

## Announcements

1. Read Chapter 9 – notion of impulse and momentum
2. Feedback questionnaire
3. Tutorials?

Review -- Work-Kinetic energy theorem:

$$W_{total}^{i \rightarrow f} = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2$$

Analyzing work in terms of “conservative” and “non-conservative”:

$$W_{total}^{i \rightarrow f} = W_{conservative}^{i \rightarrow f} + W_{non-conservative}^{i \rightarrow f} = U(\mathbf{r}_i) - U(\mathbf{r}_f) + W_{non-conservative}^{i \rightarrow f}$$

Rearranging terms to form total mechanical energy:

$$\frac{1}{2}mv_f^2 + U(\mathbf{r}_f) = \frac{1}{2}mv_i^2 + U(\mathbf{r}_i) + W_{non-conservative}^{i \rightarrow f}$$

Statement of conservation of energy: If  $W_{non-conservative}^{i \rightarrow f} = 0$

$$E_{mechanical} = \frac{1}{2}mv^2 + U(\mathbf{r}) = (\text{constant}); \Rightarrow \frac{dE_{mech}}{dt} = 0$$

A new way to look at Newton's second law:

$$\mathbf{F} = m\mathbf{a} = m \frac{d\mathbf{v}}{dt} = \frac{d(m\mathbf{v})}{dt} \equiv \frac{d\mathbf{p}}{dt}$$

Define linear momentum  $\mathbf{p} = m\mathbf{v}$

Consequences:

1. If  $\mathbf{F} = 0 \quad \Rightarrow \quad \frac{d\mathbf{p}}{dt} = 0 \quad \Rightarrow \quad \mathbf{p} = \text{constant}$

2. Notion of impulse:  $d\mathbf{p} = \mathbf{F}dt$

$$\int_i^f d\mathbf{p} = \Delta\mathbf{p}_{i \rightarrow f} = \int_i^f \mathbf{F}dt$$

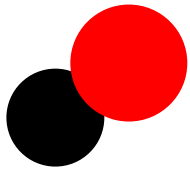
Conservation of (linear) momentum:

$$\text{If } \frac{d\mathbf{p}}{dt} = \mathbf{F} = 0 \quad , \quad \mathbf{p} = \text{constant}$$

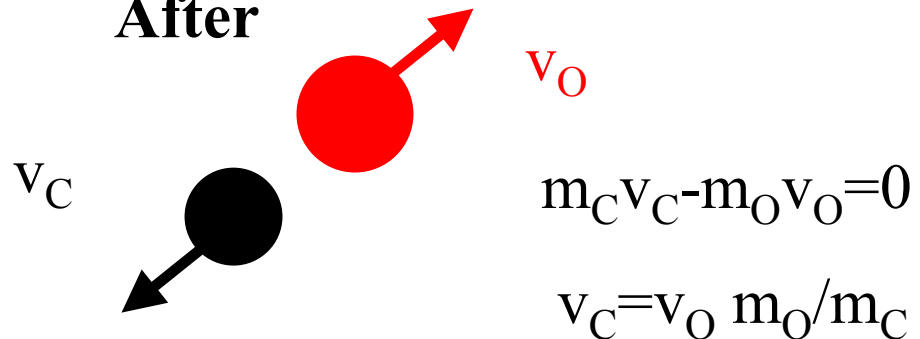
Example:

Suppose a molecule of CO is initially at rest, and it suddenly decomposes into separate C and O atoms. In this process the chemical binding energy  $E_0$  is transformed into mechanical energy of the C and O atoms. What can you say about the motion of these atoms after the decomposition?

**Before**



**After**



Further analysis:

$$E_0 = \frac{1}{2} m_C v_C^2 + \frac{1}{2} m_O v_O^2 = \frac{1}{2} m_C v_C^2 (1 + m_C/m_O)$$

$$\rightarrow \frac{1}{2} m_C v_C^2 = E_0/(1 + m_C/m_O) \sim E_0/(1 + 12/16) = 4/7 E_0$$

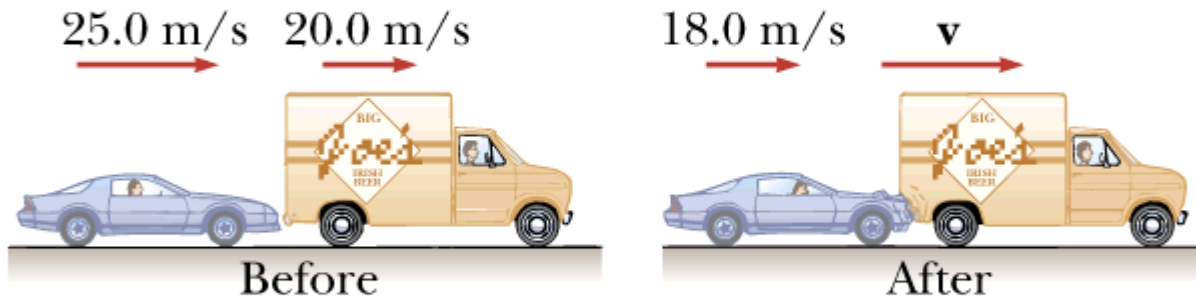
$$\rightarrow \frac{1}{2} m_O v_O^2 \sim 3/7 E_0$$

Extra credit opportunity:

Work through the details of the above analysis and verify the results for yourself ( perhaps with a different diatomic molecule).

## Another example from homework set:

Serway, Physics for Scientists and Engineers, 5/e  
Problem 9.21



In this case, mechanical energy is not conserved. (Where does it go?) However, to our level of approximation, we will assume that momentum is conserved.

