PHY 114 A General Physics II 11 AM-12:15 PM TR Olin 101

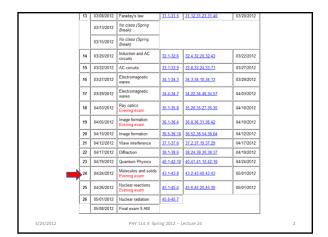
Plan for Lecture 24 (Chapter 43):

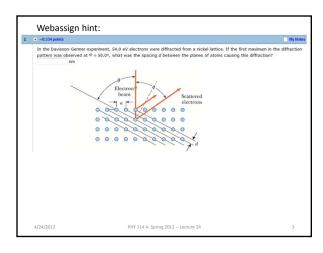
Some topics in the physics of molecules and solids

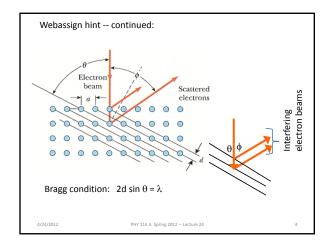
- 1. Physics of atoms
- 2. Physics of molecules
- 3. Physics of solids

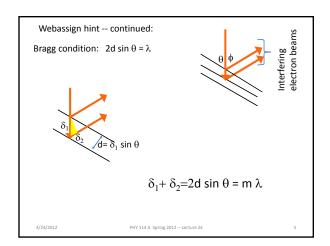
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Some ideas of quantum theory discussed last time:

Matter wave equation – Schrödinger equation:

$$\left[-\frac{\hbar^2}{2m}\frac{\partial^2}{\partial \mathbf{r}^2} + U(\mathbf{r})\right]\Psi(\mathbf{r},t) = -i\hbar\frac{\partial}{\partial t}\Psi(\mathbf{r},t)$$

Stationary-state wavefunctions: $\Psi(\mathbf{r},t) = \psi(\mathbf{r})e^{-iEt/\hbar}$ In this case, the Schrodinger equation becomes:

$$\left[-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial \mathbf{r}^2} + U(\mathbf{r}) \right] \Psi(\mathbf{r}, t) = E\Psi(\mathbf{r}, t)$$

Here Planck's constant: $h = 6.63 \times 10^{-34} J$

$$\hbar = \frac{h}{2\pi} = 1.05 \times 10^{-34} J$$

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Example -- free particle -- U(r) = 0: $\Psi(\mathbf{r}, t) = \psi(\mathbf{r})e^{-iEt/\hbar}$

$$\left[-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \right] \Psi(x,t) = E \Psi(x,t)$$

$$\Psi(x,t) = \Psi_0 \sin(kx)e^{-iEt/\hbar}$$

$$\Psi(x,t) = \Psi_0 \sin(kx)e^{-iEx/\hbar}$$

$$E = \frac{\hbar^2 k^2}{2m} \quad \text{Note : This is consistent with de Broglie's } \lambda = \frac{h}{p}$$

$$k = \frac{2\pi}{\lambda} \implies \lambda = \frac{h}{\sqrt{2mE}} \text{ or } E = \frac{h^2}{2m\lambda^2}$$

Example: Suppose we want to create a beam of electrons (m=9.1x10⁻³¹kg) for diffraction with λ =1x10⁻¹⁰m. What is the energy E of the beam?

$$E = \frac{h^2}{2m\lambda^2} = \frac{\left(6.6 \times 10^{-34} J\right)^2}{2 \cdot 9.1 \times 10^{-31} \, kg \cdot \left(10^{-10} m\right)^2} = 2.4 \times 10^{-17} \, J = 150 eV$$
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Recall de Broglie's relation between wavelength and momentum:

$$\lambda = \frac{h}{p} \qquad h = 6.6 \times 10^{-34} J$$

Which has the larger de Broglie wavelength:

- A. An electron with a velocity of 100 m/s (mass = $9.1x10^{-31}$ kg)
- B. A baseball with a velocity of 100 m/s (mass = 1 kg)

