

**Math 732 Assignment #1**  
**Due: Wednesday, January 23, 2013**

Submit full answers to the Required Problems. Remember to use complete sentences and proper grammar when writing a solution. Include sketches wherever appropriate.

**Required Problems**

G&P section 1.1: 4, 12, 18

For 12 on *stereographic projection*, you should derive the following formulas. If  $(x, y, z)$  is a point on the sphere, show that

$$\pi(x, y, z) = \left( \frac{x}{1-z}, \frac{y}{1-z} \right).$$

Show that the inverse map  $\pi^{-1}$  applied to a point  $(u, v)$  in the plane satisfies

$$\pi^{-1}(u, v) = \left( \frac{2u}{u^2 + v^2 + 1}, \frac{2v}{u^2 + v^2 + 1}, \frac{u^2 + v^2 - 1}{u^2 + v^2 + 1} \right).$$

*n.b.*, there are typos in problems 4 and 18. In 4, the ball  $B_a = \{x : |x| < a\}$ . In 18, the function  $g(x) = f(x - a)f(b - x)$ .

**Additional Problems** – you may submit these for feedback; if you do, please indicate on the top of your first page. We will discuss these in the problem session.

G&P section 1.1: 3, 8, 9, 11