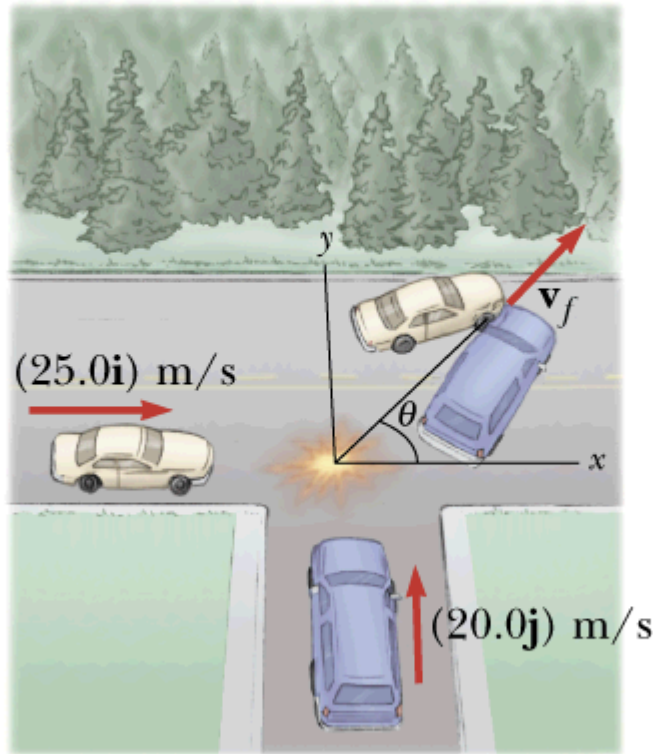
Before:

After:

$$m_c v_{0c} + m_T v_{0T} = m_c v_c + m_T v$$

Note: In general, momentum is a **vector** quantity.

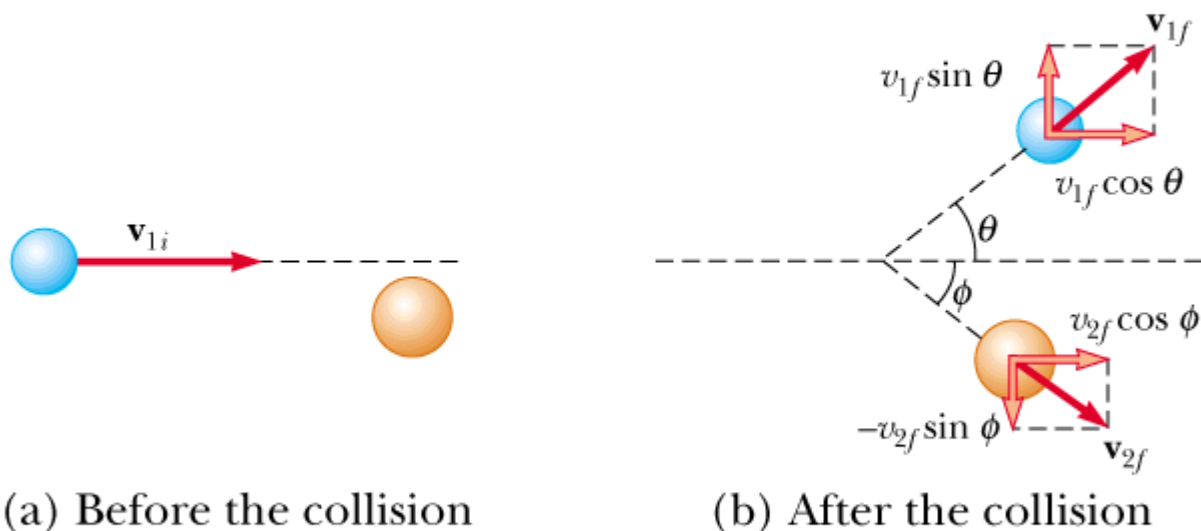
Serway, Physics for Scientists and Engineers, 5/e  
Figure 9.15



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$$m_c \mathbf{v}_{0c} + m_T \mathbf{v}_{0T} = (m_c + m_T) \mathbf{v}_f$$

$$\mathbf{v}_f = \frac{m_c}{m_c + m_T} v_{0c} \mathbf{i} + \frac{m_T}{m_c + m_T} v_{0T} \mathbf{j}$$



Statement of conservation of momentum:

$$m_1 v_{1i} = m_1 v_{1f} \cos \theta + m_2 v_{2f} \cos \phi$$

$$0 = m_1 v_{1f} \sin \theta - m_2 v_{2f} \sin \phi$$

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If mechanical (kinetic) energy is conserved, then:

$$\frac{1}{2} m_1 v_{1i}^2 = \frac{1}{2} m_1 v_{1f}^2 + \frac{1}{2} m_2 v_{2f}^2$$



### Peer instruction question:

Given the previous example, summarized with these equations:

$$\begin{aligned} m_1 v_{1i} &= m_1 v_{1f} \cos \theta + m_2 v_{2f} \cos \varphi & \frac{1}{2} m_1 v_{1i}^2 &= \frac{1}{2} m_1 v_{1f}^2 + \frac{1}{2} m_2 v_{2f}^2 \\ 0 &= m_1 v_{1f} \sin \theta - m_2 v_{2f} \sin \varphi \end{aligned}$$

which of the following statements are true?

- (a) It is in principle possible to solve the above equations uniquely.
- (b) It is not possible to solve the above equations uniquely because the mathematics is too difficult.
- (c) It is not possible to solve the above equations uniquely because there is missing physical information.