

## Announcements

1. WebAssign count will be done on 9/6/02.
2. Zac Caulder (please see me after class)
3. On line quizzes and homework assignments. (Quiz  $q_N$  is due before lecture  $N$  and  $HW_N$  is due before lecture  $N+1$ .) Due time extended to 5 PM the day of the lecture???
4. How are the tutorials? Other feedback?

## Vector manipulations

1. Definition
2. Addition, subtraction, multiplication
3. Examples

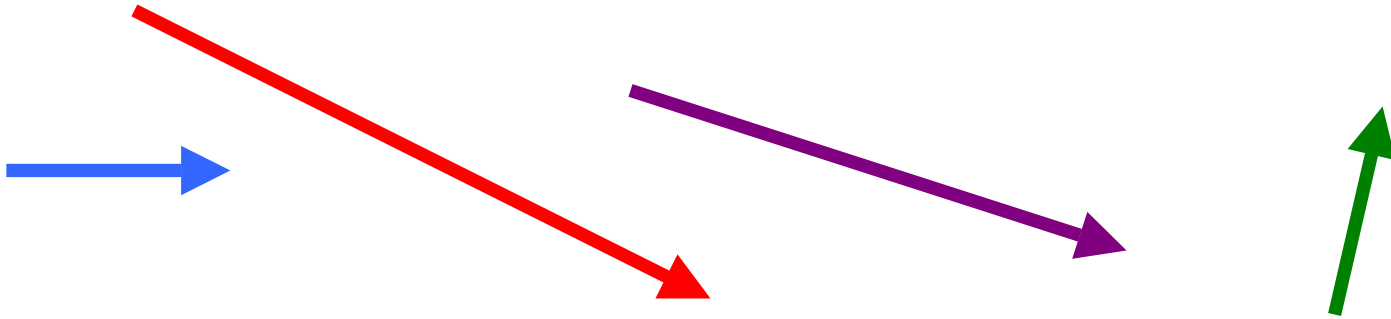
## On line quiz

Suppose that receive information from a reliable source that there is buried treasure located 30 m East and 40 m South of your dorm room. Starting at your dorm room, which of the following method(s) will get you to the treasure?

- (a) You should walk 70 m in the Southeast direction.
- (b) You should walk first 30 m East and then 40 m South.
- (c) You should walk first 40 m South and then 30 m East.
- (d) You should walk walk 50 m in a direction 53.1 degrees South of East.
- (e) You should walk walk 50 m in a direction 36.9 degrees South of East.

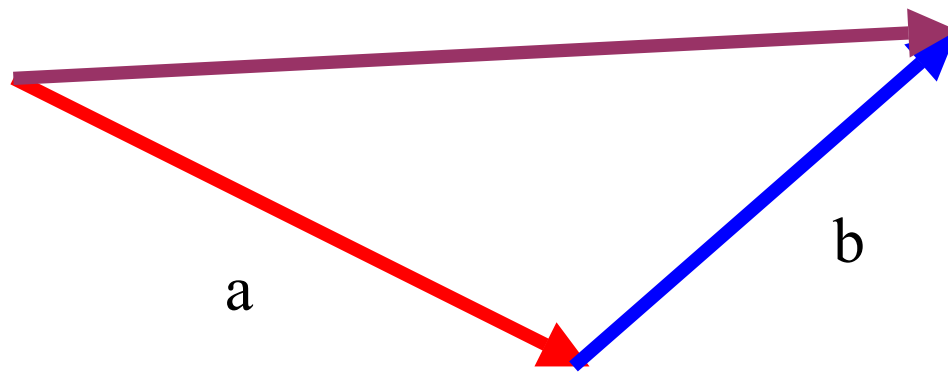
## Definition of a vector

1. A vector can be visualized its length and direction.

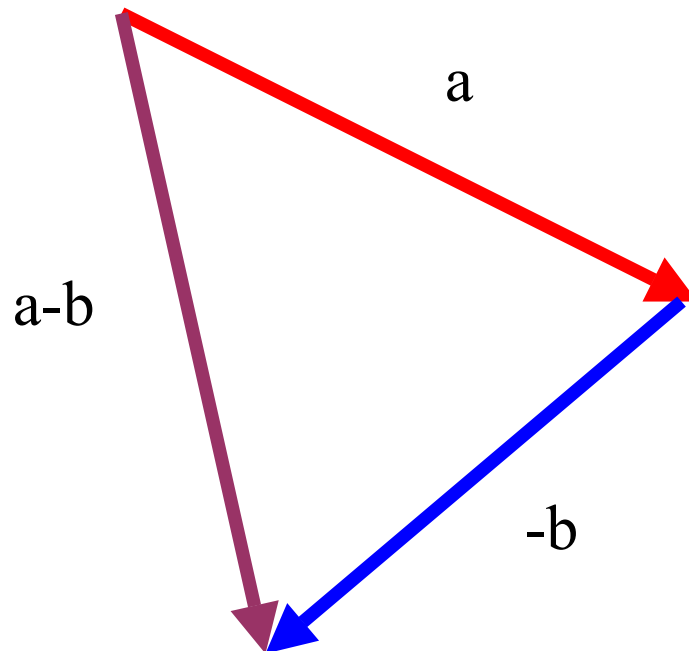


2. Addition, subtraction, and two forms of multiplication can be defined
3. Coordinate representations, and abstract extensions.

