PHY 745 – Problem Set #3

This homework is due Monday, January 26, 2009.

Continue reading Chapter 3 in Tinkham.

1. Consider the following 2×2 "normal" matrix $(NN^{\dagger} = N^{\dagger}N)$ in terms of real constants a, b, β , and γ .

$$N = \left(\begin{array}{cc} a & b \mathrm{e}^{i\beta} \\ b \mathrm{e}^{i\gamma} & a \end{array}\right).$$

(a) Find the eigenvalues λ_i and eigenvectors v_i

$$Nv_i = \lambda_i v_i.$$

(b) Show that

$$N^{\dagger} v_i = \lambda_i^* v_i.$$

- (c) Find the relationships between the constants for the case that N is Hermitian.
- (d) Find the relationships between the constants for the case that N is unitary.