

Math 112

Quiz #4

Compute the following indefinite integrals. You must show all work to receive full credit.

1. $\int \frac{Ax}{B+Cx^2} dx.$

$$\int \frac{Ax}{B+Cx^2} dx = A \int \frac{x}{B+Cx^2} dx$$

Let $u = B+Cx^2$. Then,
 $du = 2Cx dx$

$$\Rightarrow \int \frac{Ax}{B+Cx^2} dx = \frac{A}{2C} \int \frac{1}{u} du = \frac{A}{2C} \ln(|u|) + C = \frac{A}{2C} \ln(|B+Cx^2|) + C$$

2. $\int \frac{A}{B^2+x^2} dx.$

$$\int \frac{A}{B^2+x^2} dx = \frac{A}{B^2} \int \frac{1}{1+(\frac{x}{B})^2} dx$$

Let $u = \frac{x}{B}$. Then,

$$du = \frac{1}{B} dx$$

$$\Rightarrow B du = dx$$

$$\begin{aligned} \Rightarrow \int \frac{A}{B^2+x^2} dx &= \frac{A}{B} \int \frac{1}{1+u^2} du \\ &= \frac{A}{B} \tan^{-1}\left(\frac{x}{B}\right) + C. \end{aligned}$$

