

Physics 745 - Group Theory  
Homework Set 30  
Due Wednesday, April 20

1. The mass of the  $\Omega^-$  can be predicted in terms of the parameters  $a$  and  $b$  from eq. (4.36).
  - (a) Find the formula for the  $\Omega^-$  mass in terms of  $a$  and  $b$ .
  - (b) Comparing with some of the other formulas, write a formula for the  $\Omega^-$  mass in terms of some combination of the  $\Delta$ ,  $\Sigma^*$  and/or  $\Xi^*$  masses. There is more than one correct answer to this part.
  - (c) Check against the experimental value  $m_\Omega = 1672 \text{ MeV}/c^2$ .
  
2. Equation (4.40) is not complete – it doesn't show where all the indices go
  - (a) Write this equation correctly, with all the indices eliminated. You will have to have *three* coefficients in this case, which I called  $a$ ,  $b$ , and  $c$ .
  - (b) Find an equation for each of the masses  $m_K^2$ ,  $m_{\bar{K}}^2$ ,  $m_\pi^2$ , and  $m_\eta^2$  in terms of  $a$ ,  $b$ , and  $c$ .
  - (c) Find a linear equation relating these four masses, *i.e.*, eliminate  $a$ ,  $b$ , and  $c$ . Arrange it so only positive coefficients appear on each side of the equation. Check it numerically
  - (d) An identical relationship should exist for the four masses (not masses squared) for the octuplet baryons. Check it numerically as well.