


PHY 114 A General Physics II
11 AM-12:15 PM TR Olin 101

Plan for Lecture 8 (Chapter 28):

- 1. Direct-current circuits**
- 2. Voltage and resistor circuits**
- 3. Kirchhoff's rules**

2	01/24/2012	Electric field	23.4-23.7	23.22.23.20.23.61a	01/26/2012
3	01/26/2012	Gauss's Law	24.1-24.3	24.22a.24.23.24.40	01/31/2012
4	01/31/2012	Electric potential	25.1-25.4	25.12.25.23.25.34.25.01	02/02/2012
5	02/02/2012	Electric potential	25.5-25.8	(Review for exam)	
	02/07/2012	Exam			
6	02/09/2012	Capacitance and dielectrics	26.1-26.7	26.4.26.13.26.30	02/14/2012
7	02/14/2012	Current and resistance	27.1-27.6	27.3.27.12.27.29	02/16/2012
	02/16/2012	Direct current circuits	28.1-28.2	28.3.28.7.28.19	02/21/2012
9	02/21/2012	Direct current circuits	28.3-28.5	28.23.28.25.28.34	02/23/2012
10	02/23/2012	Review	26.1-28.5	(Review for exam)	
	02/28/2012	Exam			
11	03/01/2012	Magnetic fields	29.1-29.6	29.5.29.12.29.47	03/06/2012
12	03/06/2012	Magnetic field sources	30.1-30.6		
13	03/08/2012	Faraday's law	31.1-31.5		
	03/13/2012	<i>No class (Spring Break)</i>			

Remember to send in your chapter reading questions...

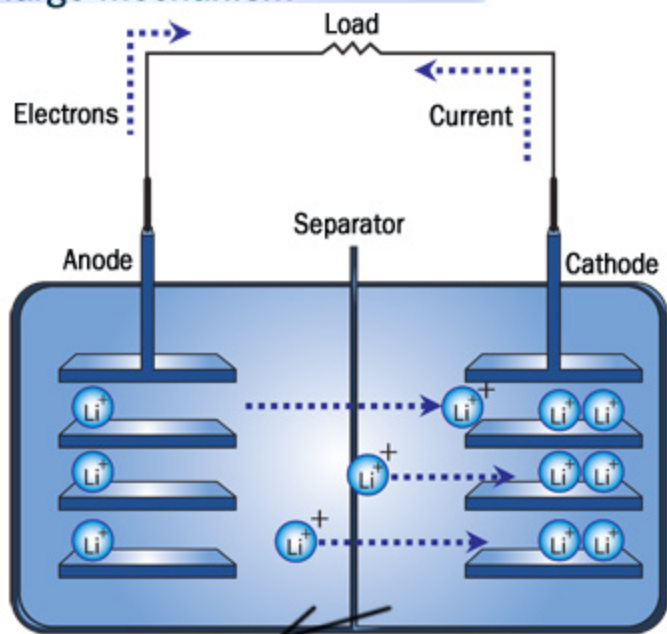
Comment on Direct current versus Alternating current

<http://www.pbs.org/wgbh/amex/edison/sfeature/acdc.html>

Example – Li ion rechargeable battery

<http://electronics.howstuffworks.com/everyday-tech/lithium-ion-battery1.htm>

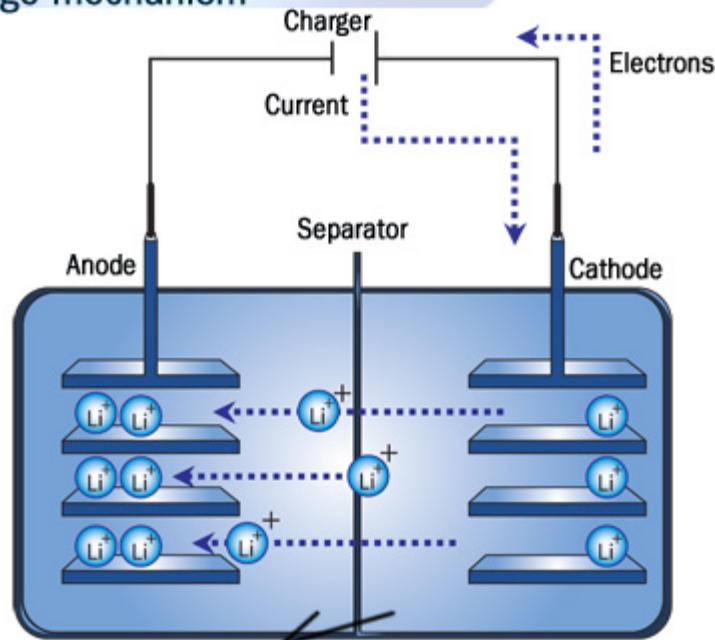
Lithium-ion rechargeable battery
Discharge mechanism



Electrolyte
(Polymer battery: gel polymer electrolyte)