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Another example -- electron bound to a proton: (H atom) $U(r) = -\frac{Ze^2}{4\pi \varepsilon_0 r}$

(H atom)
$$U(r) = -\frac{Ze^2}{4\pi\varepsilon_0 r}$$

$$\left[-\frac{\hbar^2}{2m}\frac{\partial^2}{\partial \mathbf{r}^2} + U(\mathbf{r})\right]\Psi(\mathbf{r},t) = -i\hbar\frac{\partial}{\partial t}\Psi(\mathbf{r},t)$$

Stationary-state wavefunctions:
$$\Psi(\mathbf{r},t) = \psi(\mathbf{r})e^{-iEt/\hbar}$$

Solutions: $E_n = -\frac{Z^2e^2}{8\pi\epsilon_0 a_0} \frac{1}{n^2} = -13.6 \frac{Z^2}{n^2} \text{ eV}$ $n = 1,2,3\cdots$
 $a_0 = \frac{4\pi\epsilon_0 \hbar^2}{me^2} = 0.0529 \text{ nm}$

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Quantum theory for electromagnetic radiation

The transition between bound quantum states can correspond to the emission (production) or absorption (consumption) of electromagnetic quanta:

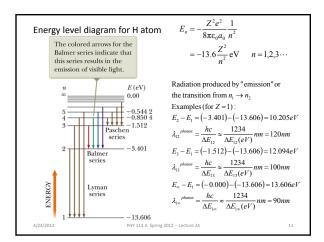
Coupling of states of matter with EM radiation:

$$\label{eq:hf_photon} hf^{\textit{photon}} = \frac{hc}{\lambda^{\textit{photon}}} = \left| E_{\textit{final}} - E_{\textit{initial}} \right| = \left| \Delta E \right|$$

$$\lambda^{photon} = \frac{hc}{\Delta E} \approx \frac{1234}{\Delta E_{12}(eV)} nm$$

hf photon $|\Delta E|$

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Physics of molecules – H₂ Recall for H atom:

$$\left[-\frac{\hbar^2}{2m} \frac{\partial^2}{\partial \mathbf{r}^2} - \frac{Ze^2}{4\pi\epsilon_0 r} \right] \psi(\mathbf{r}) = E\psi(\mathbf{r})$$

For ground state: $E_1 = -\frac{Z^2 e^2}{8\pi \varepsilon_0 a_0}$ $\psi_1(\mathbf{r}) = \frac{1}{\sqrt{\pi a_0^3}} e^{-r/a_0}$

$$\psi_1(\mathbf{r}) = \frac{1}{\sqrt{\pi a_0^3}} e^{-r/a_0}$$

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Physics of molecules - H₂ -- continued

$$|\mathbf{r} - \mathbf{R}_1|$$
 $|\mathbf{r} - \mathbf{R}_2|$

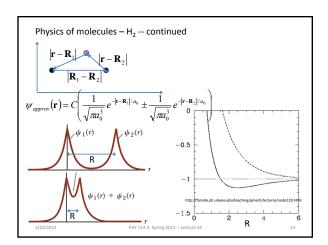
$$\left[-\frac{\hbar^2}{2m}\frac{\partial^2}{\partial \mathbf{r}^2} - \frac{Ze^2}{4\pi\varepsilon_0|\mathbf{r} - \mathbf{R}_1|} - \frac{Ze^2}{4\pi\varepsilon_0|\mathbf{r} - \mathbf{R}_2|}\right]\psi(\mathbf{r}) = E\psi(\mathbf{r})$$

Approximate solutions

$$\psi_{approx}(\mathbf{r}) = C \left(\frac{1}{\sqrt{\pi a_0^3}} e^{-|\mathbf{r} - \mathbf{R}_1|/a_0} \pm \frac{1}{\sqrt{\pi a_0^3}} e^{-|\mathbf{r} - \mathbf{R}_2|/a_0} \right)$$

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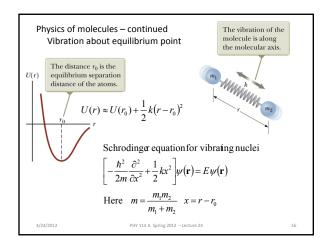