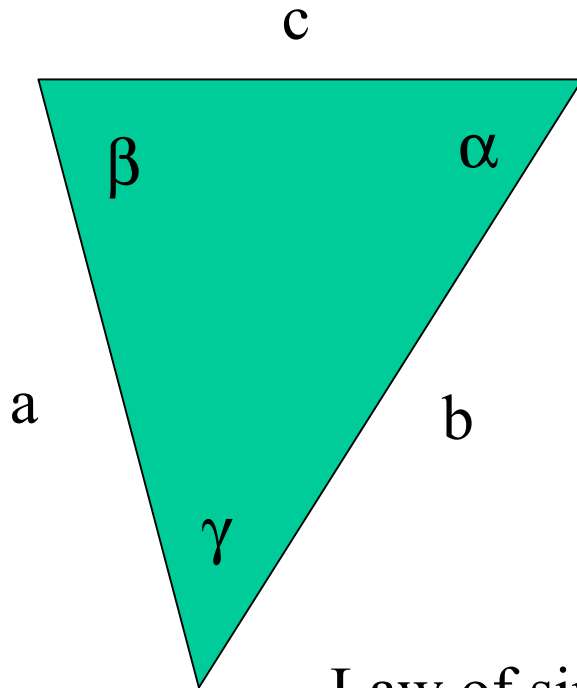
Vector addition:



Vector subtraction:



## Some useful trigonometric relations



Law of cosines:

$$a^2 = b^2 + c^2 - 2bc \cos \alpha$$

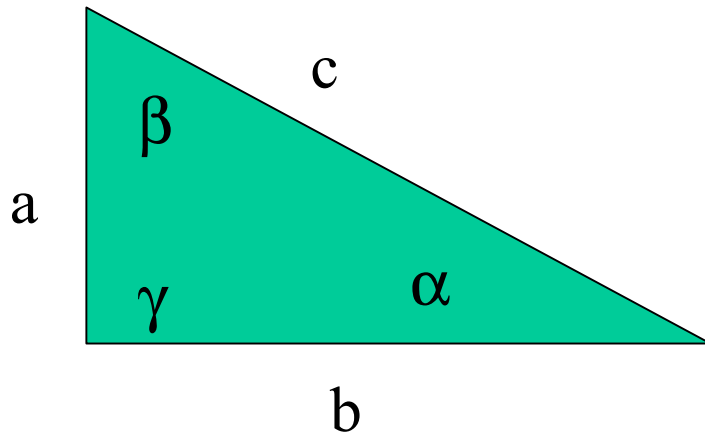
$$b^2 = c^2 + a^2 - 2ca \cos \beta$$

$$c^2 = a^2 + b^2 - 2ab \cos \gamma$$

Law of sines:

$$\frac{a}{\sin \alpha} = \frac{b}{\sin \beta} = \frac{c}{\sin \gamma}$$

## Right triangle relations



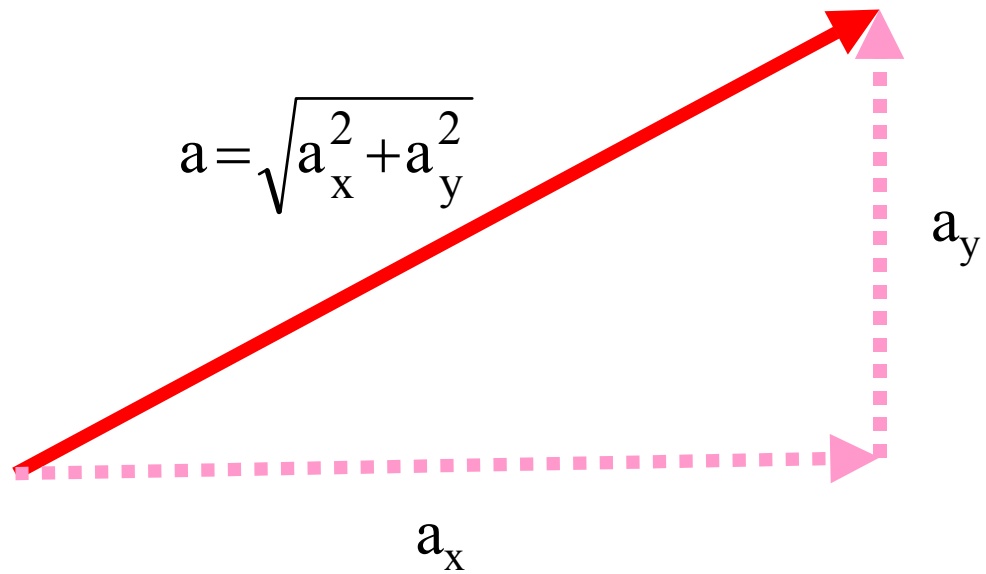
$$c = \sqrt{a^2 + b^2}$$

$$\tan \alpha = a/b$$

$$\sin \alpha = a/c$$

$$\cos \alpha = b/c$$

Vector components:



## Vector components

$$\mathbf{R}_1 = x_1 \hat{\mathbf{x}} + y_1 \hat{\mathbf{y}} + z_1 \hat{\mathbf{z}}$$

$$\mathbf{R}_2 = x_2 \hat{\mathbf{x}} + y_2 \hat{\mathbf{y}} + z_2 \hat{\mathbf{z}}$$

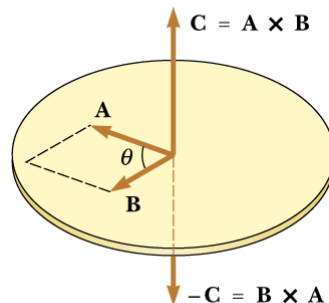
$$\mathbf{R}_1 + \mathbf{R}_2 = (x_1 + x_2) \hat{\mathbf{x}} + (y_1 + y_2) \hat{\mathbf{y}} + (z_1 + z_2) \hat{\mathbf{z}}$$

## Vector multiplication

“Dot” product  $\mathbf{A} \bullet \mathbf{B} \equiv AB \cos \theta_{AB}; \quad \hat{\mathbf{x}} \bullet \hat{\mathbf{x}} = 1$

“Cross” product  $|\mathbf{A} \times \mathbf{B}| \equiv AB \sin \theta_{AB}; \quad \hat{\mathbf{x}} \times \hat{\mathbf{y}} = \hat{\mathbf{z}}$

