

A particle in the harmonic oscillator potential has the initial wave function

$$\Psi(x,0) = A[u_0(x) + u_1(x)]$$

for some constant, A.

- (a) Normalize  $u_0(x)$ .
- (b) Use the raising operator to get  $u_1(x)$ .
- (c) Normalize  $\Psi(x,0)$ .
- (d) Find  $\Psi(x,t)$  and  $|\Psi(x,t)|^2$ .
- (e) Find the expectation value of  $x$  as a function of time. Notice that it oscillates sinusoidally. What is the amplitude of oscillation? What is the (angular) frequency?
- (f) Use your result in (e) to determine  $\langle p \rangle$ . Check that Ehrenfest's equation,
$$\frac{d\langle p \rangle}{dt} = -\langle dV/dx \rangle,$$
holds for this wave function.
- (g) Graph/animate  $|\Psi(x,t)|^2$  from  $t = 0$  to  $t = (4\pi/\omega)$  using Maple. You can use the one for the double well as a template.