©2006 HowStuffWorks

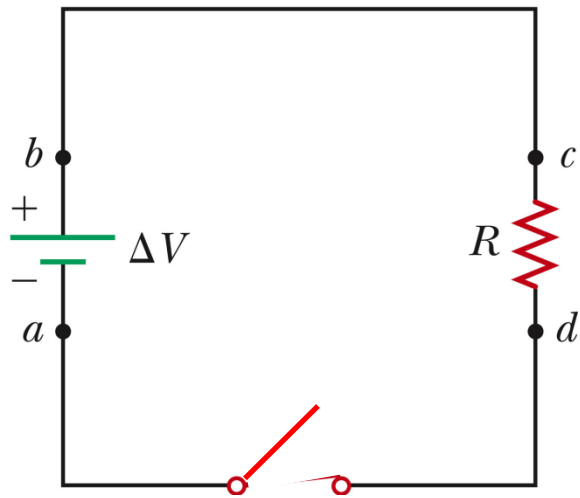
Lithium-ion rechargeable battery
Charge mechanism



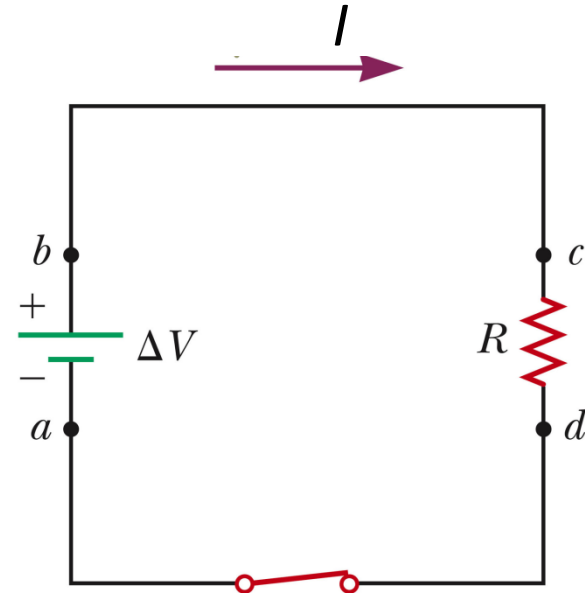
Electrolyte
(Polymer battery: gel polymer electrolyte)

©2006 HowStuffWorks

Switch open, no current flowing, battery storing energy



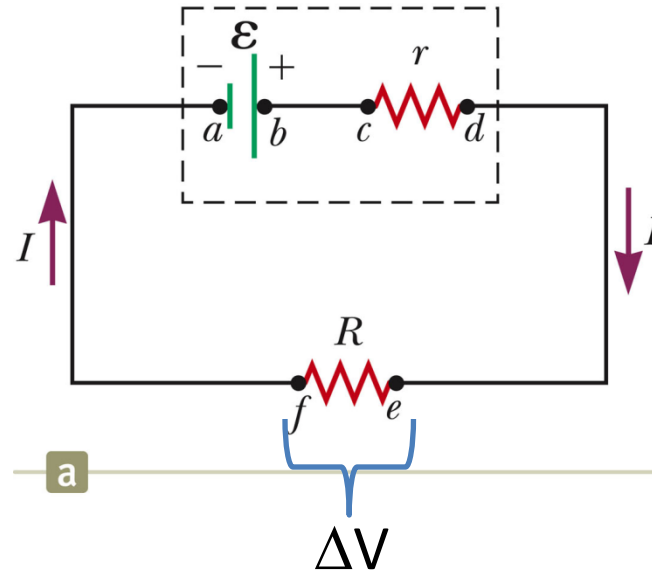
Switch closed, current flowing, battery discharging



Equivalent circuit for \mathcal{E}

$$\mathcal{E} - Ir - IR = 0$$

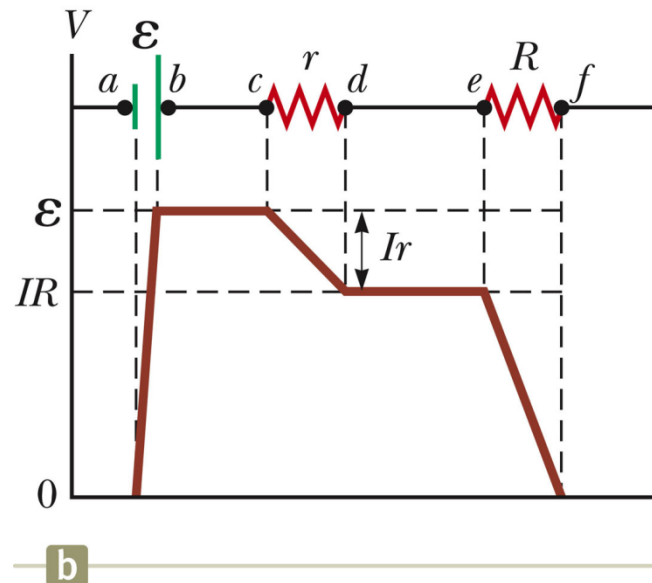
$$I = \frac{\mathcal{E}}{r + R}$$



$\mathcal{E}=12\text{V}$, $r=0.1\Omega$, $R=9.9\Omega$;

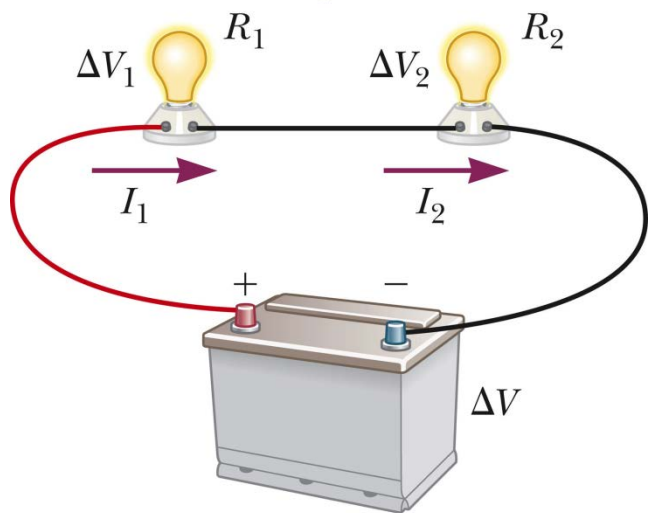
what is ΔV ?