Serway, Physics for Scientists and Engineers, 5/e  
Figure 11.8



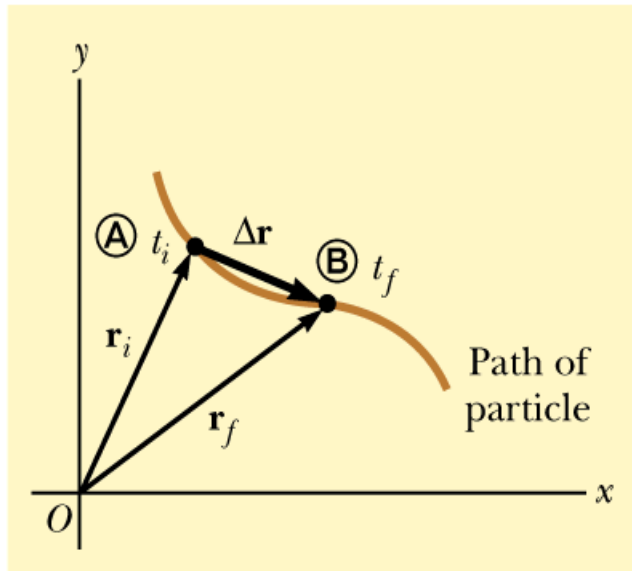
Right-hand rule



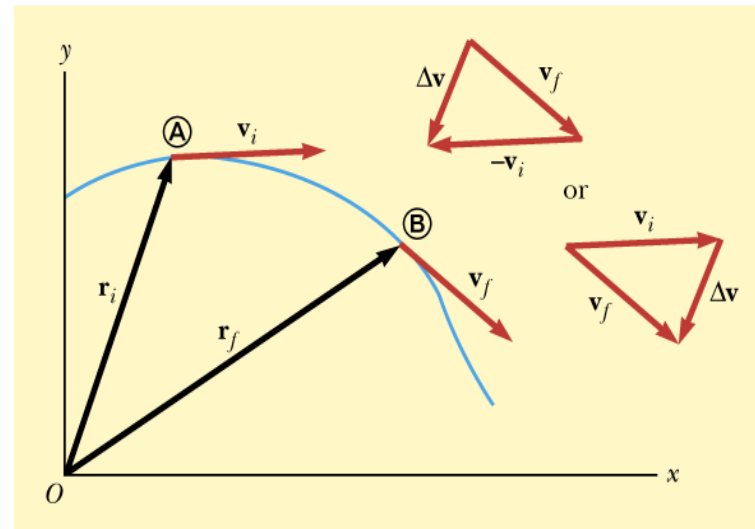


# Examples of vectors: Position & Velocity

Serway, Physics for Scientists and Engineers, 5/e  
Figure 4.1

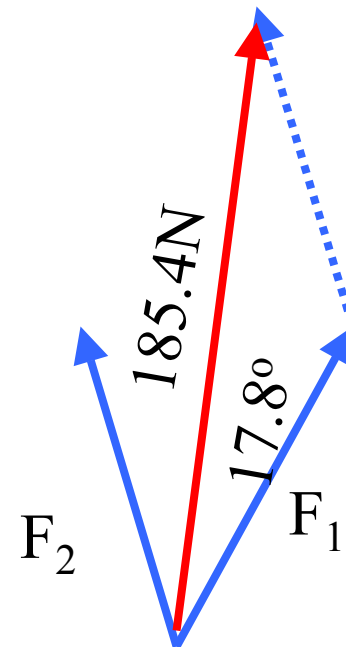
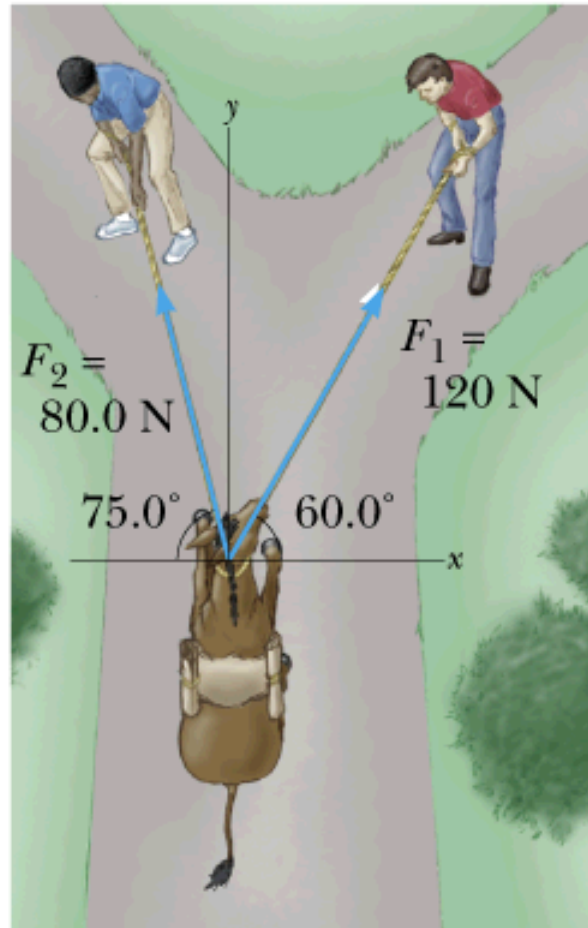


Serway, Physics for Scientists and Engineers, 5/e  
Figure 4.3



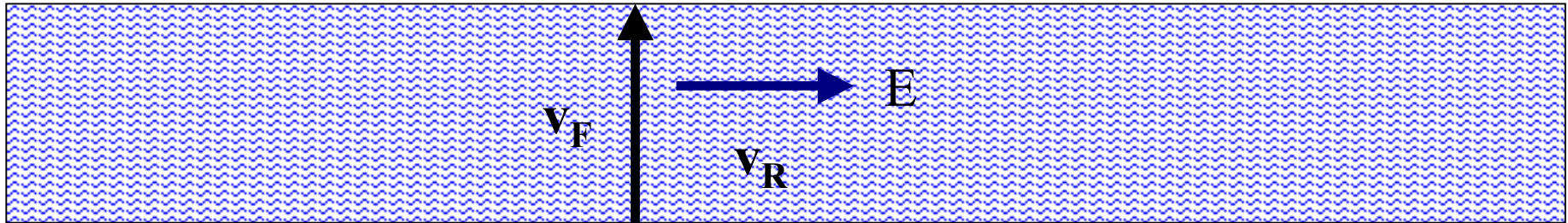
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## Peer instruction question

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Suppose a Ferry moves due *north* at  $\mathbf{v}_F=4\text{m/s}$  across a river which is flowing *east* at a velocity of  $\mathbf{v}_R=3\text{m/s}$ . What is the velocity of the Ferry relative to the water?

- (a)  $4\text{m/s}$  (north)   (b)  $7\text{m/s}$   $37^\circ$ (east of north)  
(c)  $5\text{m/s}$   $37^\circ$ (east of north)   (d)  $5\text{m/s}$  (west of north)