Physics of molecules – continued
Energy diagram for NaCl molecule as a function of ion separation

The asymptot of the cure for large values of rs marked Na* + Cl values of rs marked Na* + C

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Physics of molecules – continued
Vibration about equilibrium point

Solution to Schrodinger equation for vibrating nuclei

$$\begin{bmatrix} -\frac{\hbar^2}{2m}\frac{\partial^2}{\partial x^2} + \frac{1}{2}kx^2 \end{bmatrix} \psi(\mathbf{r}) = E\psi(\mathbf{r})$$

$$= \frac{1}{2}\psi(\mathbf{r})$$

$$= \frac{1}{2}\psi(\mathbf{r})$$

$$= \frac{1}{2}\psi(\mathbf{r})$$

$$= \frac{1}{2}\psi$$

$$= \frac{9}{2}\psi$$

$$= \frac{9}{2}\psi$$

$$= \frac{9}{2}\psi$$

$$= \frac{9}{2}\psi$$

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The spacings between dispersional levels are equal if the probability of the probability of

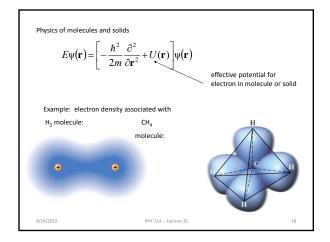
Given that f_0 =6x10¹³ cycle/s for a vibrating CO molecule, if this vibration were to couple to EM radiation, what would be the wavelength of light?

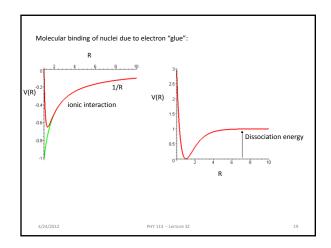
A. 5x10⁻⁶m B. 2x10

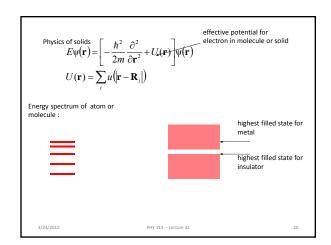
B. 2x10⁵m C. 1x10⁻⁴⁷m

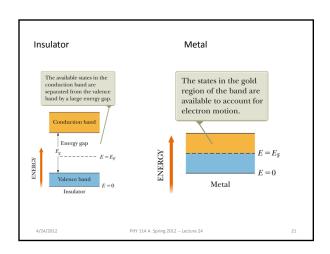
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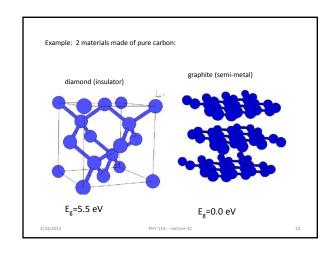
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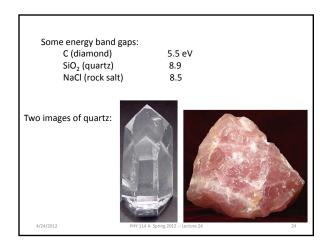


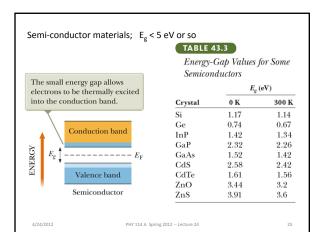












Electron conductivity in metals and semiconductors:

$$\sigma = \frac{ne^2\tau}{m^*} = ne^2\tau \frac{1}{\hbar^2} \frac{\partial^2 \varepsilon(k)}{\partial k^2}$$

 $n \equiv \# \text{ carriers/volume}$

 $\tau = \text{scattering time}$

$$\frac{1}{m^*} \equiv \frac{1}{\hbar^2} \frac{\partial^2 \varepsilon(k)}{\partial k^2}$$
 "effective mass"

In a perfect semiconductor at T=0K $\,$ n=0. To control conduction, impurities are introduced.

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