- A. $\Delta V = \mathcal{E}$
- B. $\Delta V < \mathcal{E}$
- C. $\Delta V > \mathcal{E}$

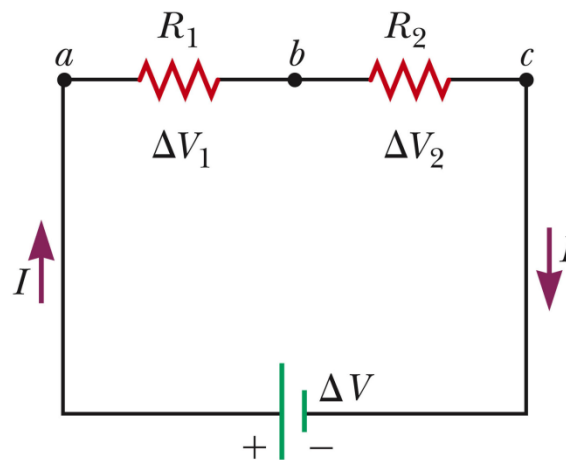


Resistors in series:

A pictorial representation of two resistors connected in series to a battery



A circuit diagram showing the two resistors connected in series to a battery



a

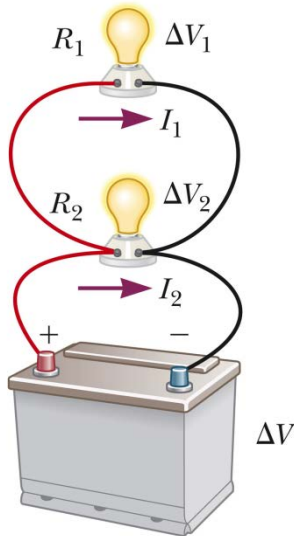
b

$$\Delta V - IR_1 - IR_2 = 0$$

$$I = \frac{\Delta V}{R_1 + R_2} \quad R_{series} = R_1 + R_2$$

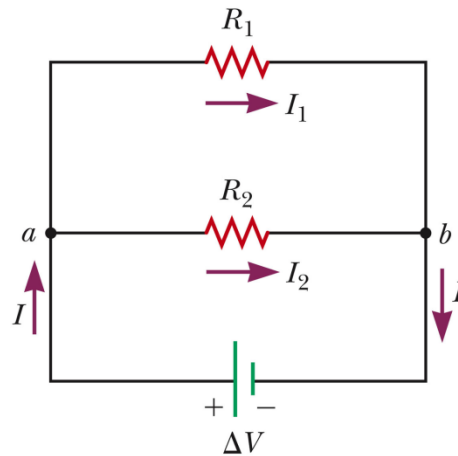
Resistors in parallel

A pictorial representation of two resistors connected in parallel to a battery



a

A circuit diagram showing the two resistors connected in parallel to a battery



b

$$\Delta V - I_1 R_1 = 0$$

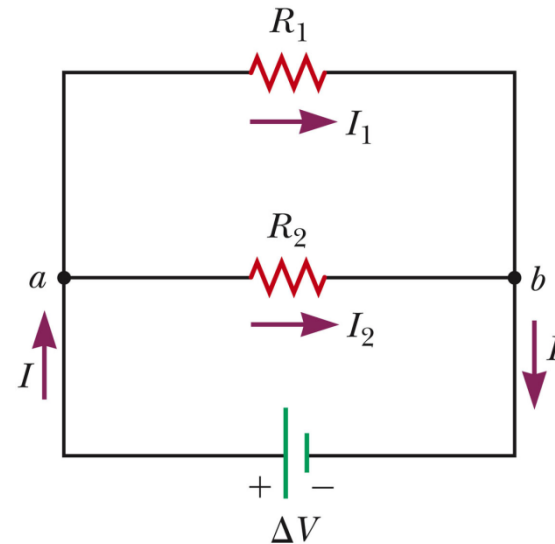
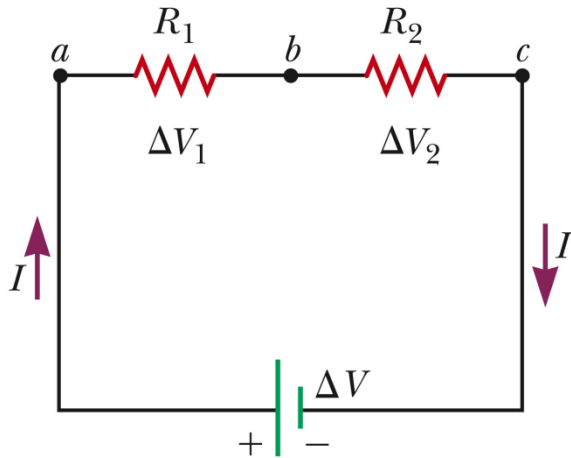
$$\Delta V - I_2 R_2 = 0$$

