solid State Ionics* **177**, 257 (2006).
3. C. H. Choi et al., *Electrochemical and Solid-state Letters*, **5**, A14 (2002).
4. Wen-Yuan Liu et al, *Electrochemical and Solid-state Letters*, **7**, J36 (2004).
5. Sandra et al., *Phys. Rev. B*, **77**, 104301 (2008).
6. B. K. Money and K. Hariharan, *Appl. Phys. A*, **88**, 647 (2007).

Future work

We will consider other materials such as P_2O_5 , LiPN_2 , and Li_7PN_4 .