$$I = I_1 + I_2 = \frac{\Delta V}{R_1} + \frac{\Delta V}{R_2}$$

$$\Delta V = I \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}} \equiv IR_{Parallel}$$

$$R_{Parallel} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$$

Examples: $R_1=1\Omega$, $R_2=100\Omega$, $\Delta V=100V$



$$\Delta V - IR_1 - IR_2 = 0$$

$$I = \frac{\Delta V}{R_1 + R_2} = \frac{100}{101} = 0.99A$$

$$\Delta V_1 = IR_1 = 0.99V$$

$$\Delta V_2 = IR_2 = 99.01V$$

$$\Delta V - I_1 R_1 = 0$$

$$\Delta V - I_2 R_2 = 0$$

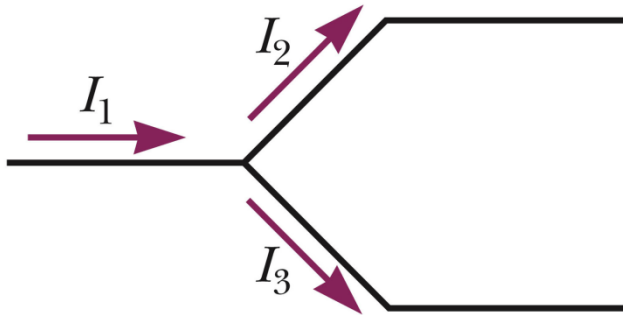
$$I_1 = \frac{\Delta V}{R_1} = \frac{100}{1} = 100A$$

$$I_2 = \frac{\Delta V}{R_2} = \frac{100}{100} = 1A$$

$$I = I_1 + I_2 = 101A$$

Circuit analysis – Kirchhoff's rules

Conservation of charge (current) at a junction:

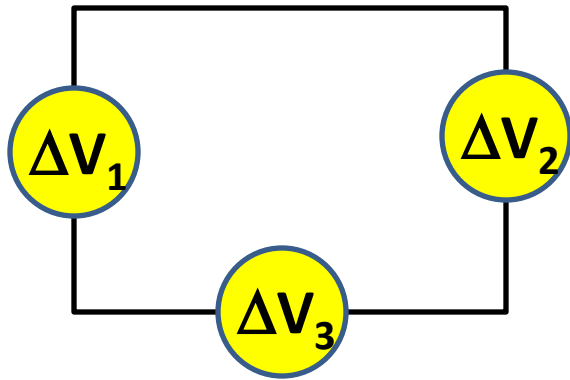


$$\sum_{\text{junction}} I = 0$$

$$I_1 - I_2 - I_3 = 0$$

Circuit analysis – Kirchhoff's rules

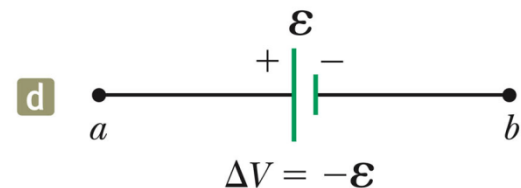
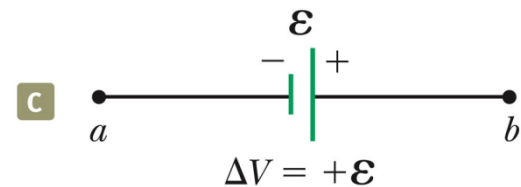
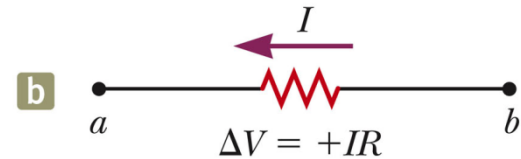
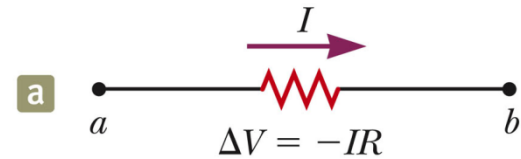
Conservation of potential around a closed circuit:



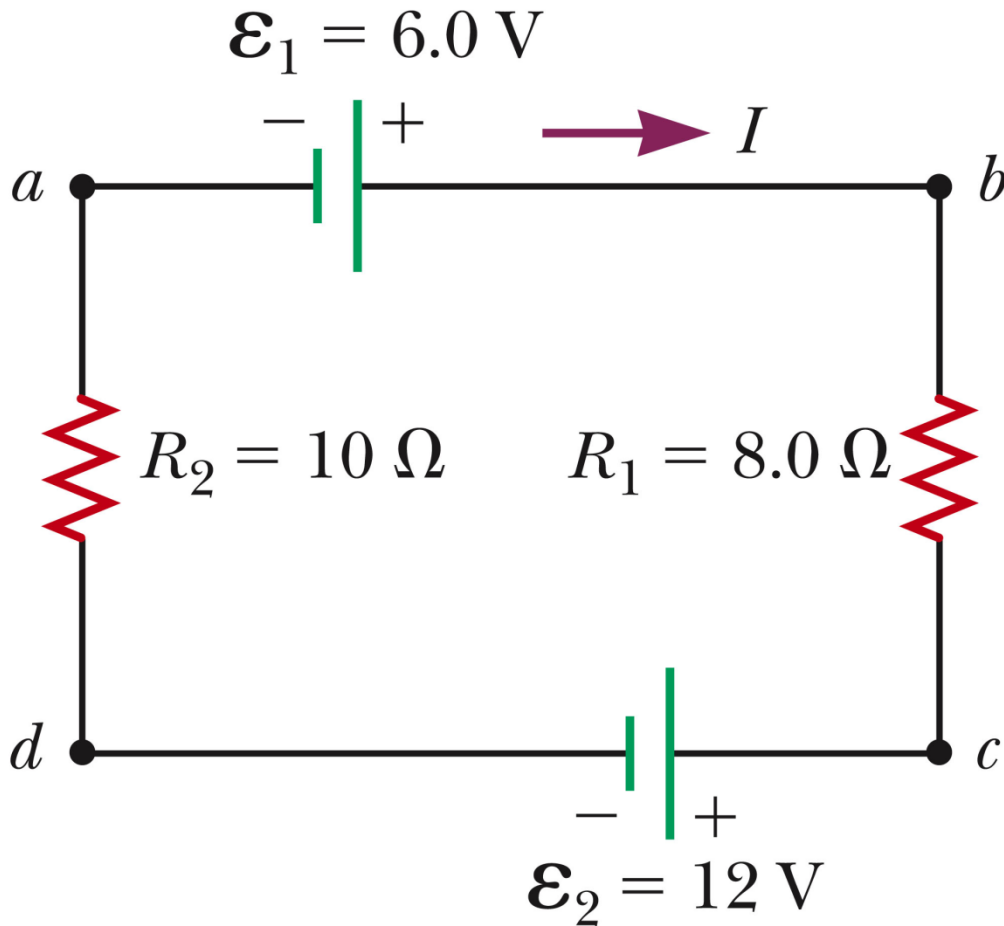
$$\sum_{\text{closed loop}} \Delta V = 0$$

$$\Delta V_1 + \Delta V_2 + \Delta V_3 = 0$$

Sign conventions: $\Delta V = V_b - V_a$



Example:



$$\mathcal{E}_1 - IR_1 - \mathcal{E}_2 - IR_2 = 0$$

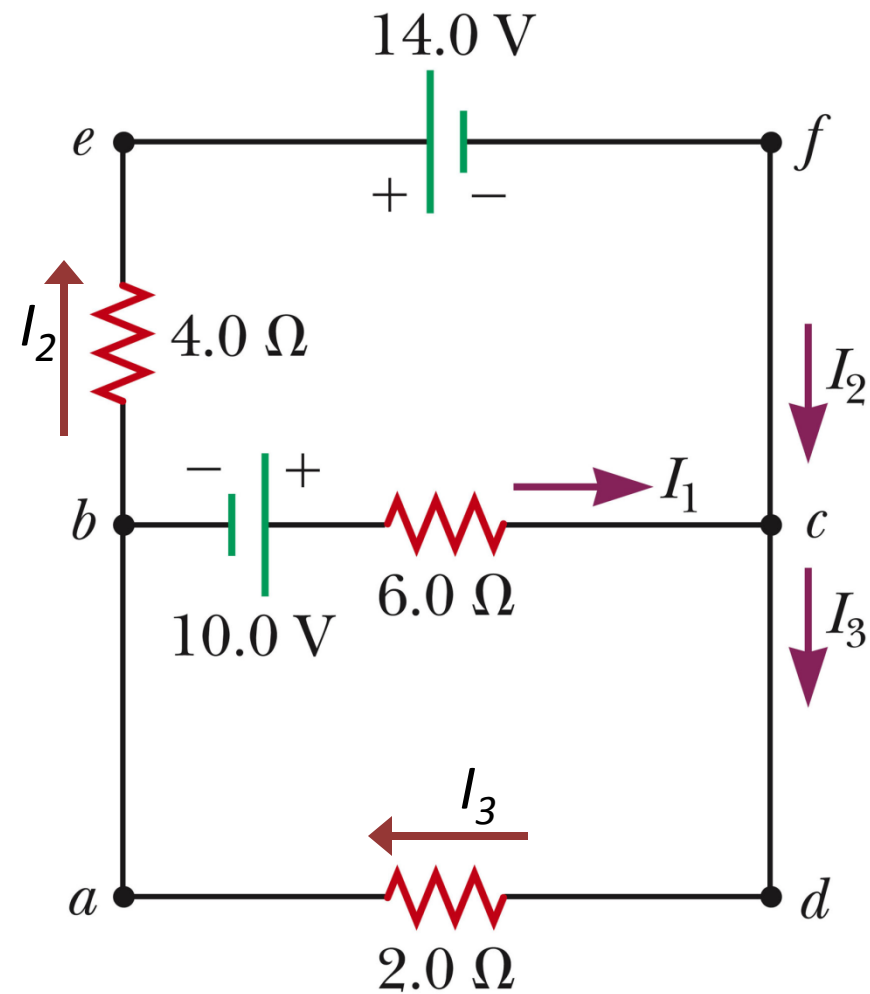
Solve for I :

$$I = \frac{\mathcal{E}_1 - \mathcal{E}_2}{R_1 + R_2} = \frac{6 - 12}{8 + 10} = -0.33 \text{ A}$$

$I < 0$ means:

- A. The circuit is wrong (cannot exist or will blow up).
- B. The current flows opposite the arrow.

Example:



$$-14 - 2I_3 - 4I_2 = 0$$

$$10 - 6I_1 - 2I_3 = 0$$

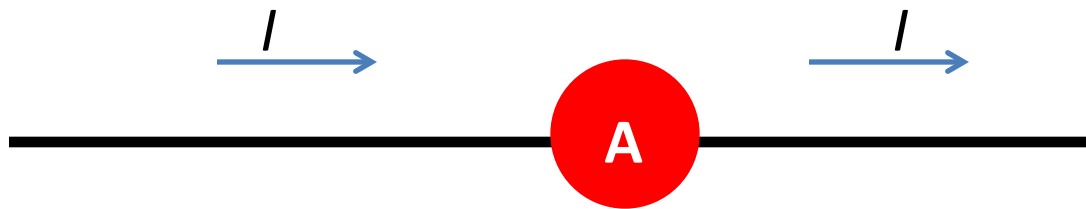
$$I_1 + I_2 = I_3$$

$$I_1 = 2\text{ A}$$

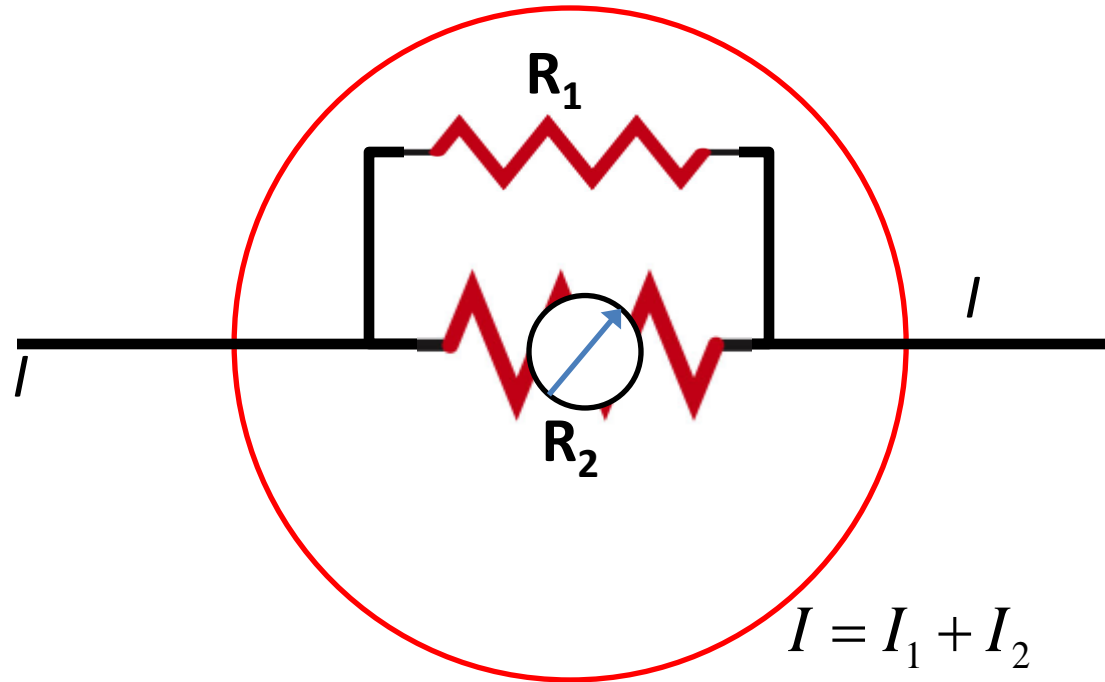
$$I_2 = -3\text{ A}$$

$$I_3 = -1\text{ A}$$

How to measure current



Inside ammeter:

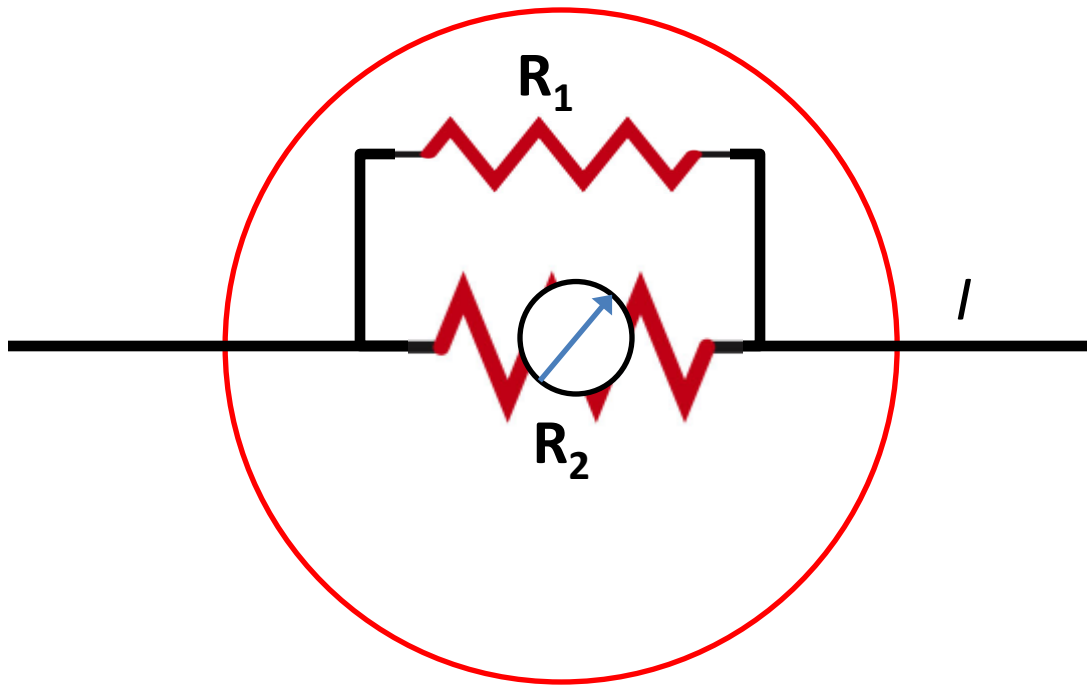


$I_1 \equiv$ "shunt" current; $R_1 \ll R_2$

$I_2 \equiv$ device current; $I_2 \ll I_1$

$$I = I_1 + I_2$$

$$R_{eq} = \frac{1}{\frac{1}{R_1} + \frac{1}{R_2}}$$



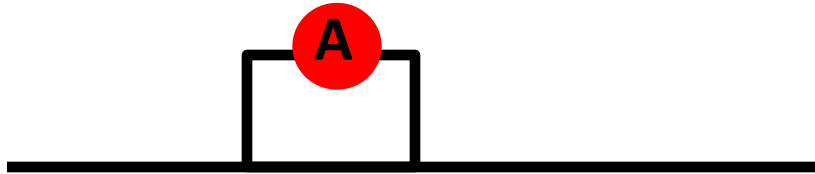
Suppose that :

$$I = 10A, R_1 = 0.01\Omega, R_2 = 100\Omega$$

$$I_2 = \frac{I}{1 + \frac{R_2}{R_1}} = \frac{10}{10001} A = 0.001A$$

➔ Current that drives measurement device.

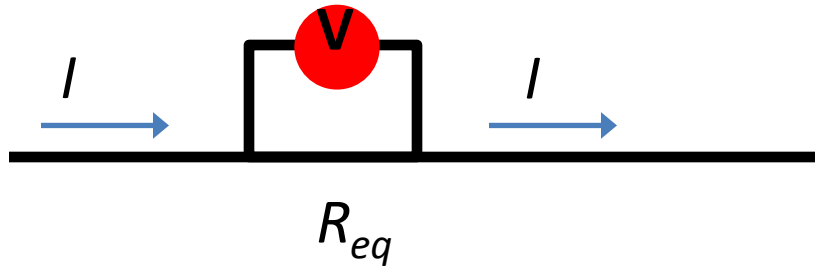
What if the ammeter were connected in parallel to the wire?
(Assume that the wire resistance is $R_w = 0.001\Omega$.)



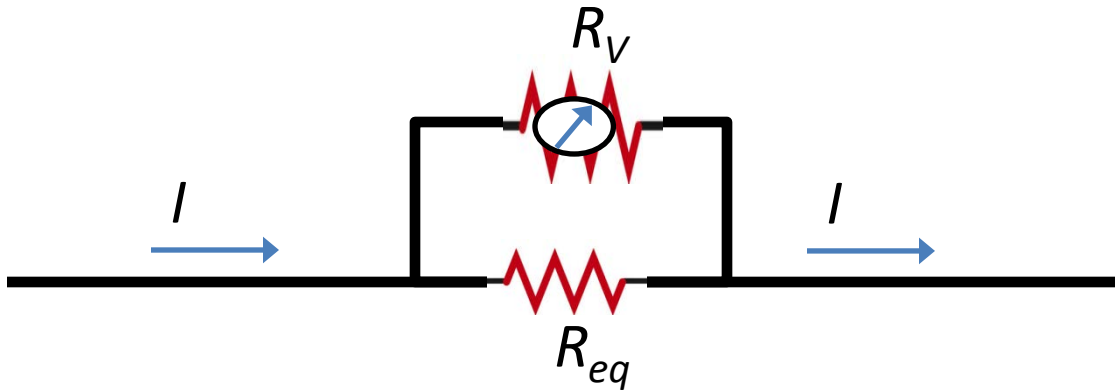
- A. The measurement would be identical to series result.
- B. The measurement would be less than the series result.
- C. The measurement would be greater than the series result.

$$I_2 = \frac{I}{1 + \frac{R_2}{R_1} + \frac{R_2}{R_w}} = \frac{10}{110001} A = 0.0001A$$

How to measure voltage



Total equivalent circuit:

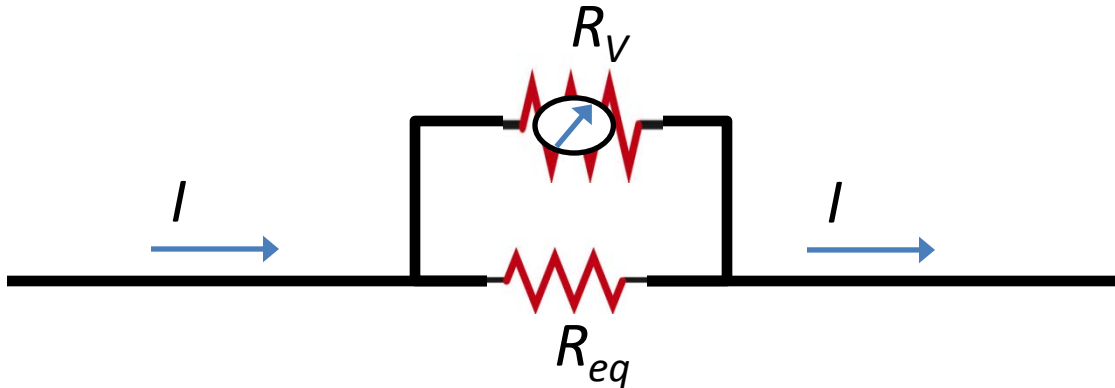


$$I_V R_V = \frac{I R_{eq}}{1 + \frac{R_{eq}}{R_V}}$$

\Rightarrow Works well if

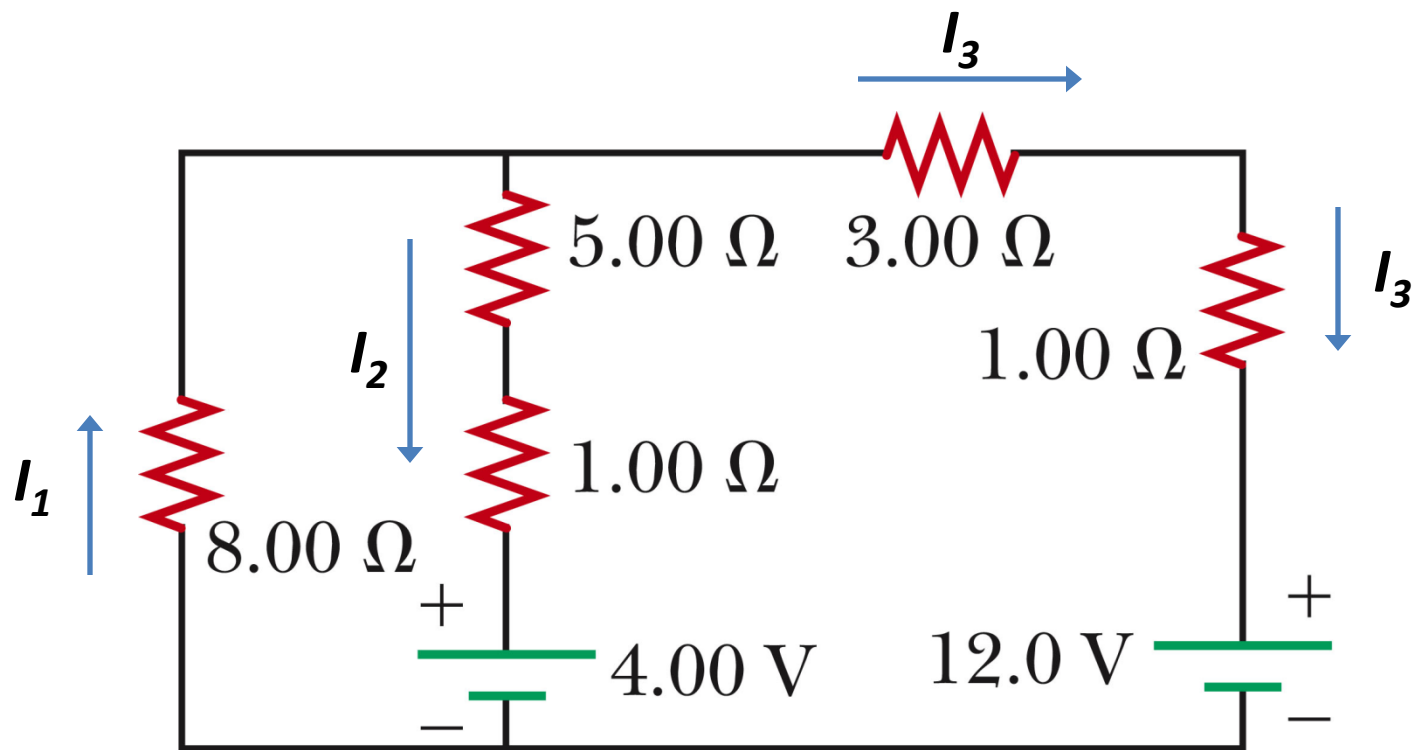
$$R_V \gg R_{eq}$$

Total equivalent circuit: Suppose $I=10\text{A}$, $R_{eq}=10\Omega$, $R_V=100\Omega$



$$I_V R_V = \frac{10 \times 100}{1 + \frac{10}{100}} = 909.1$$

$$\frac{I R_{eq} - I_V R_V}{I R_{eq}} = 9\%$$



3 unknowns \rightarrow need 3 equations

$$I_1 = I_2 + I_3$$

$$-8I_1 - 6I_2 - 4 = 0$$

$$-4I_3 - 12 - 8I_1 = 0$$

$$-4I_3 - 12 + 4 + 6I_2 = 0$$